

CLEO-c Measurements of Purely Leptonic Decays of Charmed Mesons

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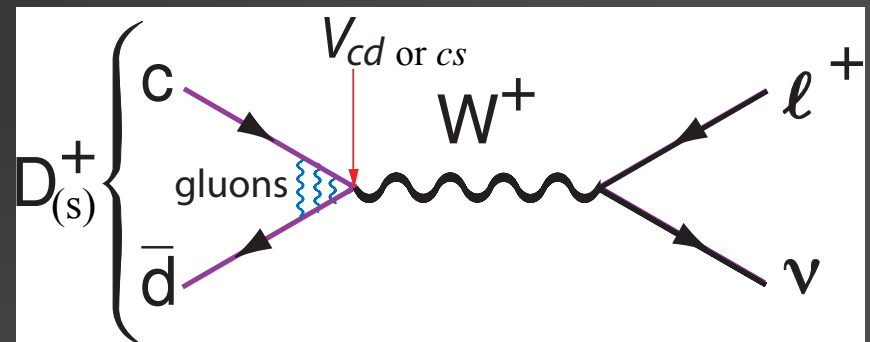


Leptonic Decays: $D \rightarrow \ell^+ \nu$

Introduction: Pseudoscalar decay constants

c and \bar{q} can annihilate, probability is \propto to wave function overlap

Example :



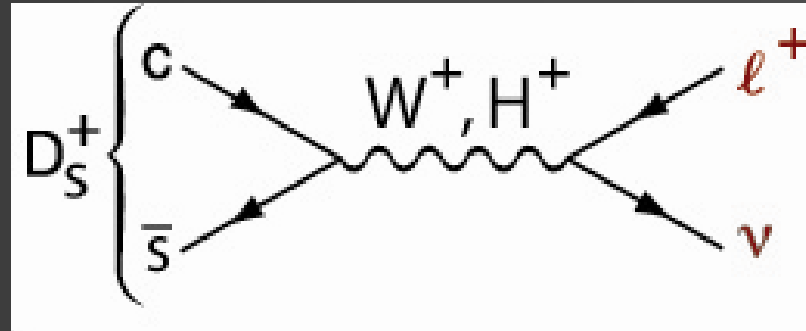
In general for all pseudoscalars:

$$\Gamma(P^+ \rightarrow \ell^+ \nu) = \frac{1}{8\pi} G_F^2 f_P^2 m_\ell^2 M_P \left(1 - \frac{m_\ell^2}{M_P^2}\right)^2 |V_{Qq}|^2$$

Calculate, or measure if V_{Qq} is known

New Physics Possibilities

- Besides the obvious interest in comparing with Lattice & other calculations of f_P there are NP possibilities



- Another Gauge Boson could mediate decay
- Ratio of leptonic decays could be modified e.g. in Standard Model

$$\frac{\Gamma(P^+ \rightarrow \tau^+ \nu)}{\Gamma(P^+ \rightarrow \mu^+ \nu)} = m_\tau^2 \left(1 - \frac{m_\tau^2}{M_P^2}\right)^2 / m_\mu^2 \left(1 - \frac{m_\mu^2}{M_P^2}\right)^2$$

See Hewett [hep-ph/9505246] & Hou, PRD 48, 2342 (1993).

- If H^\pm couples to $M^2 \Rightarrow$ no effect

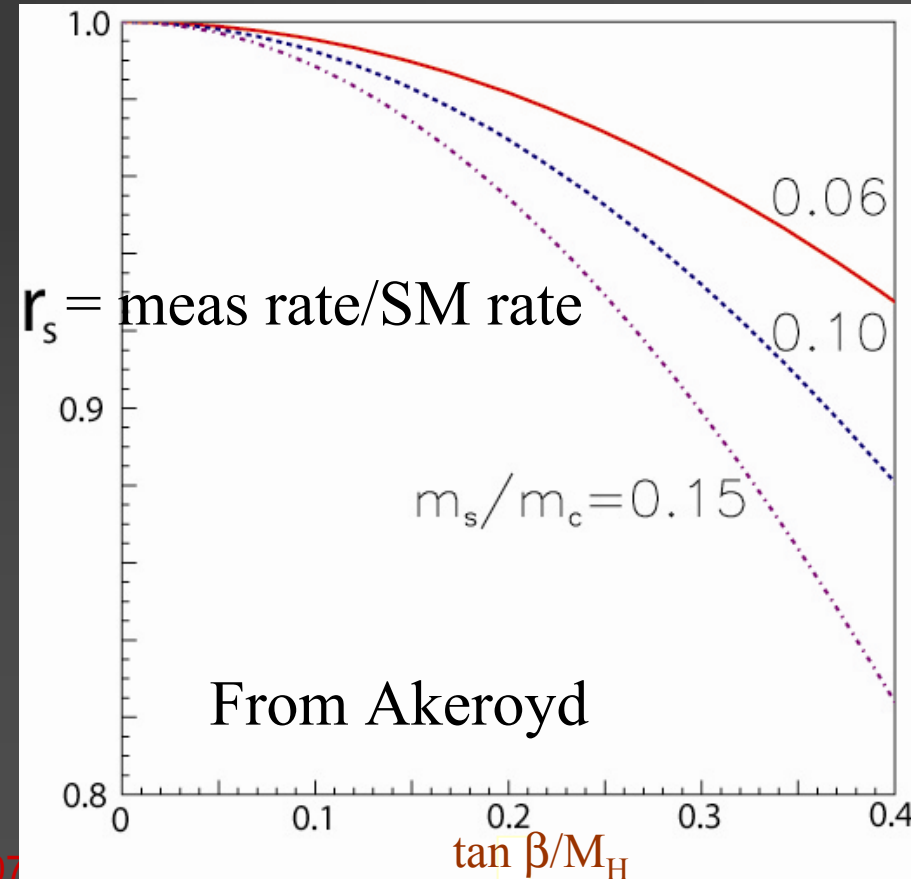
New Physics Possibilities II

- Leptonic decay rate is modified by H^\pm
- Can calculate in SUSY as function of m_q/m_c ,
- In 2HDM predicted decay width is x by

$$r_q = \left[1 - M_D^2 \left(\frac{\tan \beta}{M_{H^\pm}} \right)^2 \left(\frac{m_q}{m_c + m_q} \right) \right]^2$$

- Since m_d is ~ 0 , effect can be seen only in D_s

See Akeryod [hep-ph/0308260]



Experimental methods

- $D\bar{D}$ production at threshold: used by Mark III, and more recently by CLEO-c and BES-II.

- Unique event properties
 - Only $D\bar{D}$ not $D\bar{D}x$ produced

- Large cross sections:

$$\sigma(D^0\bar{D}^0) = 3.72 \pm 0.09 \text{ nb}$$

$$\sigma(D^+D^-) = 2.82 \pm 0.09 \text{ nb}$$

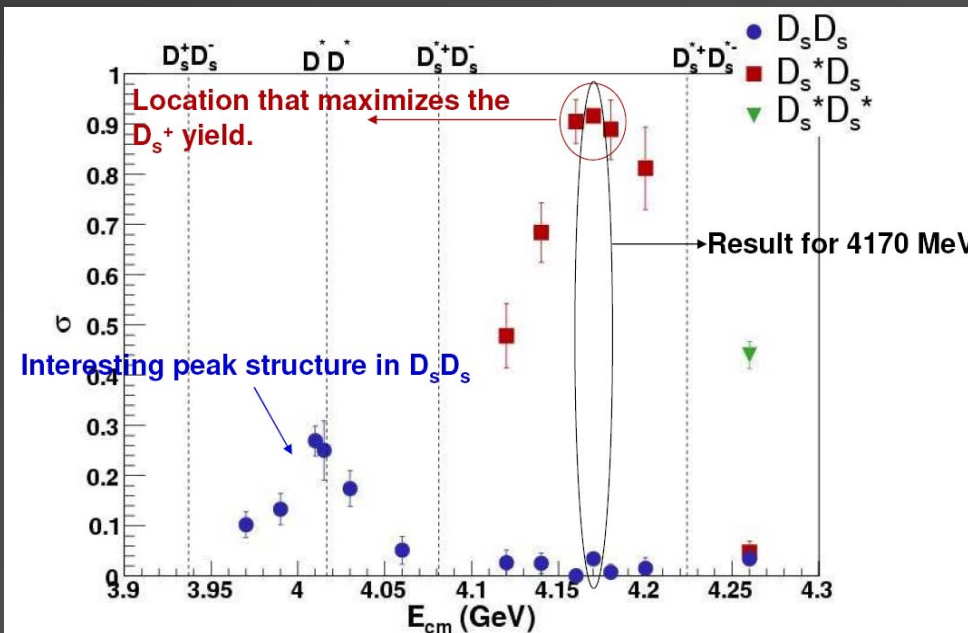
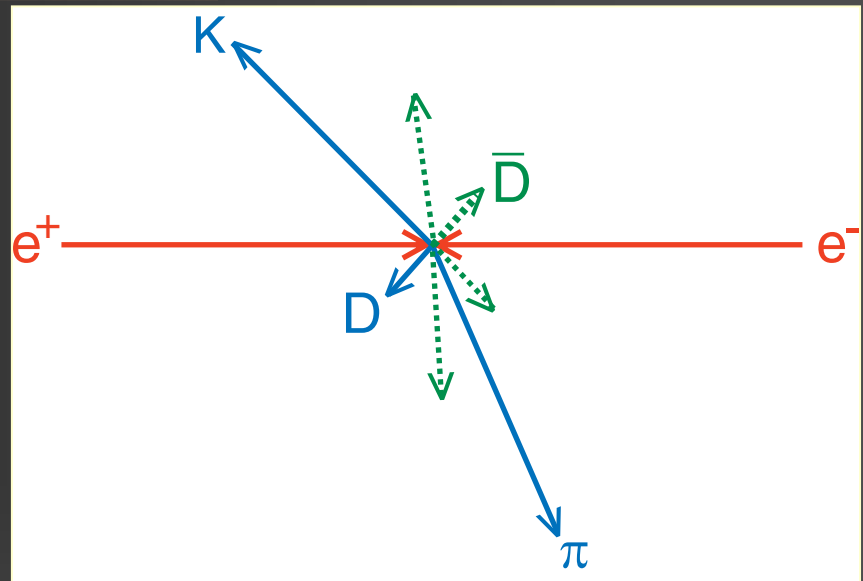
World Ave

$$\sigma(D_S D_S^*) = \sim 0.9 \text{ nb}$$

Continuum $\sim 12 \text{ nb}$

- Ease of B measurements using "double tags"

- $B_A = \# \text{ of } A / \# \text{ of } D\text{'s}$



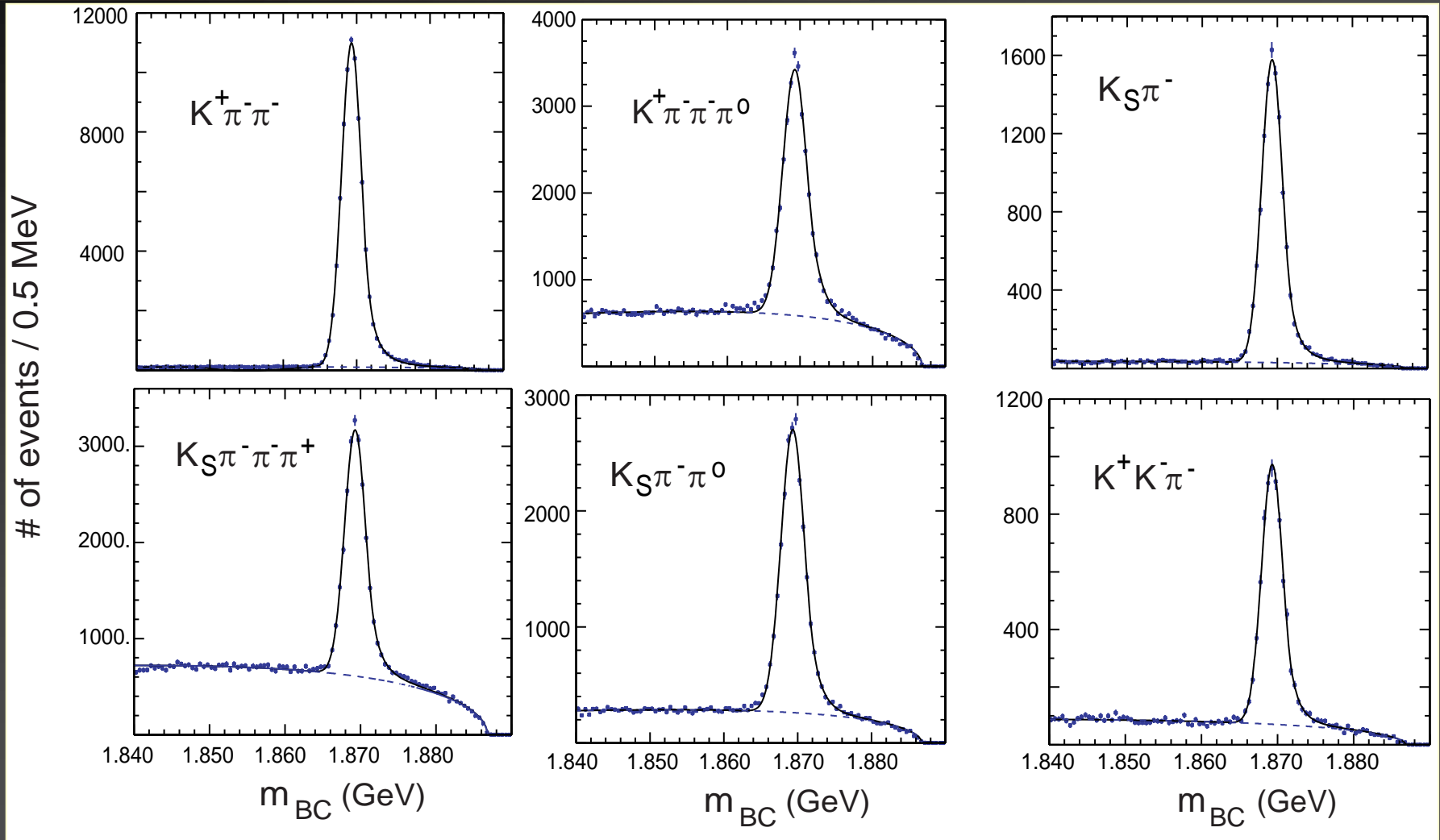
Technique for $D^+ \rightarrow \mu^+ \nu$

- Fully reconstruct a D^- , and count total # of tags
- Seek events with only one additional oppositely charged track and no additional photons > 250 MeV (to veto $D^+ \rightarrow \pi^+ \pi^0$)
- Charged track must deposit only minimum ionization in calorimeter
- Compute MM^2 . If close to zero then almost certainly we have a $\mu^+ \nu$ decay.

$$MM^2 = (E_{D^+} - E_{\ell^+})^2 - (\vec{p}_{D^+} - \vec{p}_{\ell^+})^2$$

We know $E_{D^+} = E_{\text{beam}}$, $\mathbf{p}_{D^+} = -\mathbf{p}_{D^-}$

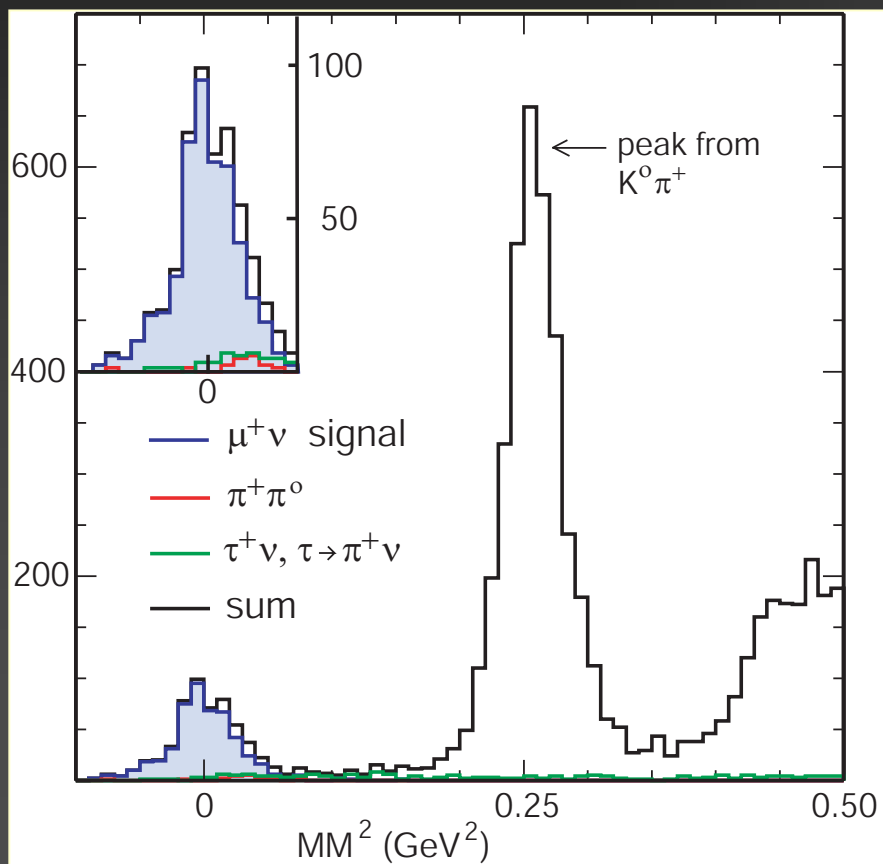
D^- Candidates (in 281 pb^{-1})



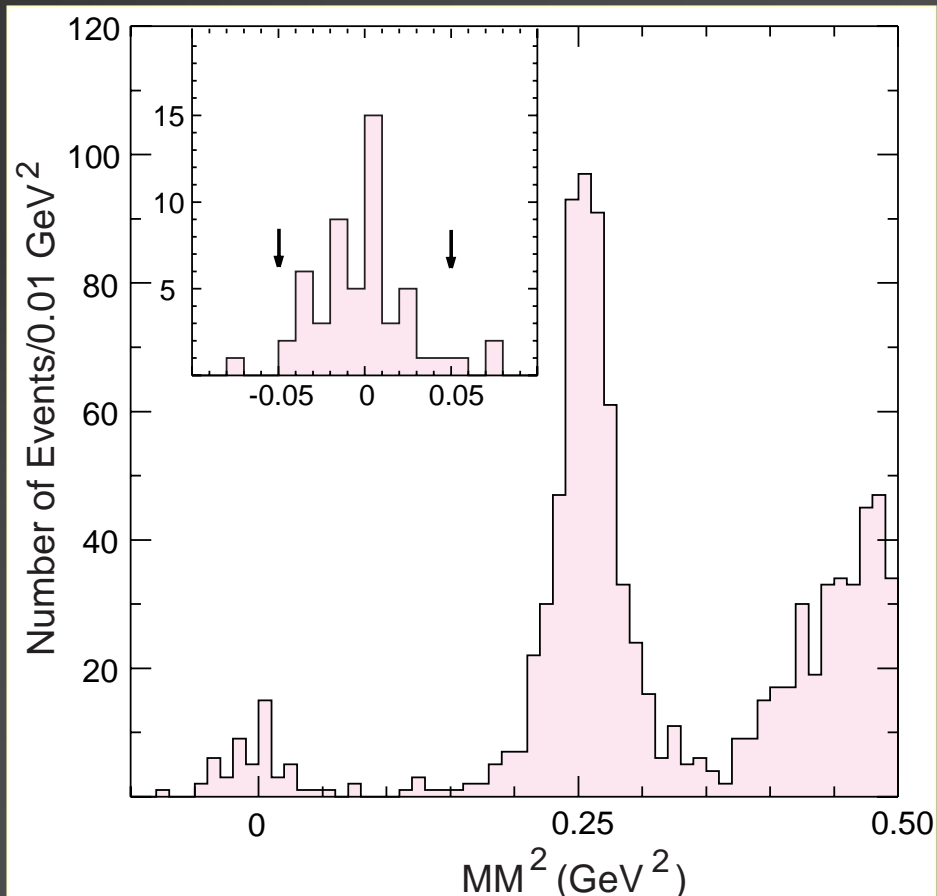
of tags = $158,354 \pm 496$, includes charge-conjugate modes

Measurement of f_{D^+}

MC Expectations from 1.7 fb^{-1} , 30 X of our data



Data: 50 events in the signal region in 281 pb^{-1}



Deriving a Value for f_{D^+}

Backgrounds		
Mode	$\mathcal{B}(\%)$	# Events
$\pi^+\pi^0$	0.13 ± 0.02	$1.40\pm 0.18\pm 0.22$
$K^0\pi^+$	2.77 ± 0.18	$0.33\pm 0.19\pm 0.02$
$\tau^+\nu$ ($\tau\rightarrow\pi^+\nu$)	$2.65^* \mathcal{B}(D^+\rightarrow\mu^+\nu)$	$1.08\pm 0.15\pm 0.16$
Other D^+ , D^0		$<0.4, <0.4 @ 90\% \text{ c.l.}$
Continuum		$<1.2 @ 90\% \text{ c.l.}$
Total		$2.81\pm 0.30^{+0.84}_{-0.27}$

- There are 158,354 tags. $\varepsilon = 67.7\%$
- $\mathcal{B}(D^+ \rightarrow \mu^+\nu) = (4.40\pm 0.66^{+0.09}_{-0.12}) \times 10^{-4}$
- $f_{D^+} = (222.6\pm 16.7^{+2.3}_{-3.4}) \text{ MeV} \quad |V_{cd}| = .2238$
- $\mathcal{B}(D^+ \rightarrow e^+\nu) < 2.4 \times 10^{-5} @ 90\% \text{ c.l.},$

Efficiencies: μ^+ detection (69.4%); extra shower (96.1%); correction for easier tag reconstruction in $\mu^+\nu$ events (1.5%)

rules out some non-Standard model theories

Systematic Errors

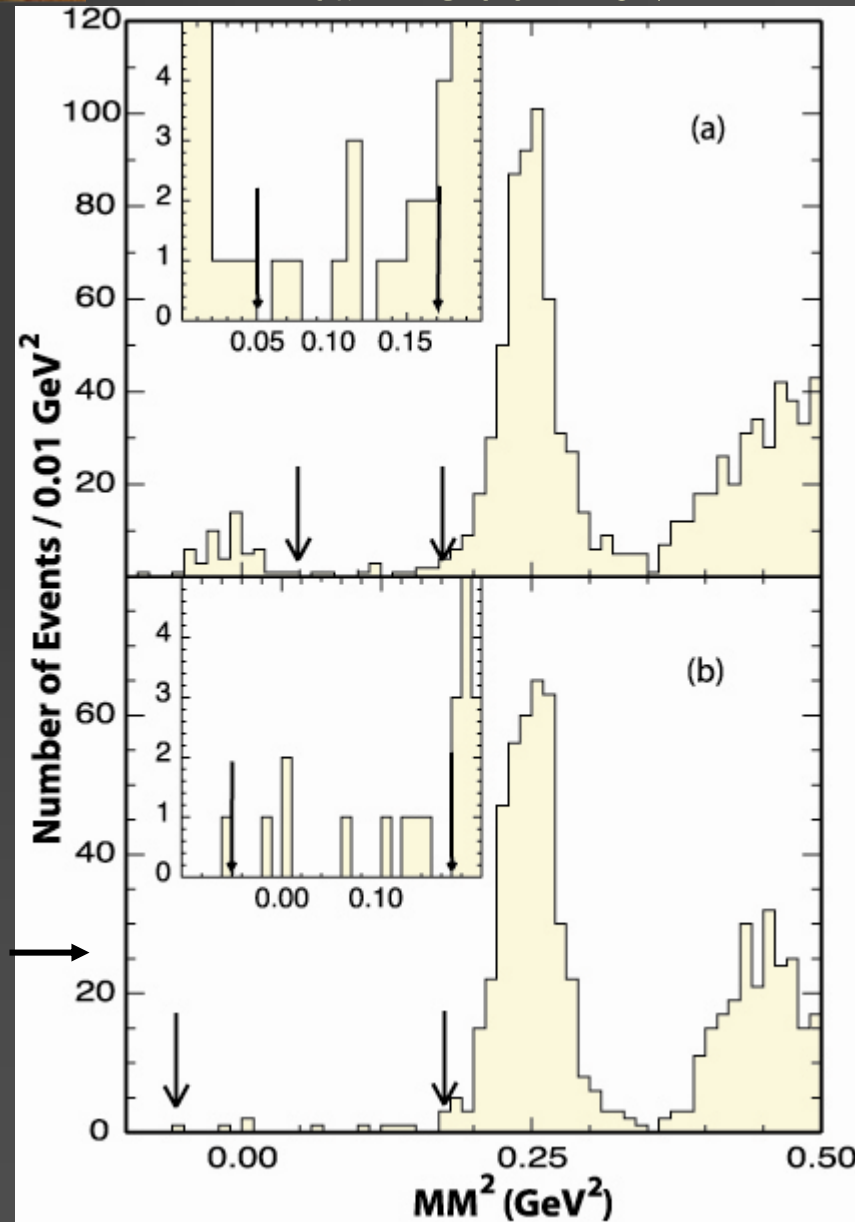
Source of Error	%
Finding the μ^+ track	0.7
Minimum ionization of μ^+ in EM cal	1.0
Particle identification of μ^+	1.0
MM ² width	1.0
Extra showers in event > 250 MeV	0.5
Background	0.6
Number of single tag D^+	0.6
Monte Carlo statistics	0.4
Total	2.1

Upper limit on $D^+ \rightarrow \tau^+ \nu$

$E_{cal} < 300 \text{ MeV}$

- By using intermediate MM^2 region
- $\mathcal{B}(D^+ \rightarrow \tau^+ \nu) < 2.1 \times 10^{-3}$
- $\frac{\Gamma(D^+ \rightarrow \tau^+ \nu)}{\Gamma(D^+ \rightarrow \mu^+ \nu)} < 1.8 \times (2.65)$
 - where 2.65 is SM expectation
 - both at 90% c.l

$E_{cal} > 300 \text{ MeV}$ →

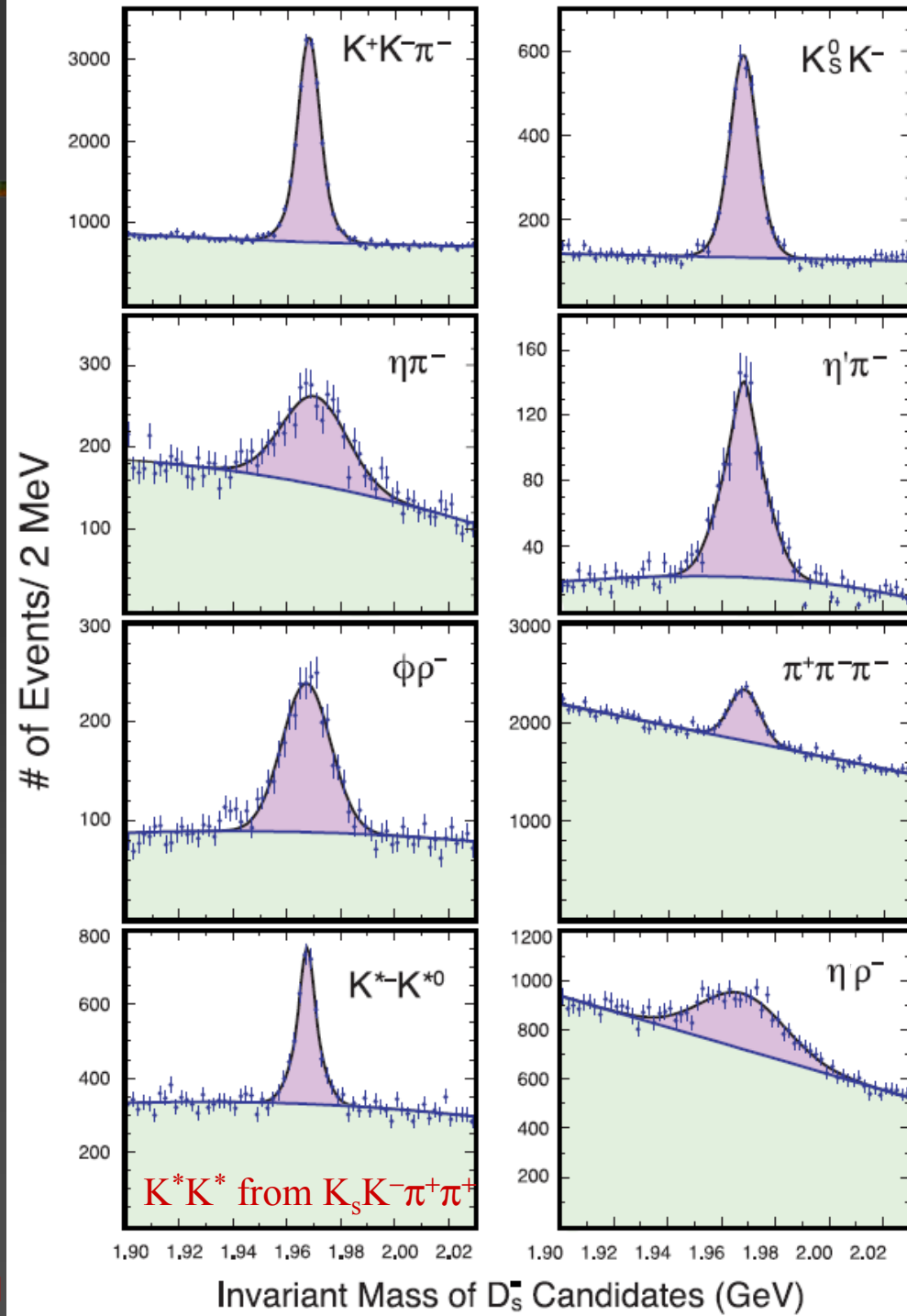


Measurements of f_{D_S}

- Two separate techniques. [Here expect in SM: $\Gamma(D_S \rightarrow \tau^+ \nu) / \Gamma(D_S \rightarrow \mu^+ \nu) = 9.72$]
 - (1) Measure $D_S^+ \rightarrow \mu^+ \nu$ along with $D_S \rightarrow \tau^+ \nu$, $\tau \rightarrow \pi^+ \nu$. This requires finding a D_S^- tag, a γ from either $D_S^{*-} \rightarrow \gamma D_S^-$ or $D_S^{*+} \rightarrow \gamma \mu^+ \nu$. Then find the muon or pion & apply kinematical constraints (mass & energy) to resolve this ambiguity & improve resolution (use 314 pb^{-1} , *results are published*)
 - (2) Find $D_S^+ \rightarrow \tau^+ \nu$, $\tau \rightarrow e^+ \nu \nu$ opposite a D_S^- tag (use 298 pb^{-1} , *results are final arXiv:0712.1175*)

Invariant masses

- $D_s \rightarrow \mu^+ \nu$ Study
- D_s studies done at $E_{\text{cm}} = 4170$ MeV
- To choose tag candidates:
 - Fit distributions & determine σ
 - Cut at $\pm 2.5 \sigma$
- Define sidebands to measure backgrounds $5-7.5 \sigma$
- Total # of Tags
= $31,302 \pm 472$ (stat)

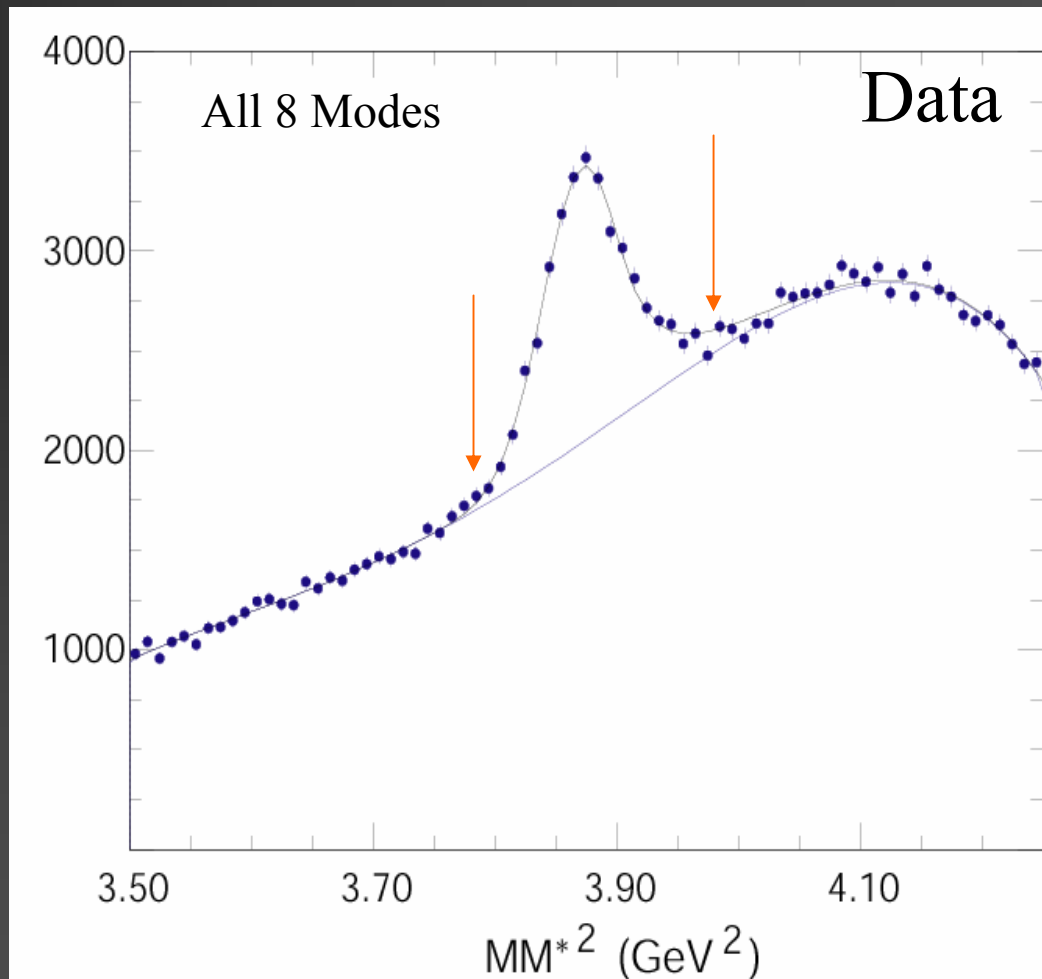


Tag Sample using γ

- First we define the tag sample by computing the MM^{*2} off of the γ & D_s tag

$$MM^{*2} = (E_{CM} - E_{D_s} - E_{\gamma})^2 - (-\vec{p}_{D_s} - \vec{p}_{\gamma})^2$$

- Total of $11880 \pm 399 \pm 504$ tags, after the selection on MM^{*2} .



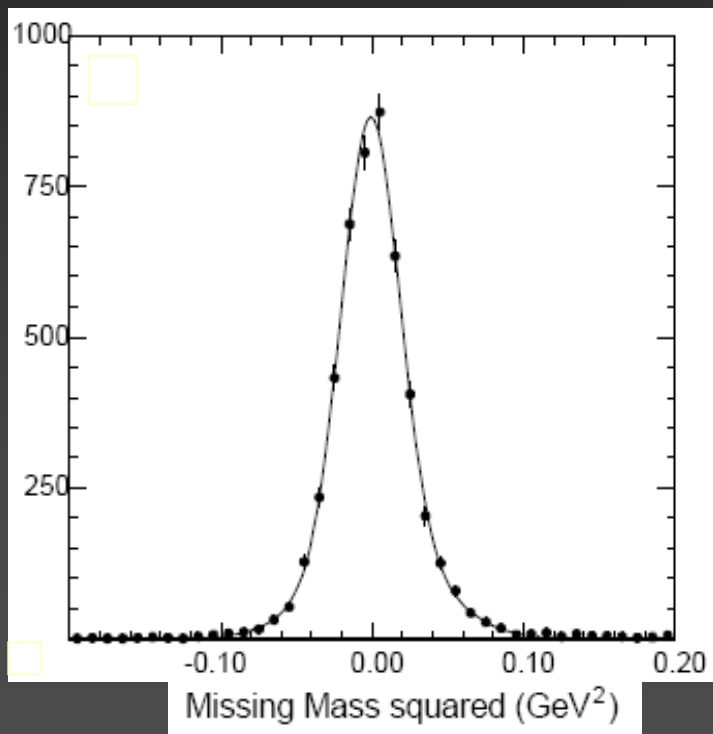
Define Three Classes

- Class (i), single track deposits < 300 MeV in calorimeter (consistent with μ) & no other $\gamma > 300$ MeV. (accepts 99% of muons and 60% of kaons & pions)
- Class (ii), single track deposits > 300 MeV in calorimeter & no other $\gamma > 300$ MeV (accepts 1% of muons and 40% of kaons & pions)
- Class (iii) single track consistent with electron & no other $\gamma > 300$ MeV

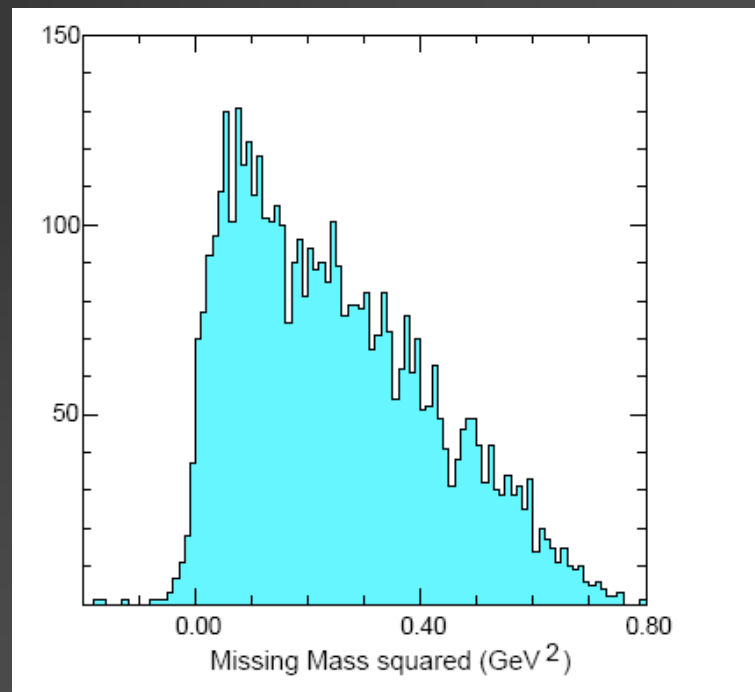
The MM^2

- To find the signal events, we compute

$$MM^2 = (E_{CM} - E_{D_S} - E_{\gamma} - E_{\mu})^2 - (-\vec{p}_{D_S} - \vec{p}_{\gamma} - \vec{p}_{\mu})^2$$



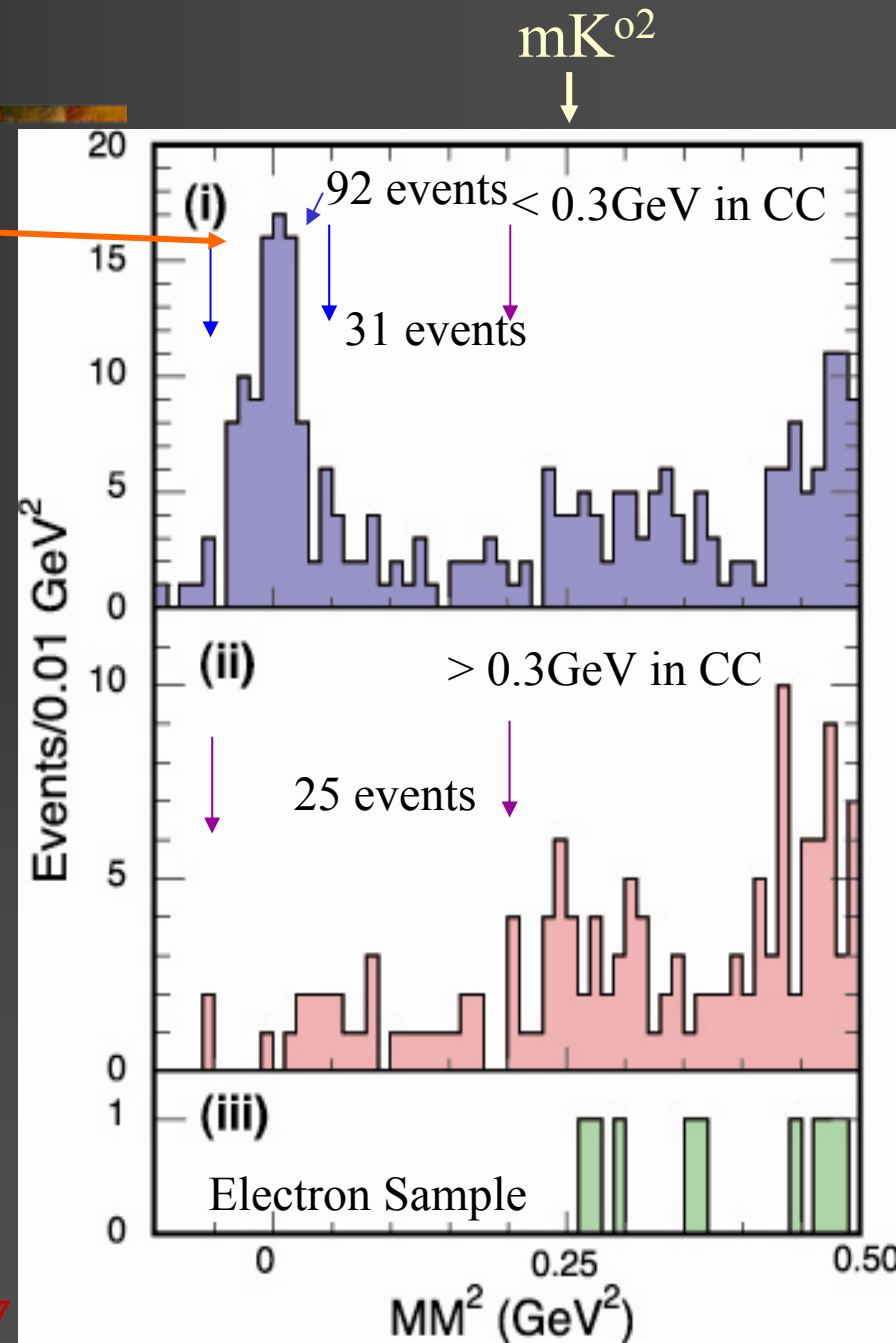
Monte Carlo Signal $\mu\nu$



Monte Carlo Signal $\tau\nu, \tau \rightarrow \pi\nu$

MM² In Data

- Clear $D_S^+ \rightarrow \mu^+ \nu$ signal for case (i)
- Most events < 0.2 GeV² are $D_S \rightarrow \tau^+ \nu$, $\tau \rightarrow \pi^+ \nu$ in cases (i) & (ii)
- No $D_S \rightarrow e^+ \nu$ seen, case (iii)



Branching Ratio & Decay Constant

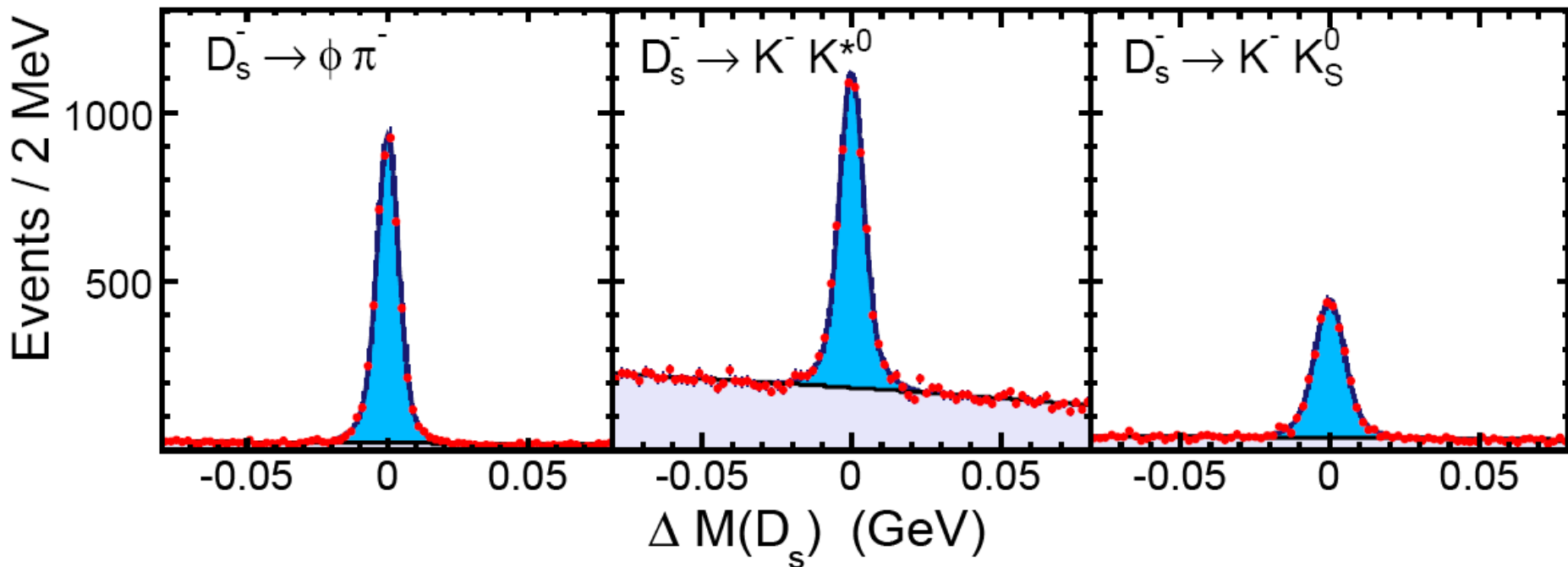
- $D_S^+ \rightarrow \mu^+ \nu$
 - 92 signal events, 3.5 background, use SM to calculate $\tau \nu$ yield near 0 MM^2 based on known $\tau \nu / \mu \nu$ ratio
 - $B(D_S^+ \rightarrow \mu^+ \nu) = (0.597 \pm 0.067 \pm 0.039)\%$
- $D_S^+ \rightarrow \tau^+ \nu, \tau^+ \rightarrow \pi^+ \nu$
 - Sum case (i) $0.2 > MM^2 > 0.05 \text{ GeV}^2$ & case (ii) $MM^2 < 0.2 \text{ GeV}^2$. Total of 56 signal and 8.6 bkgrnd
 - $B(D_S^+ \rightarrow \tau^+ \nu) = (8.0 \pm 1.3 \pm 0.4)\%$
- By summing both cases above, find
 $B^{\text{eff}}(D_S^+ \rightarrow \mu^+ \nu) = (0.638 \pm 0.059 \pm 0.033)\%$
- $f_{D_S} = 274 \pm 13 \pm 7 \text{ MeV}$, for $|V_{cs}| = 0.9738$
- $B(D_S^+ \rightarrow e^+ \nu) < 1.3 \times 10^{-4}$

$\mathcal{B}(D_s^+ \rightarrow \mu^+ \nu)$ Systematic errors

Error Source	Size (%)
Track finding	0.7
Photon veto	1
Minimum ionization <input type="checkbox"/>	1
Number of tags	5
Total	5.2

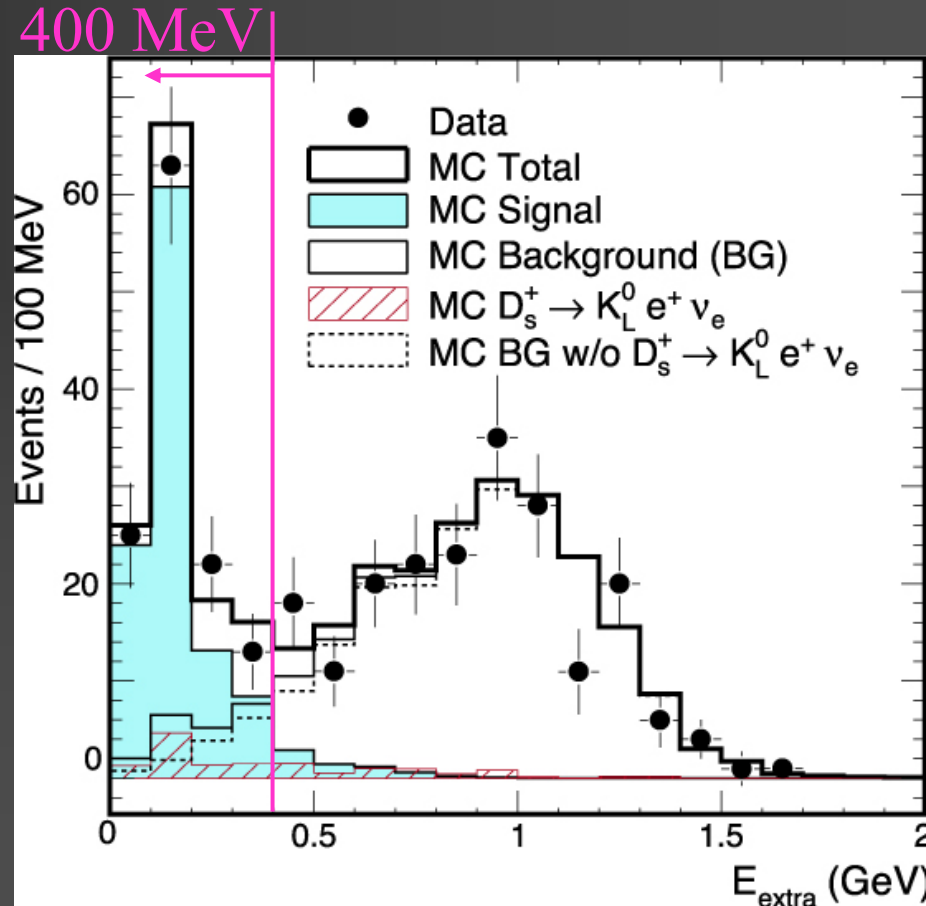
Measuring $D_s^+ \rightarrow \tau^+ \nu$, $\tau^+ \rightarrow e^+ \nu \nu$

- $B(D_s^+ \rightarrow \tau^+ \nu) \cdot B(\tau^+ \rightarrow e^+ \nu \nu) \sim 1.3\%$ is “large” compared with expected $B(D_s^+ \rightarrow X e^+ \nu) \sim 8\%$
- We will be searching for events opposite a tag with one electron and not much other energy



Measuring $D_S^+ \rightarrow \tau^+ \nu$, $\tau^+ \rightarrow e^+ \nu \nu$

- Technique is to find events with an e^+ opposite D_S^- tags & no other tracks, with Σ calorimeter energy < 400 MeV
- No need to find γ from D_S^*
- $B(D_S^+ \rightarrow \tau^+ \nu)$
 $= (6.17 \pm 0.71 \pm 0.36)\%$
- $f_{D_S} = 273 \pm 16 \pm 8$ MeV



f_{D_s} & f_{D_s} / f_{D^+}

- **Weighted Average:** $f_{D_s} = 274 \pm 10 \pm 5$ MeV, the systematic error is mostly uncorrelated between the measurements
- **Using** $f_{D^+} = (222.6 \pm 16.7^{+2.3}_{-3.4})$ MeV[†]
M. Artuso et al., Phys. Rev. Lett. 95 (2005) 251801
- **$f_{D_s} / f_{D^+} = 1.23 \pm 0.10 \pm 0.03$**
- **$\Gamma(D_s^+ \rightarrow \tau^+ \nu) / \Gamma(D_s^+ \rightarrow \mu^+ \nu) = 11.0 \pm 1.4 \pm 0.6$, SM = 9.72, consistent with lepton universality**

Radiative Corrections

- Not just final state radiation which is already corrected for.
- Includes $D \rightarrow D^* \rightarrow \gamma D \rightarrow \gamma \mu^+ \nu$. Based on calculations of Burdman et al.
- $\Gamma(D_{(s)}^+ \rightarrow \gamma \mu^+ \nu) / \Gamma(D_{(s)}^+ \rightarrow \mu^+ \nu) \sim 1/40 - 1/100$
- Using narrow MM² region makes this much smaller
- Other authors in general agreement, see Hwang Eur. Phys. J. C46, 379 (2006), except Korchemsky, Pirjol & Yan PRD 61, 114510 (2000)
- Wang, Chang & Feng [hep-ph/0102251] find a -8% correction for $\Gamma(D_S \rightarrow \tau^+ \nu)$, negligible for $\Gamma(D_S \rightarrow \mu^+ \nu)$.
- Somebody please help!

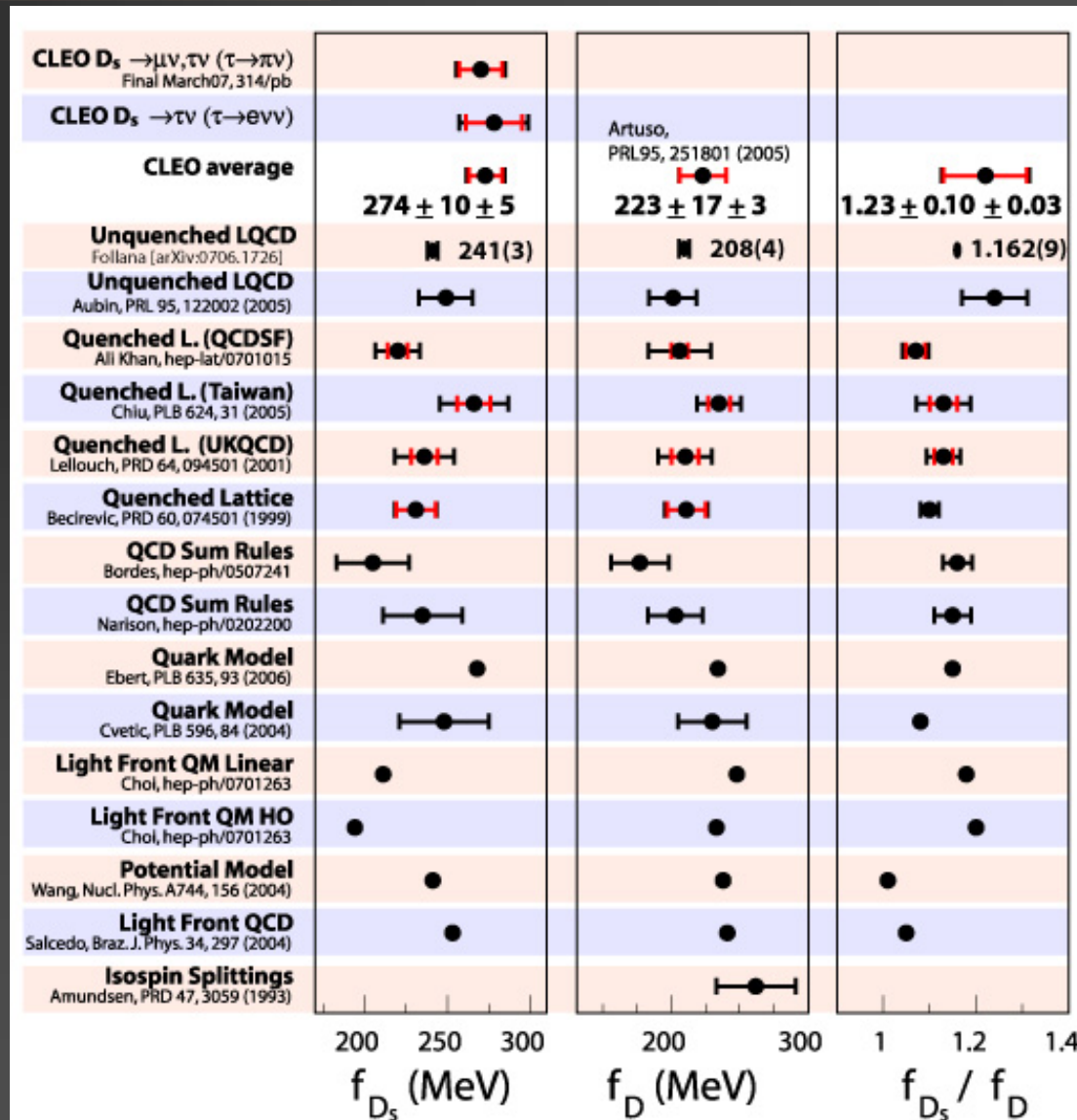
Comparison with Other Experiments

Exp.	Mode	$\mathcal{B}_{\phi\pi}$ (%)	$f_{D_s^+}$ (MeV)
CLEO-c	$\mu^+\nu$ [7]		$264 \pm 15 \pm 7$
CLEO-c	$\tau^+\nu$ [7]		$310 \pm 25 \pm 8$
CLEO-c	$\tau^+\nu$ [8]		$273 \pm 16 \pm 8$
CLEO-c	combined		$274 \pm 10 \pm 5$
Belle [9]	$\mu^+\nu$	preliminary Manchester EPS	$275 \pm 16 \pm 12$
Average			274 ± 10
CLEO [10]	$\mu^+\nu$	3.6 ± 0.9	$273 \pm 19 \pm 27 \pm 33$
BEATRICE [11]	$\mu^+\nu$	3.6 ± 0.9	$312 \pm 43 \pm 12 \pm 39$
ALEPH [12]	$\mu^+\nu$	3.6 ± 0.9	$282 \pm 19 \pm 40$
ALEPH [12]	$\tau^+\nu$		
L3 [13]	$\tau^+\nu$		$299 \pm 57 \pm 32 \pm 37$
OPAL [14]	$\tau^+\nu$		$283 \pm 44 \pm 41$
BaBar [15]	$\mu^+\nu$	4.71 ± 0.46	$283 \pm 17 \pm 7 \pm 14$

- CLEO-c is most precise result to date for both f_{D_s} & f_{D^+}

Comparisons with Theory

- We are $\sim 3\sigma$ above Follana et al. Either:
 - Calculation is wrong
 - There is new physics that interferes constructively with SM
 - Note: No value of M_H is allowed in 2HDM at 99.5% *c.l.*
- Comparing measured f_{D_S}/f_{D^+} with Follana prediction we find $m_H > 2.2 \text{ GeV } \tan\beta$
- Using Follana ratio find $|V_{cd}/V_{cs}| = 0.217 \pm 0.019$ (exp) ± 0.002 (theory)



Projections

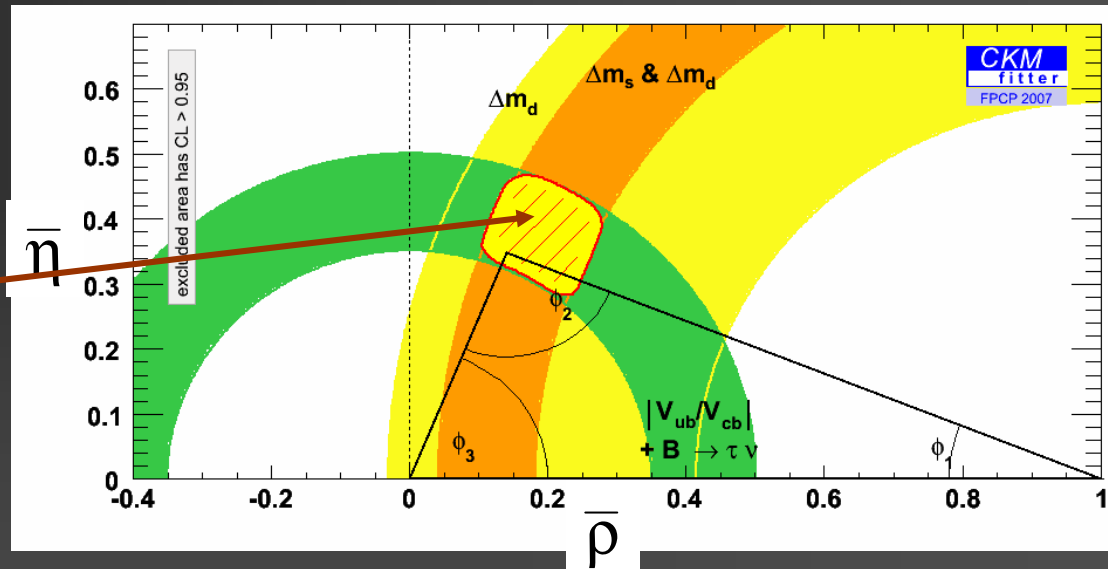
- We will almost triple the D^+ sample, including some improvements in technique, error in f_{D^+} should decrease to $\sim 3.7\%$ (8 MeV)
- We will likely double the D_S sample, may improve technique, expect error in f_{D_S} to decrease to $\sim 2.6\%$ (7 MeV)



The End

Goals in Leptonic Decays

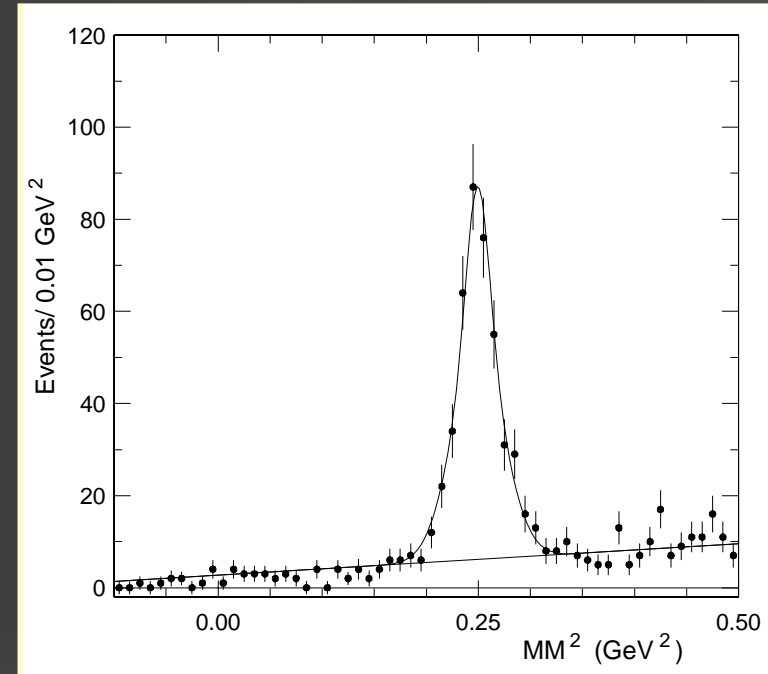
- Test theoretical calculations in strongly coupled theories in non-perturbative regime
- f_B & f_{B_s}/f_B needed to improve constraints from Δm_d & $\Delta m_s/\Delta m_d$. Hard to measure directly (i.e. $B \rightarrow \tau^+ \nu$ gives $V_{ub} f_B$), but we can determine f_D & f_{D_s} using $D \rightarrow \ell^+ \nu$ and use them to test theoretical models (i.e. Lattice QCD)



Constraints from V_{ub} , Δm_d , Δm_s & $B \rightarrow \tau^+ \nu$

Check: $\mathcal{B}(D_s^+ \rightarrow K^+ K^0)$

- Do almost the same analysis but consider MM^2 off of an identified K^+
- Allow extra charged tracks and showers so not to veto K^0 decays or interactions in EM
- Signal verifies expected MM^2 resolution
- Find $(2.90 \pm 0.19 \pm 0.18)\%$, compared with result from double tags $(3.00 \pm 0.19 \pm 0.10)\%$



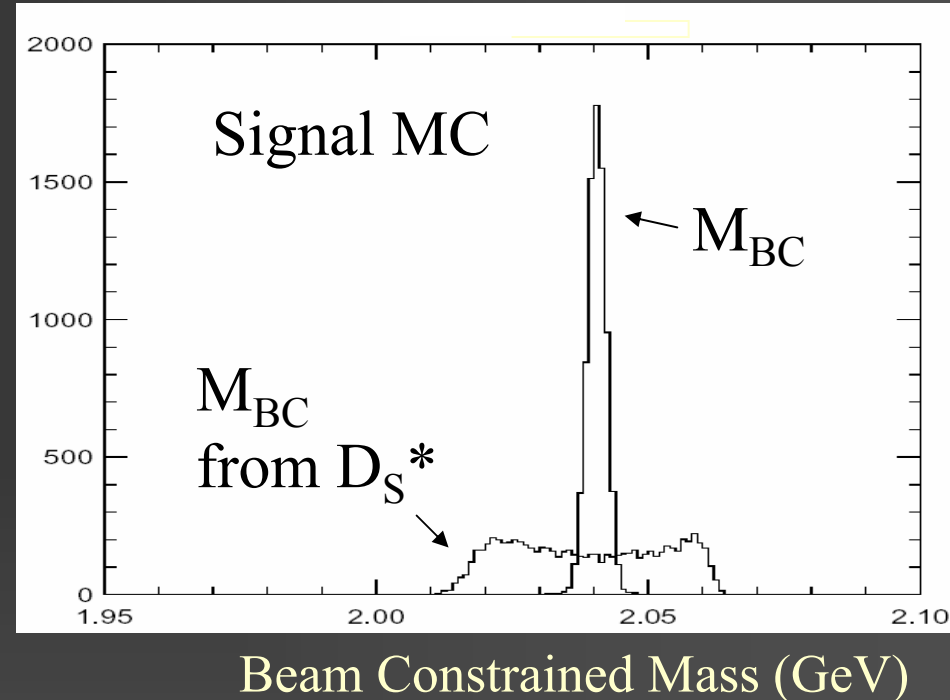
CLEO D_S^+ Results at 4170 MeV

- Since $e^+e^- \rightarrow D_S^* D_S$, the D_S from the D_S^* will be smeared in beam-constrained mass.

- $$M_{BC}^2 = E_{\text{beam}}^2 - \sum_i \vec{p}_i^2$$

- \therefore cut on M_{BC} & plot invariant mass (equivalent to a p cut)

- We use 314 pb^{-1} of data



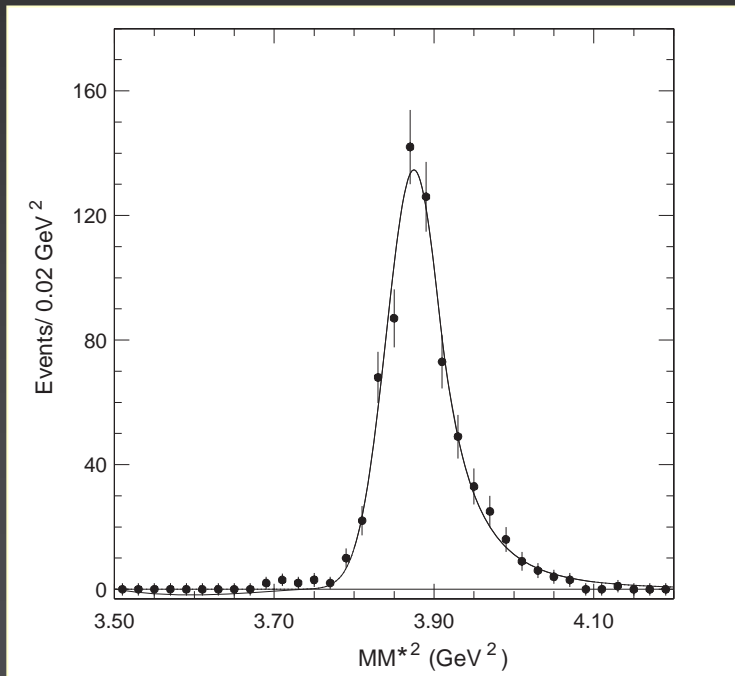
#Tags: $D_s + \gamma$

- Compute MM^{*2}

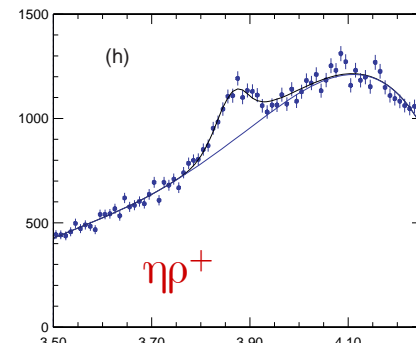
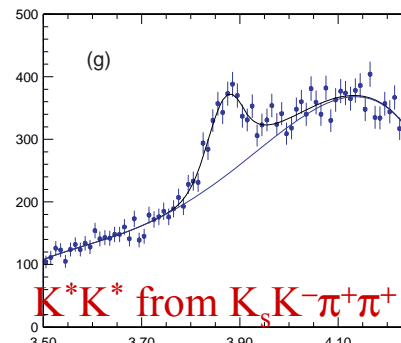
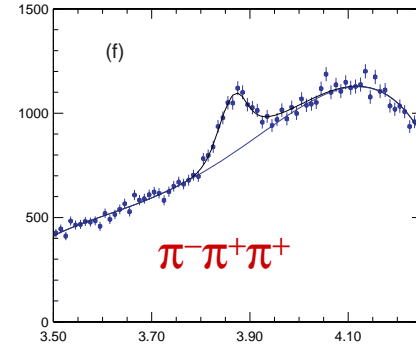
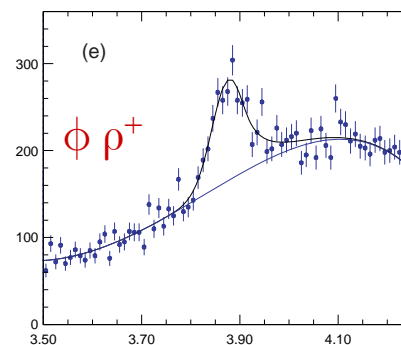
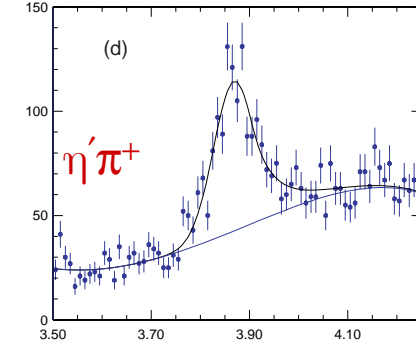
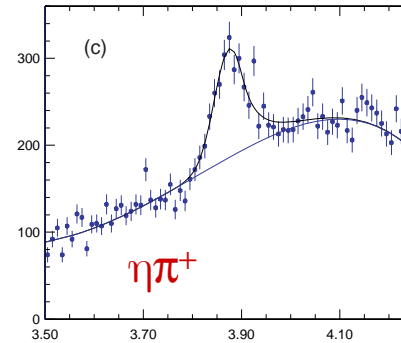
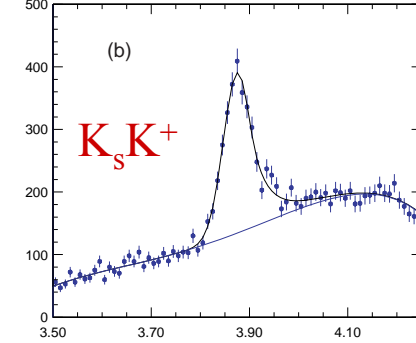
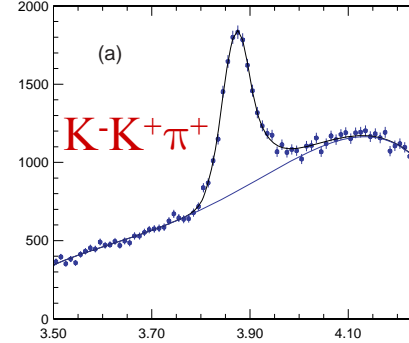
$$MM^{*2} = (E_{CM} - E_{D_s} - E_{\gamma})^2 - (-\vec{p}_{D_s} - \vec{p}_{\gamma})^2$$

in each individual mode

- Use $D_s^* D_s$ sample to measure shape of tail



of Events / 0.01 GeV²



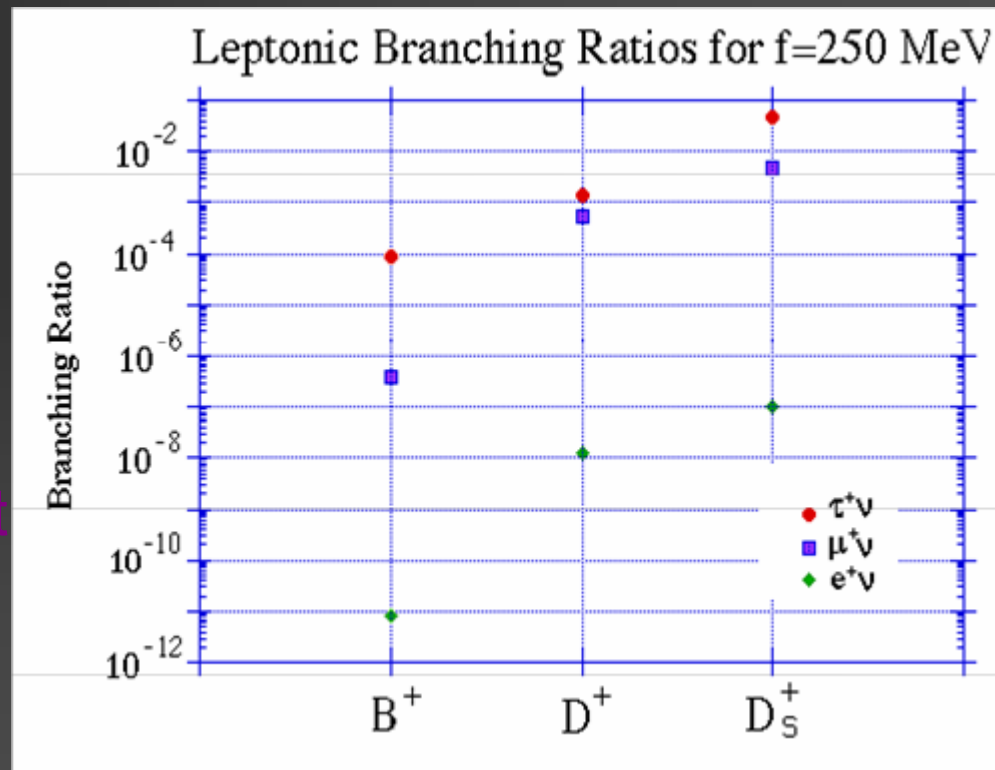
MM^{*2} (GeV²)

Measurement of $D_S^+ \rightarrow \mu^+ \nu$

- In this analysis we use $D_S^* D_S$ events where we detect the γ from the $D_S^* \rightarrow \gamma D_S$ decay
- We see all the particles from $e^+ e^- \rightarrow D_S^* D_S, \gamma, D_S$ (tag) + μ^+ except for the ν
- We use a kinematic fit to (a) improve the resolution & (b) remove ambiguities
 - Constraints include: total p & E, tag D_S mass, $\Delta m = M(\gamma D_S) - M(D_S)$ [or $\Delta m = M(\gamma \mu \nu) - M(\mu \nu)$] = 143.6 MeV, E of D_S (or D_S^*) fixed
 - Lowest χ^2 solution in each event is kept
 - No χ^2 cut is applied

Expected \mathcal{B} for $P^+ \rightarrow \ell^+ \nu$ decays

- We know:
 - $f_\pi = 131.73 \pm 0.15$ MeV
 - $f_K = 160.6 \pm 1.3$ MeV
- The D_s has the largest \mathcal{B} , for $\mu^+ \nu$ rate is $\sim 0.5\%$
- f_{D_s} Measured by several groups, best CLEO II, but still poorly known
- $e^+ \nu$ rate is ~ 4 orders of magnitude smaller than $\mu^+ \nu$, in the Standard Model



Combining Semileptonics & Leptonics

- Semileptonic decay rate into Pseudoscalar:

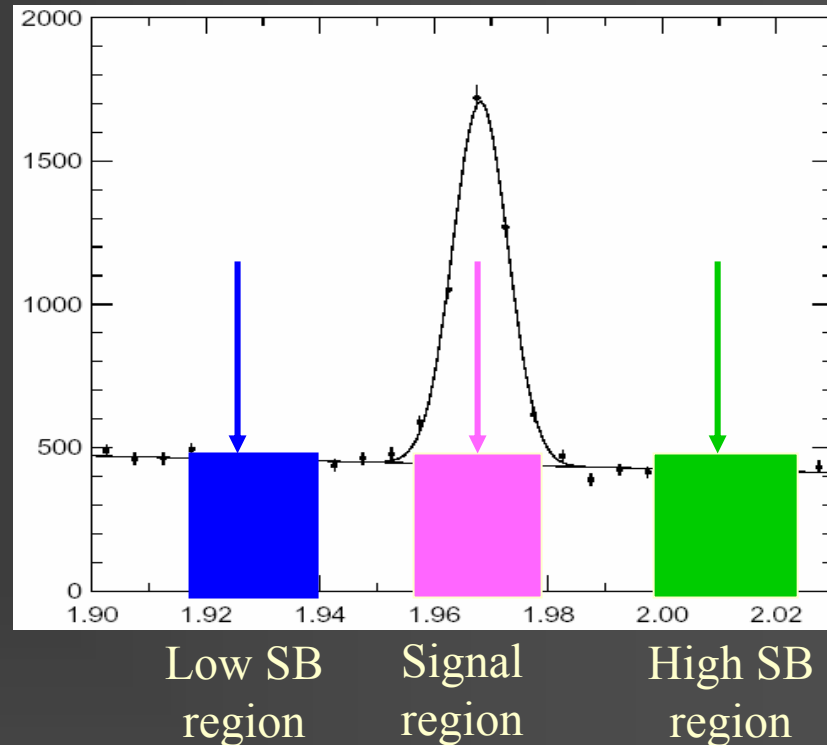
$$\frac{d\Gamma(D \rightarrow P e \nu)}{dq^2} = \frac{|V_{cq}|^2 P_P^3}{24\pi^3} |f_+(q^2)|^2$$

- Note that the ratio below depends only on QCD:

$$\frac{1}{\Gamma(D^+ \rightarrow \ell \nu)} \frac{d\Gamma(D^+ \rightarrow \pi e \nu)}{dq^2} \propto \frac{P_\pi^3 |f_+(q^2)|^2}{f_{D^+}^2}$$

Background Samples

- Two sources of background
- A) Backgrounds under invariant mass peaks – Use sidebands to estimate
- In $\mu^+\nu$ signal region 3.5 background (92 total)
- bkgnd $MM^2 < 0.20 \text{ GeV}^2 = 9.0 \pm 2.3$
- B) Backgrounds from real D_S decays, e.g. $\pi^+\pi^0\pi^0$, or $D_S \rightarrow \tau^+\nu$, $\tau \rightarrow \pi^+\pi^0\nu \dots < 0.2 \text{ GeV}^2$, none in $\mu\nu$ signal region
- $B(D_S \rightarrow \pi^+\pi^0) < 1.1 \times 10^{-3}$ & γ energy cut yields < 0.2 evts



Backgrounds from real D_S^+

TABLE III: Backgrounds in the $D_S^+ \rightarrow \tau^+\nu$, $\tau^+ \rightarrow \pi^+\bar{\nu}$ sample for correctly reconstructed tags, case (i) for $0.05 < MM^2 < 0.20 \text{ GeV}^2$ and case (ii) for $-0.05 < MM^2 < 0.20 \text{ GeV}^2$.

Source	$B(\%)$	# of events case (i)	# of events case(ii)	Sum
$D_S^+ \rightarrow X\mu^+\nu$	8.2	$0_{-0}^{+1.8}$	0	$0_{-0}^{+1.8}$
$D_S^+ \rightarrow \pi^+\pi^0\pi^0$	1.0	0.03 ± 0.04	0.08 ± 0.03	0.11 ± 0.04
$D_S^+ \rightarrow \tau^+\nu$	6.4			
$\tau^+ \rightarrow \pi^+\pi^0\bar{\nu}$	1.5	0.55 ± 0.22	0.64 ± 0.24	1.20 ± 0.33
$\tau^+ \rightarrow \mu^+\bar{\nu}\nu$	1.0	0.37 ± 0.15	0	0.37 ± 0.15
Sum		$1.0_{-0}^{+1.8}$	0.7 ± 0.2	$1.7_{-0.4}^{+1.8}$

Sum of $D_S^+ \rightarrow \mu^+ \nu + \tau^+ \nu$, $\tau \rightarrow \pi^+ \nu$

- As we will see, there is very little background present in any sub-sample for $MM^2 < 0.2 \text{ GeV}^2$

