

# Future Kaon Experiments

R. Tschirhart  
Fermilab

April 27<sup>th</sup> , 2010

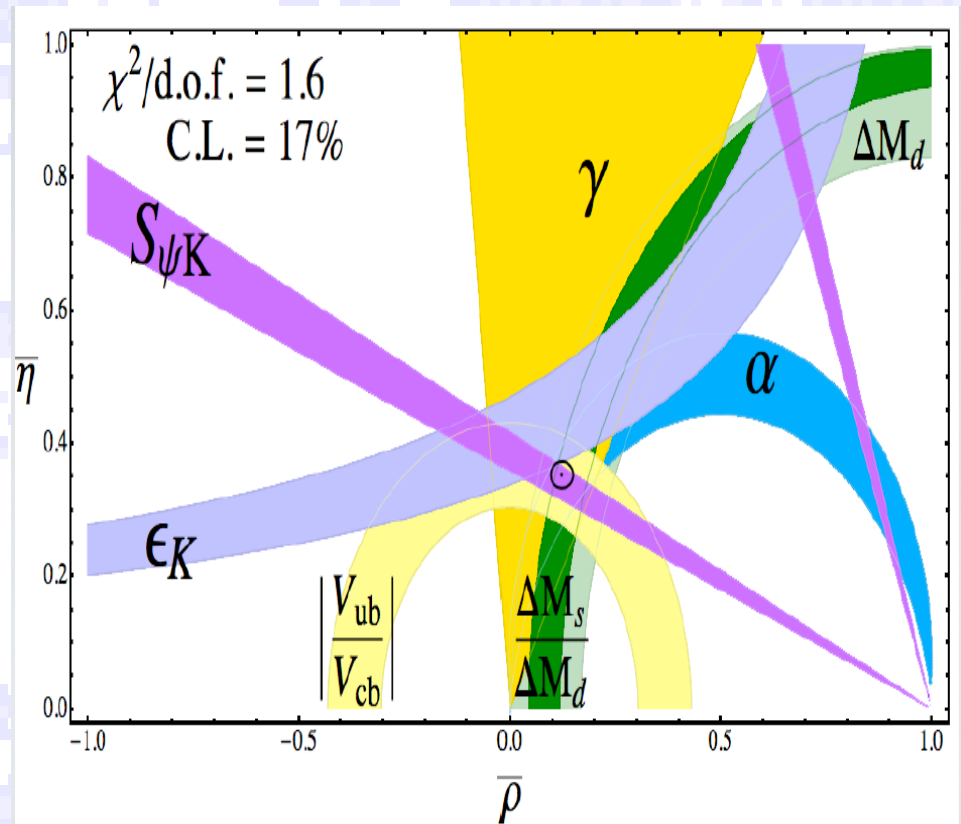
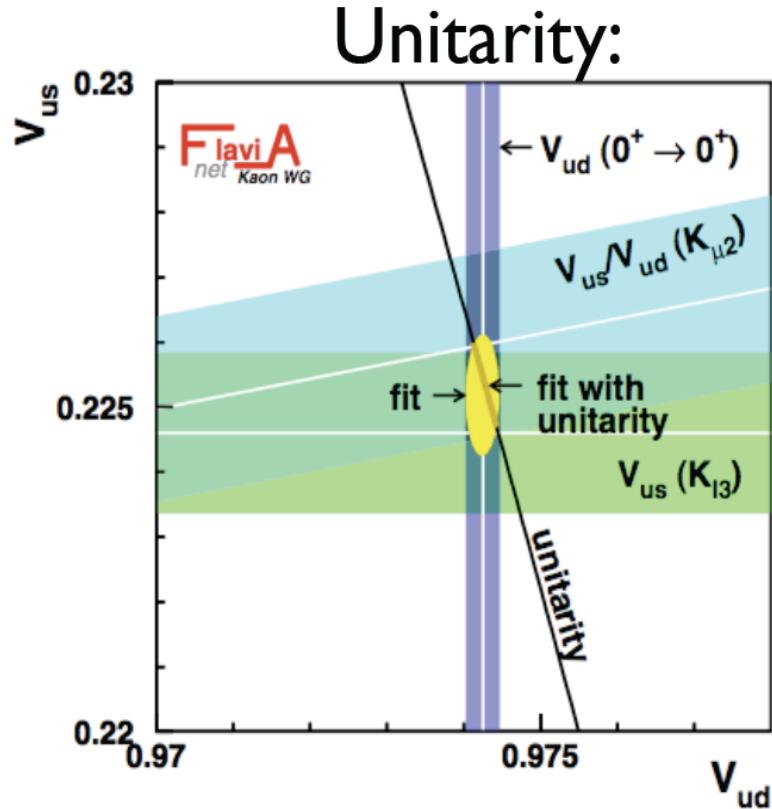
# LQCD Targets in Kaon Physics: Now and Then...

- LQCD post-dictions to interpret existing precision measurements.
- LQCD post-dictions to interpret existing measurements that could have large contributions from physics beyond the Standard Model.
- LQCD predictions of future measurements that are highly sensitive to new physics beyond the Standard Model.

# Interpreting Existing Precision Measurements

Enrico Lunghi, LME-2010, Fermilab

Laiho, Lunghi, Van de Water, arXiv:0910.2928



Precision unitarity tests require  $f_K$  and form-factors

$\epsilon_K$  interpretation requires  $B_K$ , but now limited by  $|V_{cb}|$  !

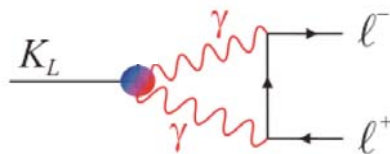
# Hiding in Plain Sight...

- $\text{Re}(\varepsilon'_K/\varepsilon_K)$ :

$$\frac{\Gamma(K^0 \rightarrow \pi^+\pi^-) - \Gamma(\bar{K}^0 \rightarrow \pi^+\pi^-)}{\Gamma(K^0 \rightarrow \pi^+\pi^-) + \Gamma(\bar{K}^0 \rightarrow \pi^+\pi^-)} = (5.04 \pm 0.22) \times 10^{-6} *$$

*Large component of this asymmetry might arise from New Physics.*

- $K_L \rightarrow \mu\mu$ :



$$\text{B}(K_L^0 \rightarrow \mu^+\mu^-) = (6.84 \pm 0.11) \times 10^{-9} *$$

*~10% of this amplitude is from 2<sup>nd</sup> order EW loops...where new physics can contribute.*

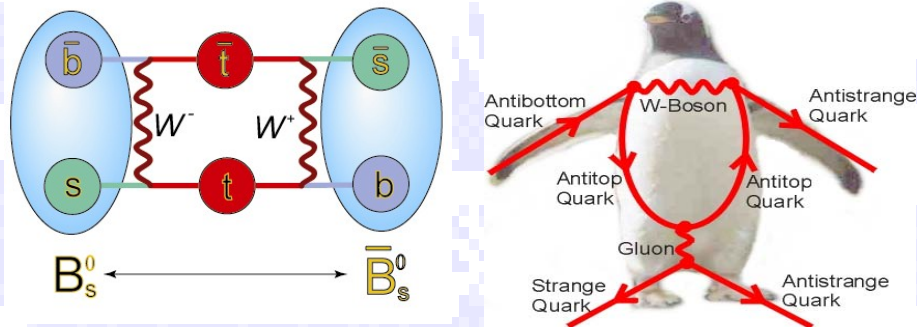


\* PDG

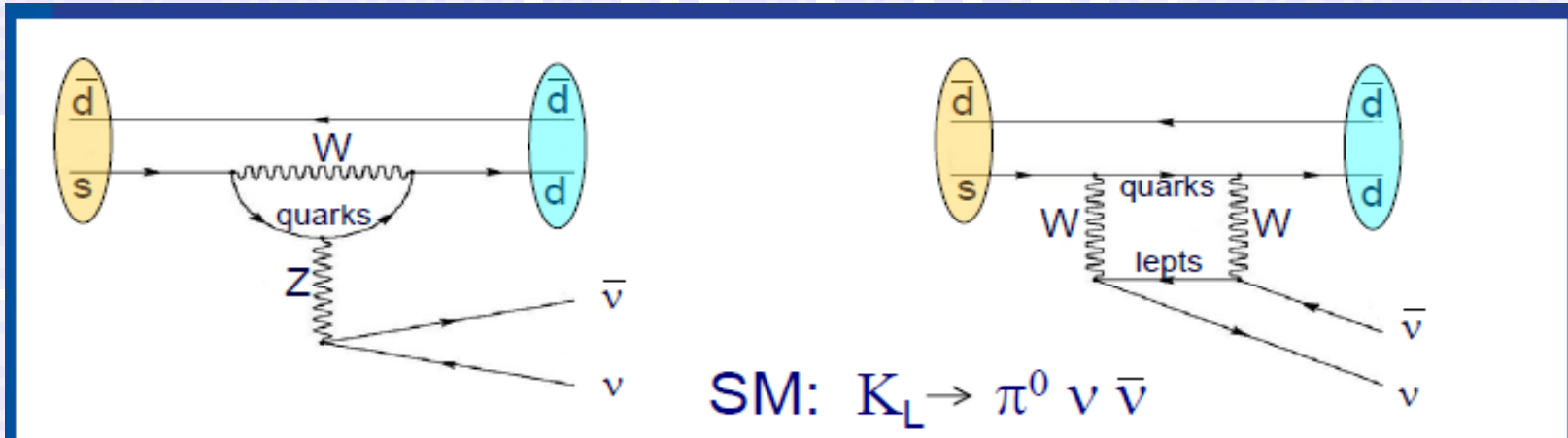
Urban-Art camouflage

# Future Rare Kaon Decay Experiments Deeply Attack The Flavor Problem

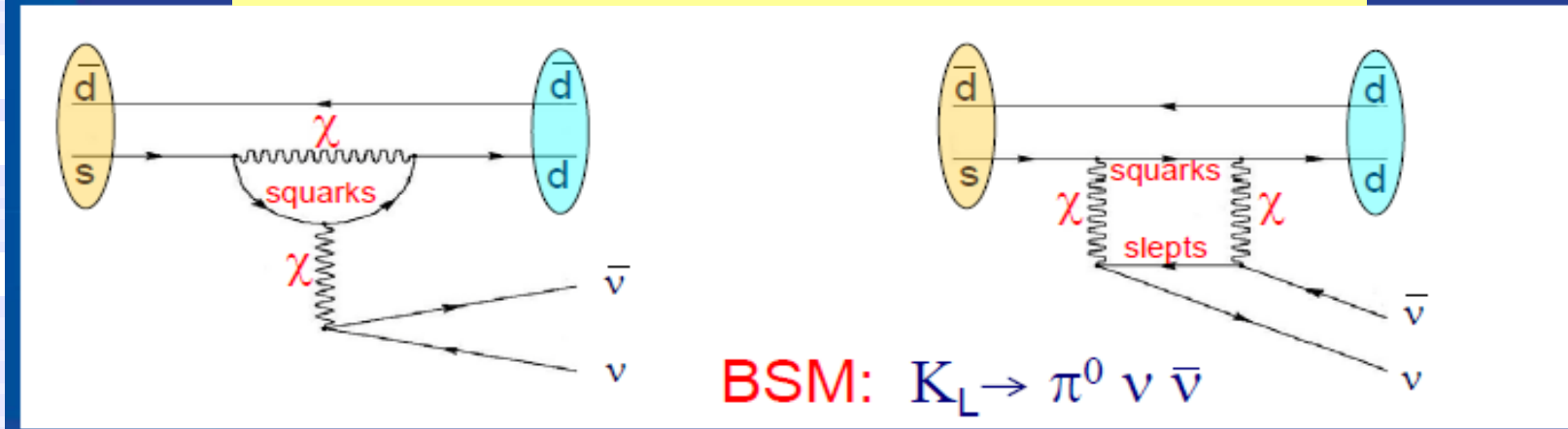
Why don't we see the *Terascale Physics we expect* affecting the flavor physics we study today??



# The Window of Ultra-rare Kaon Decays



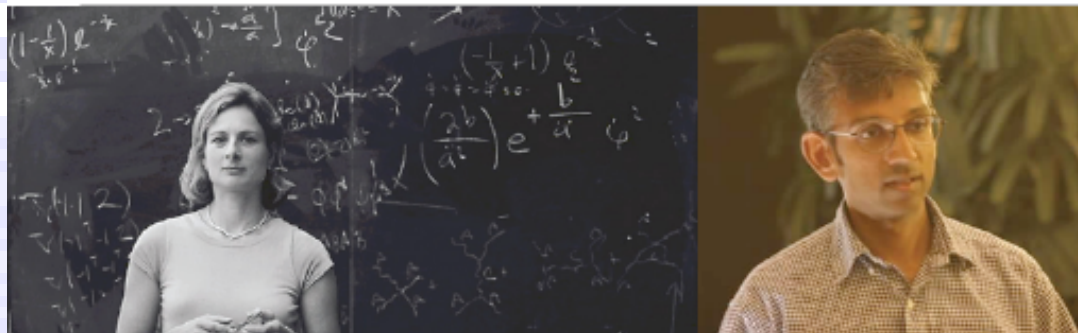
*Standard Model rate of 3 parts per 100 billion!*



*BSM particles within loops can increase the rate by  $\times 10$  with respect to SM.*

# Rates sensitive to many BSMs...e.g., Warped Extra Dimensions as a Theory of Flavor??

## The Randall-Sundrum (RS) idea



**Island Universes in Warped Space-Time**

According to string theory, our universe might consist of a three-dimensional "brane," embedded in higher dimensions. In the model developed by Lisa Randall and Raman Sundrum, gravity is much weaker on our brane than on another brane, separated from us by a fifth dimension. (Time is the unseen fourth dimension.)

**GRAVITY BRANE**  
(where gravity is concentrated)

**Fifth dimension**  
Space is warped by energy throughout five-dimensional space-time. As a result, gravity is much weaker on our brane.

**Gravitons,**  
which transmit gravity, are closed strings, which are not confined to either brane.

**Warped space-time**  
Because space-time is warped, things are exponentially bigger and lighter closer to our brane.

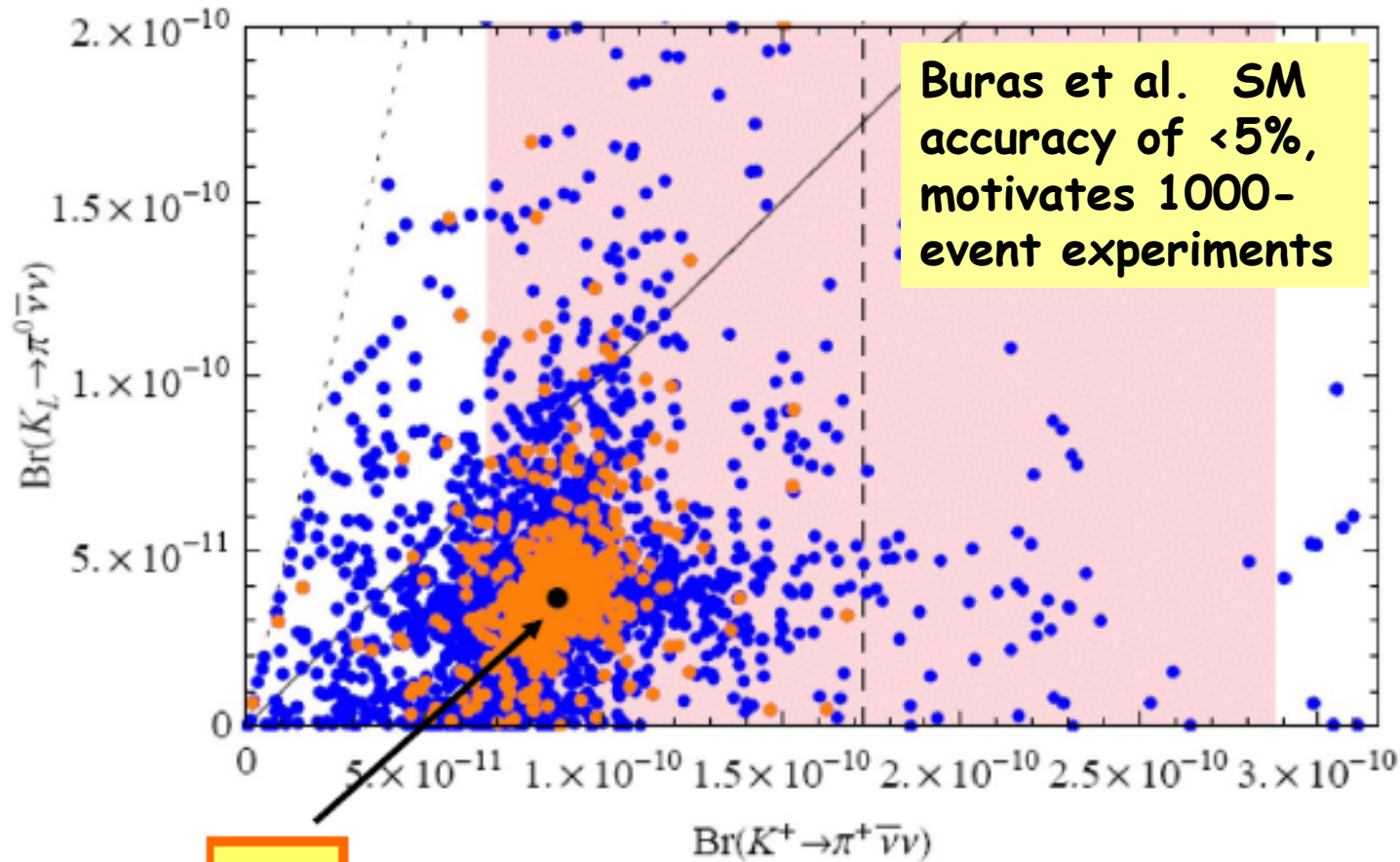
**BRANE**  
(our universe)

The ends of **open strings**, whose oscillations are particles and forces other than gravity, are stuck to our brane.

(Wikipedia)

$$\mathbf{K_L \rightarrow \pi^0 \nu\bar{\nu} \text{ vs. } K^+ \rightarrow \pi^+ \nu\bar{\nu}} \quad (\text{RS})$$

(Up to Factor 3 and 2 Enhancements)



*Effect of Warped Extra Dimension Models on Branching Fractions*



# Sensitivity of Kaon Physics Today

- CERN NA62:  $100 \times 10^{-12}$  measurement sensitivity of  $K^+ \rightarrow e^+ \nu$
- Fermilab KTeV:  $20 \times 10^{-12}$  measurement sensitivity of  $K_L \rightarrow \mu \mu e e$
- Fermilab KTeV:  $20 \times 10^{-12}$  search sensitivity for  $K_L \rightarrow \pi \mu e, \pi \pi \mu e$
- BNL E949:  $20 \times 10^{-12}$  measurement sensitivity of  $K^+ \rightarrow \pi^+ \nu \bar{\nu}$
- BNL E871:  $1 \times 10^{-12}$  measurement sensitivity of  $K_L \rightarrow e^+ e^-$
- BNL E871:  $1 \times 10^{-12}$  search sensitivity for  $K_L \rightarrow \mu e$

***Probing new physics above a 10 TeV scale with 20-50 kW of protons.***

***Next goal: 1000-event  $\pi \nu \nu$  experiments...  $10^{-14}$  sensitivity.***

# Kaon Experiment Goals This Decade

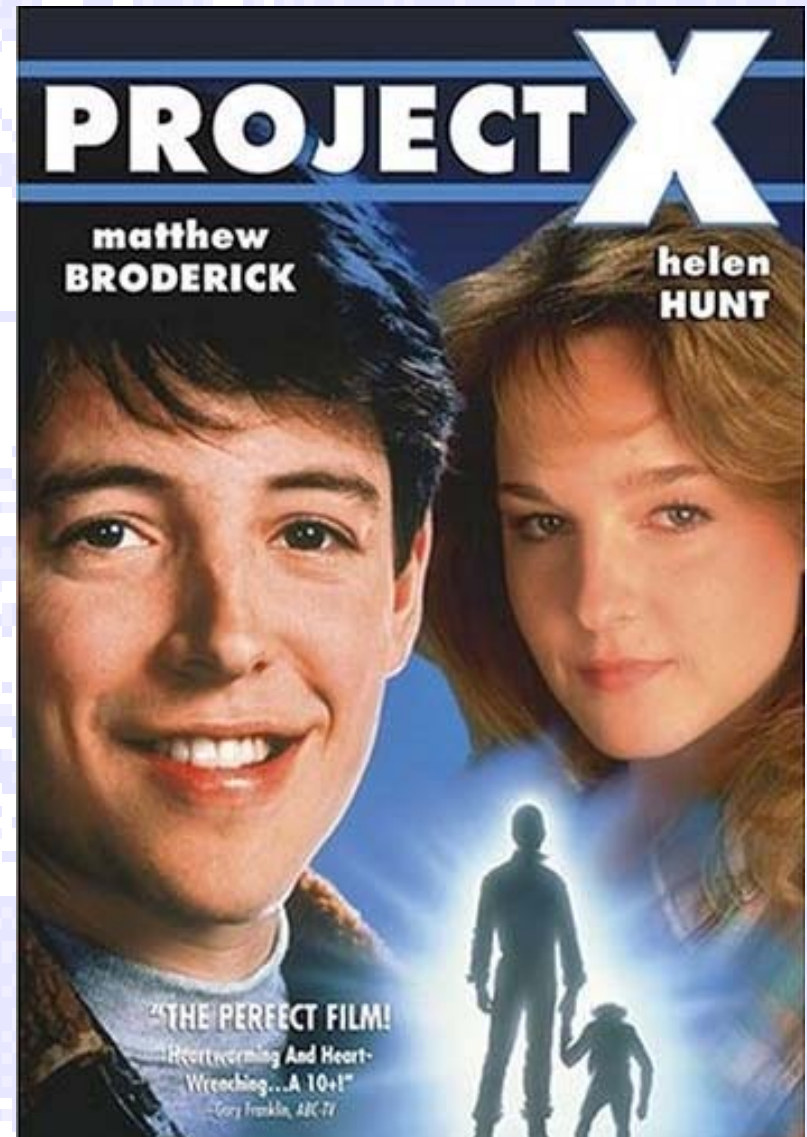
- $K^+ \rightarrow \pi^+ \nu \bar{\nu}$ : >100 events, first measurement with BSM sensitivity  
*CERN NA62 experiment, data taking in 2013.*  
*1000-event proposal to Fermilab (P996).*
- $K^+ \rightarrow \pi^0 \mu^+ \nu$ : Search for T-violating muon polarization.
- $K^+ \rightarrow (\pi, \mu)^+ \nu_\chi$ : Search for anomalous heavy neutrinos.  
*JPARC E06 "TREK" experiment, advanced approval.*
- $K_L \rightarrow \pi^0 \nu \bar{\nu}$ : Sensitivity approaching the Standard Model prediction.  
*JPARC E14 "KOTO" experiment, advanced approval.*
- $K_S \rightarrow \gamma\gamma$ : Precision measurement, test of ChPT...LQCD?  
*KLOE-2, advanced approval.*

# Kaon Physics Measurements Enabled by Project-X, Data Taking in the Next Decade

- $K^+ \rightarrow \pi^+ \nu \bar{\nu}$ : >1000 events, Precision rate and form factor.... $V_{cb}$  !
- $K^+ \rightarrow \pi^0 \mu^+ \nu$ : Measurement of T-violating muon polarization.
- $K^+ \rightarrow (\pi, \mu)^+ \nu_\chi$ : Search for anomalous heavy neutrinos.
- $K_L \rightarrow \pi^0 \nu \bar{\nu}$ : 1000 events, enabled by high flux & precision TOF.
- $K_2 \rightarrow \pi^0 e^+ e^-$ : <10% measurement of CP violating amplitude.
- $K_2 \rightarrow \pi^0 \mu^+ \mu^-$ : <10% measurement of CP violating amplitude.
- $K^0 \rightarrow X$ : Precision study of a pure  $K^0$  interferometer:  
Reaching out to the Plank scale ( $\Delta m_K / m_K \sim 1/m_p$ )
- $K^0, K^+ \rightarrow LFV$ : Next generation Lepton Flavor Violation experiments  
...and more

4th Project-X Physics Workshop: November 9-10<sup>th</sup> 2009

# Project-X, What it's not...



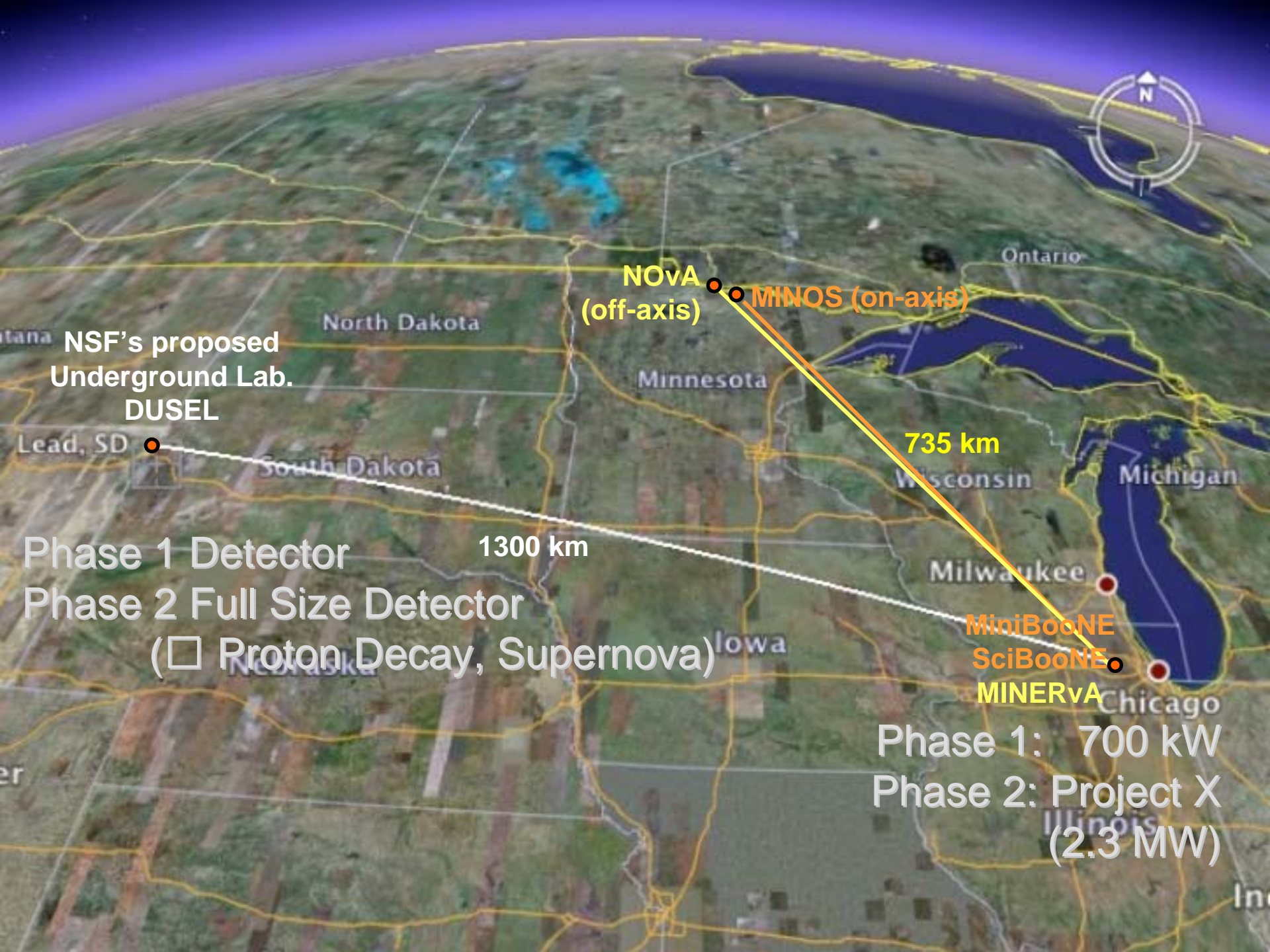
# The Project-X Research Program

- *Long baseline neutrino oscillation experiments:*

Driven by a high-power proton source with proton energies between 50 and 120 GeV that would produce intense neutrino beams directed toward massive detectors at a distant deep underground laboratory.

- *Kaon, muon, nuclei & neutron precision experiments driven by high intensity proton beams running simultaneously with the neutrino program:*

These could include world leading experiments searching for muon-to-electron conversion, nuclear and neutron electron dipole moments (edms), and world-leading precision measurements of ultra-rare kaon decays.



NOvA  
(off-axis)

MINOS (on-axis)

735 km

1300 km

NSF's proposed  
Underground Lab.  
DUSEL

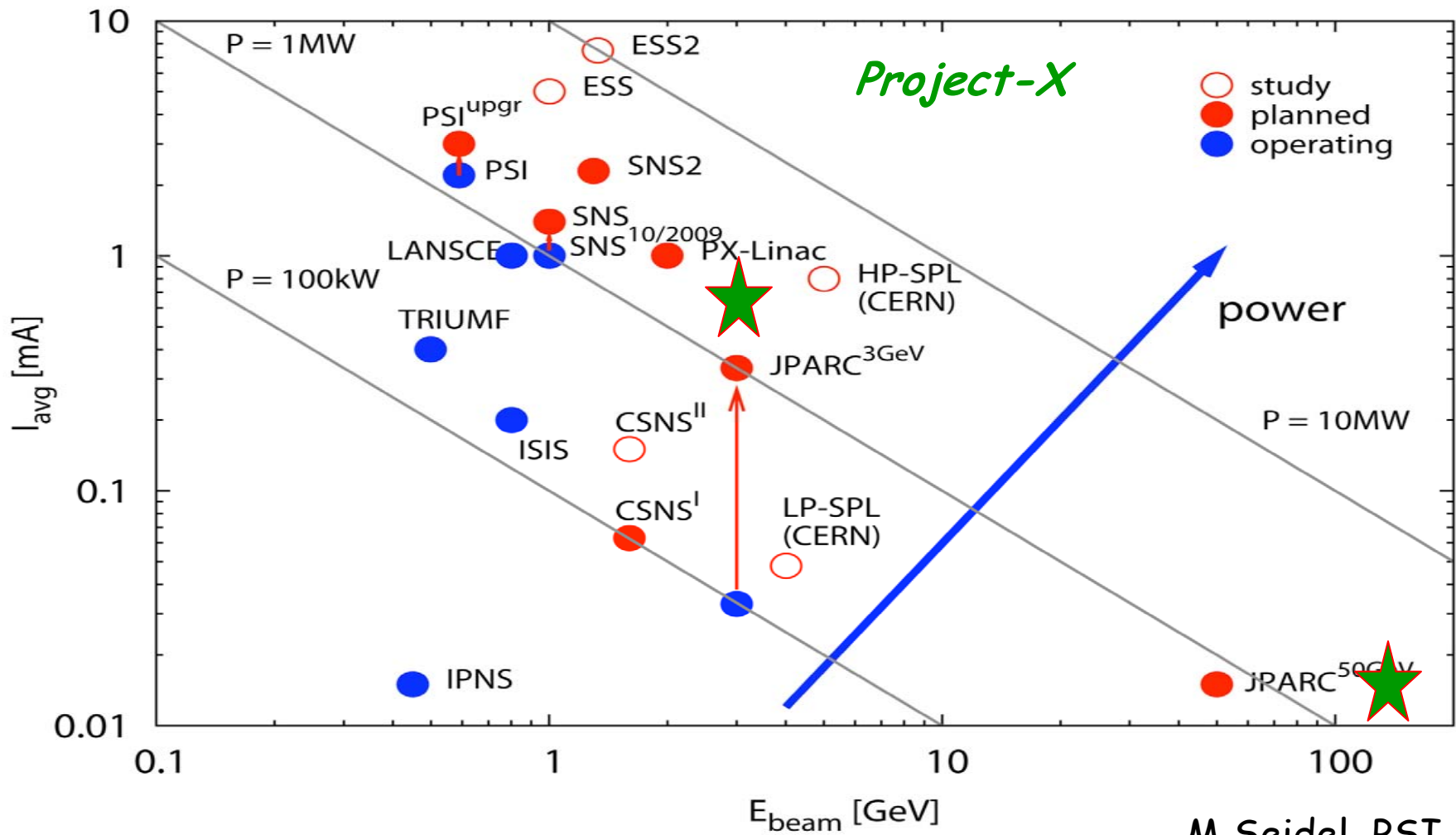
Lead, SD

Phase 1 Detector  
Phase 2 Full Size Detector  
(□ Proton Decay, Supernova)

MiniBooNE  
SciBooNE  
MINERvA

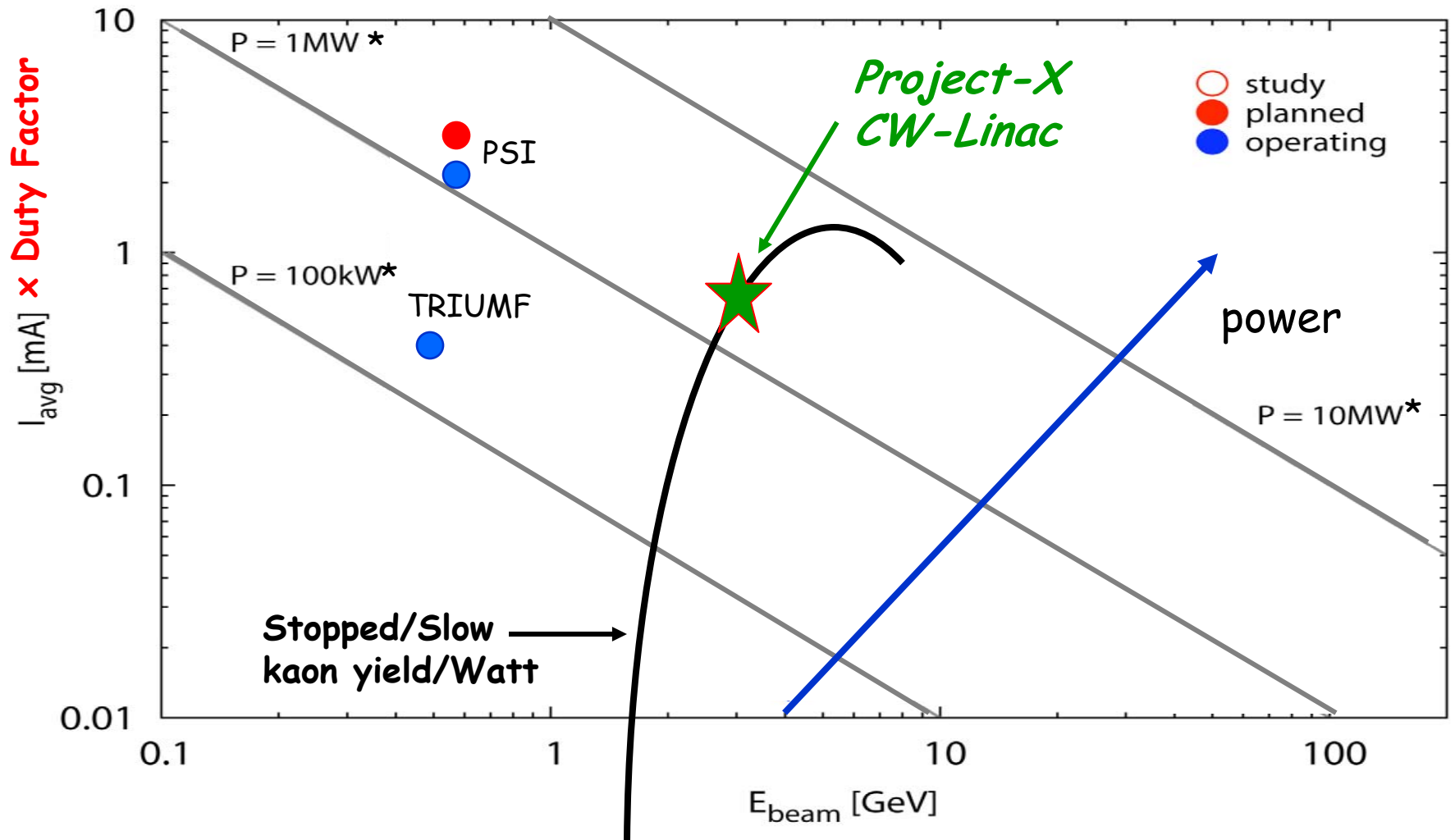
Phase 1: 700 kW  
Phase 2: Project X  
(2.3 MW)

# This Science has attracted Competition: The Proton Source Landscape This Decade...



M Seidel, PSI

# The High **Duty Factor** Proton Source Landscape This Decade...

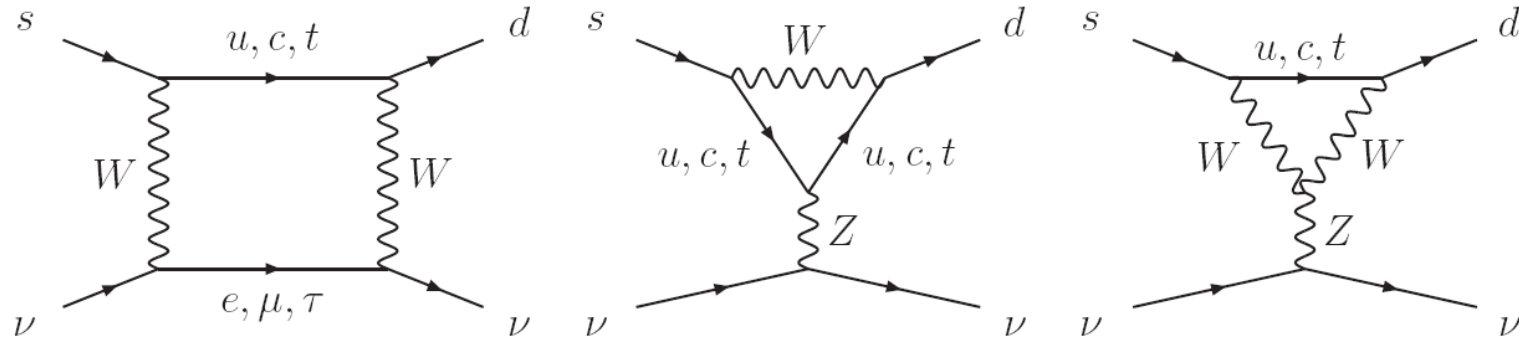


\* Beam power  $\times$  **Duty Factor**

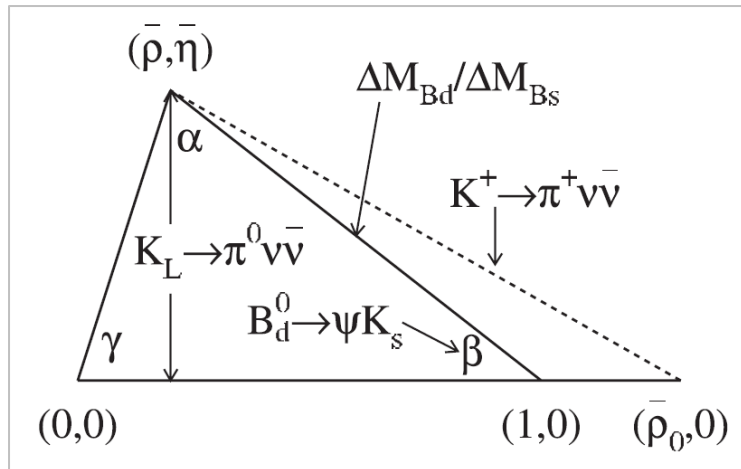


# $K^+ \rightarrow \pi^+ \nu \bar{\nu}$ in the Standard Model

The  $K \rightarrow \pi \nu \bar{\nu}$  decays are the most precisely calculated FCNC decays.



- A single effective operator  $(\bar{s}_L \gamma^\mu d_L)(\bar{\nu}_L \gamma_\mu \nu_L)$
- Dominated by top quark (charm significant, but controlled)
- Hadronic matrix element shared with Ke3
- uncertainty from CKM elements (*will improve*)
- **Remains clean in New Physics models** (*unlike many other observables*)



$$\text{BSM}(K^+ \rightarrow \pi^+ \nu \bar{\nu}) = (8.5 \pm 0.7) \times 10^{-11}$$

# Theoretical Progress

## SM Precision

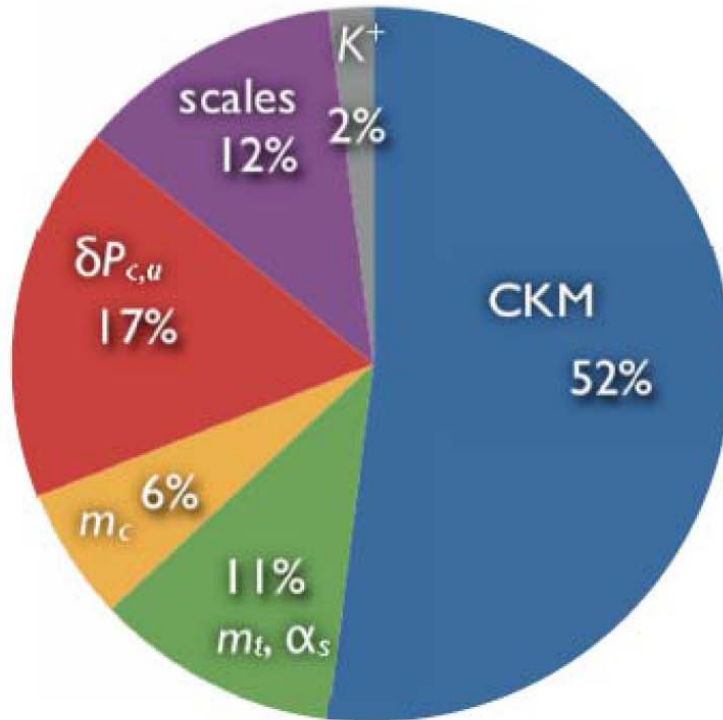
- Buchalla, Buras, 1993
- Lu, Wise, 1994
- Marciano, Parsa, 1996
- Misiak, Urban, 1999
- Buchalla, Buras, 1999
- Falk, Lewandowski, Petrov, 2000
- Isidori, Mescia, Smith, 2005
- Isidori, Martinelli, Turchetti, 2006
- Buras, Gorbahn, Haisch, Nierste, 2006
- Mescia, Smith, 2007
- Bijnens, Ghorbani, 2007
- Kühn, Steinhauser, Sturm, 2007
- Brod, Gorbahn, 2008

## BSM Excitement

- Grossman, Nir, 1997
- Buras, Romanino, Silvestrini, 1998
- Buras, Fleischer, 2001
- Grossman, Isidori, Murayama, 2004
- Buras, Ewerth, Jäger, Rosiek, 2004
- Choudhury, Gaur, Joshi, McKellar, '04
- He, Valencia, 2004
- Bobeth *et al.*, 2005
- Isidori, Mescia, Paradisi, Smith, Trine, 2006
- Blanke, 2009
- And many more—see Buras, Schwab, Uhlig, RMP 2008 for complete refs.

# Summary of SM Theory Uncertainties

CKM parameter uncertainties  
dominate the error budget today.



With foreseeable improvements, it is reasonable to expect the total SM theory error  $\leq 6\%$ .

A. Kronfeld

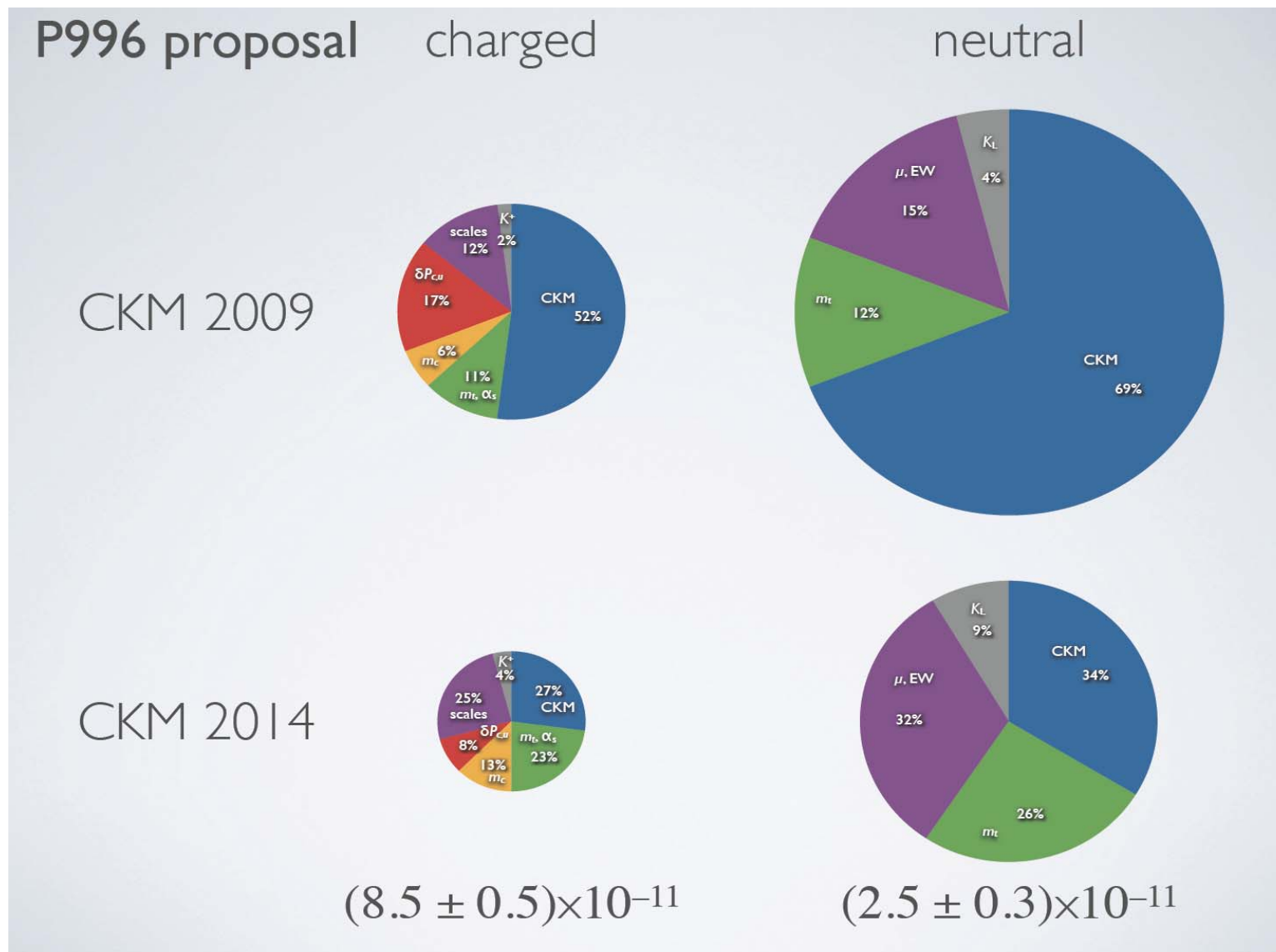
Unmatched by any other FCNC process (K or B).

30% deviation from the SM would be a  $5\sigma$  signal of NP

SM theory error for  $K_L^0 \rightarrow \pi^0 \nu \bar{\nu}$  mode exceed that for  $K^+ \rightarrow \pi^+ \nu \bar{\nu}$ .

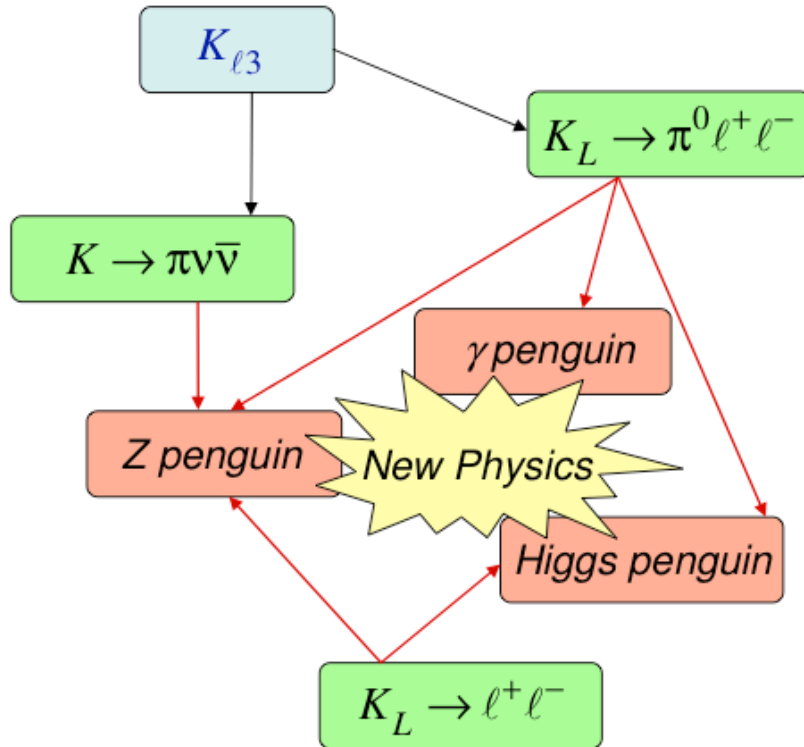
U. Haisch, arXiv:0707.3098

# Components of $K \rightarrow \pi\nu\bar{\nu}$ Uncertainty in the Standard Model

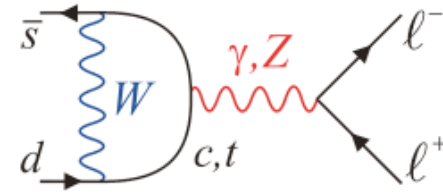


# LQCD and $K_2 \rightarrow \pi^0 e^+ e^- \dots$

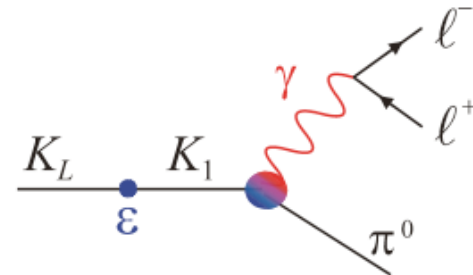
LD in rare K 3/10



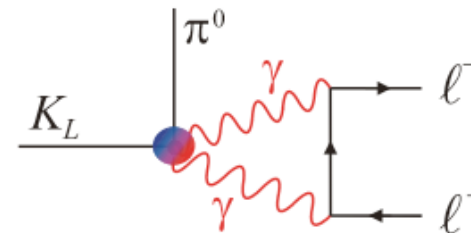
Direct CP-violation:



Indirect CP-violation:

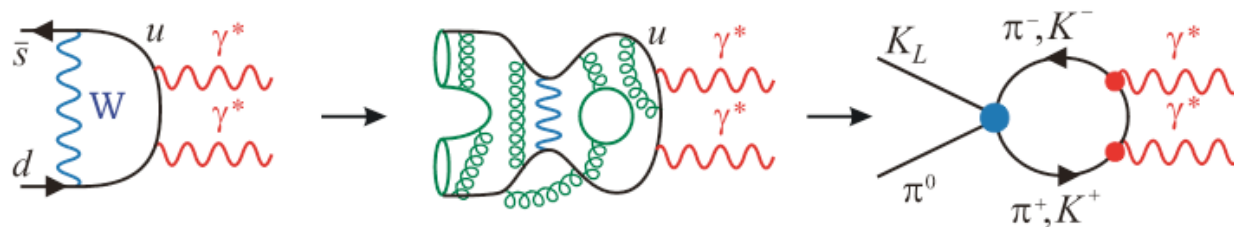


CP-conserving:



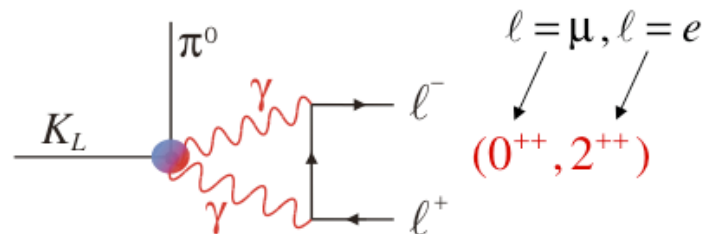
From NA62 Physics-Handbook: Christopher Smith

*C. CP-conserving long-distance double photon penguin*



LO ( $p^4$ ) is finite, produces  $l^+ l^-$  in a scalar state only (helicity-suppressed),

Higher order estimated using the  $K_L \rightarrow \pi^0 \gamma \gamma$  rate and spectrum:



- Production of  $(\mu^+ \mu^-)_{0^{++}}$  under control within 30%.

*Isidori, Unterdorfer, C.S. '04*

- No signal of  $(\gamma \gamma)_{2^{++}}$  implies  $(e^+ e^-)_{2^{++}}$  is negligible.

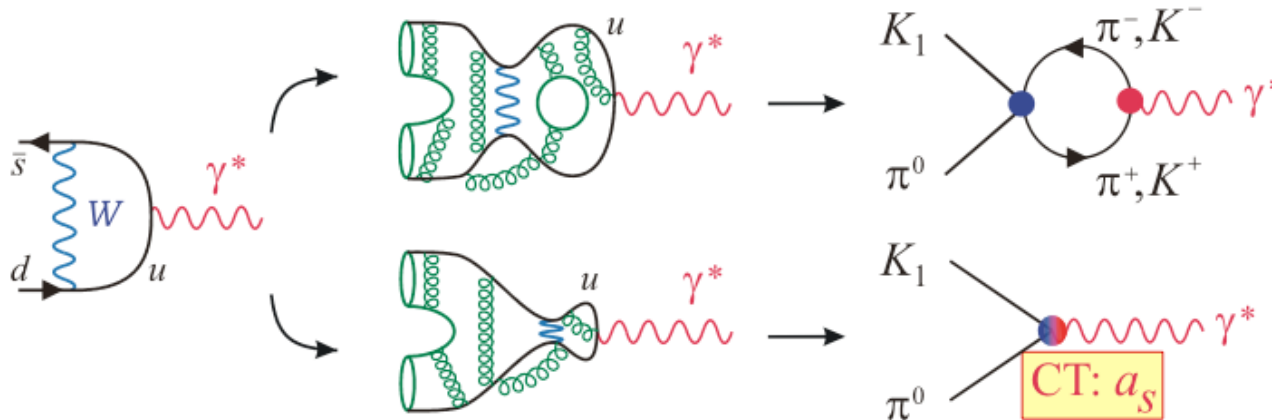
*Buchalla, D'Ambrosio, Isidori '03*

( $K_S \rightarrow \gamma \gamma$  is also useful to constrain the  $p^6$  LEC structure)

*B. Indirect CPV: Long-distance photon penguin*

D'Ambrosio et al. '98

Indirect CP-violation is  $K_L \rightarrow \epsilon K_1 \rightarrow \pi^0 \ell^+ \ell^-$ , related to  $K_S \rightarrow K_1 \rightarrow \pi^0 \ell^+ \ell^-$ :



Loops are rather small, a single LEC  $a_S$  dominates.

It is fixed from  $K_S \rightarrow \pi^0 \ell^+ \ell^-$  (up to its sign) measured by NA48:

$$\left. \begin{aligned} Br(K_S \rightarrow \pi^0 e^+ e^-)_{m_{ee} > 165 \text{ MeV}} &= (3.0^{+1.5}_{-1.2} \pm 0.2) \times 10^{-9} \\ Br(K_S \rightarrow \pi^0 \mu^+ \mu^-) &= (2.9^{+1.4}_{-1.2} \pm 0.2) \times 10^{-9} \end{aligned} \right\} \rightarrow |a_S| = 1.2 \pm 0.2$$

K1 and K2 interference into the *same*  $\pi^0 e^+ e^-$  final state can boost the K2 signal out of the  $K_L \rightarrow \gamma\gamma ee$  background!

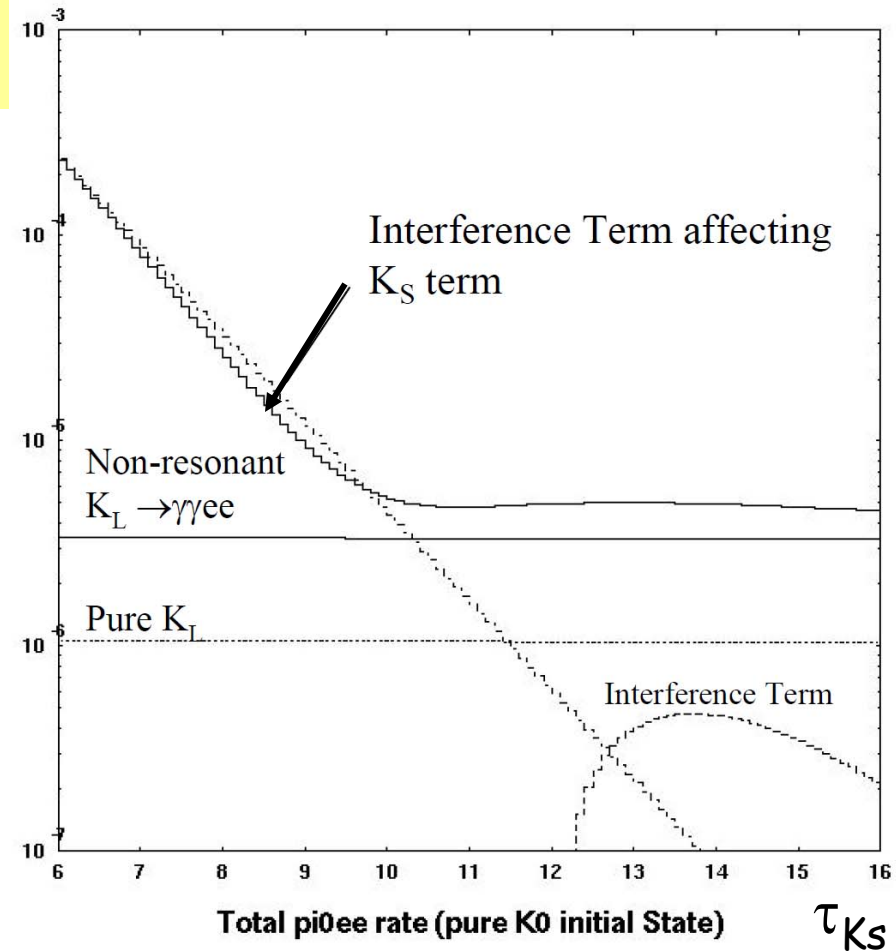
$$\frac{dN}{dt} \sim e^{-t/t_S} + 2D\sqrt{R} \cdot \cos(\Delta m + \Delta\phi) e^{-t(t_S+t_L)/(2t_S t_L)} + (R + R_{ee\gamma\gamma}) e^{-t/t_L} \quad (5)$$

where  $D=0.3$  (dilution factor),  $\Delta m = m_L - m_S$ ,  $\Delta\phi = \phi_S - \phi_L = 57^\circ$  [4], and

$$R = \left[ 15.3 - 6.8 \frac{\text{Im}(\lambda_t)}{A_S} + 2.8 \left( \frac{\text{Im}(\lambda_t)}{A_S} \right)^2 \right] \quad (6)$$

$$R_{ee\gamma\gamma} = 10^{-12} \frac{t_S}{t_L} \frac{1}{5.2 \cdot 10^{-9}} \quad 10^{-10} \frac{t_S}{t_L} \frac{1}{A_S^2 5.2 \cdot 10^{-9}}$$

**$D$  is the dilution factor. For high energy K production  $D = 0.3$  ; For threshold production  $D = 1.0$**

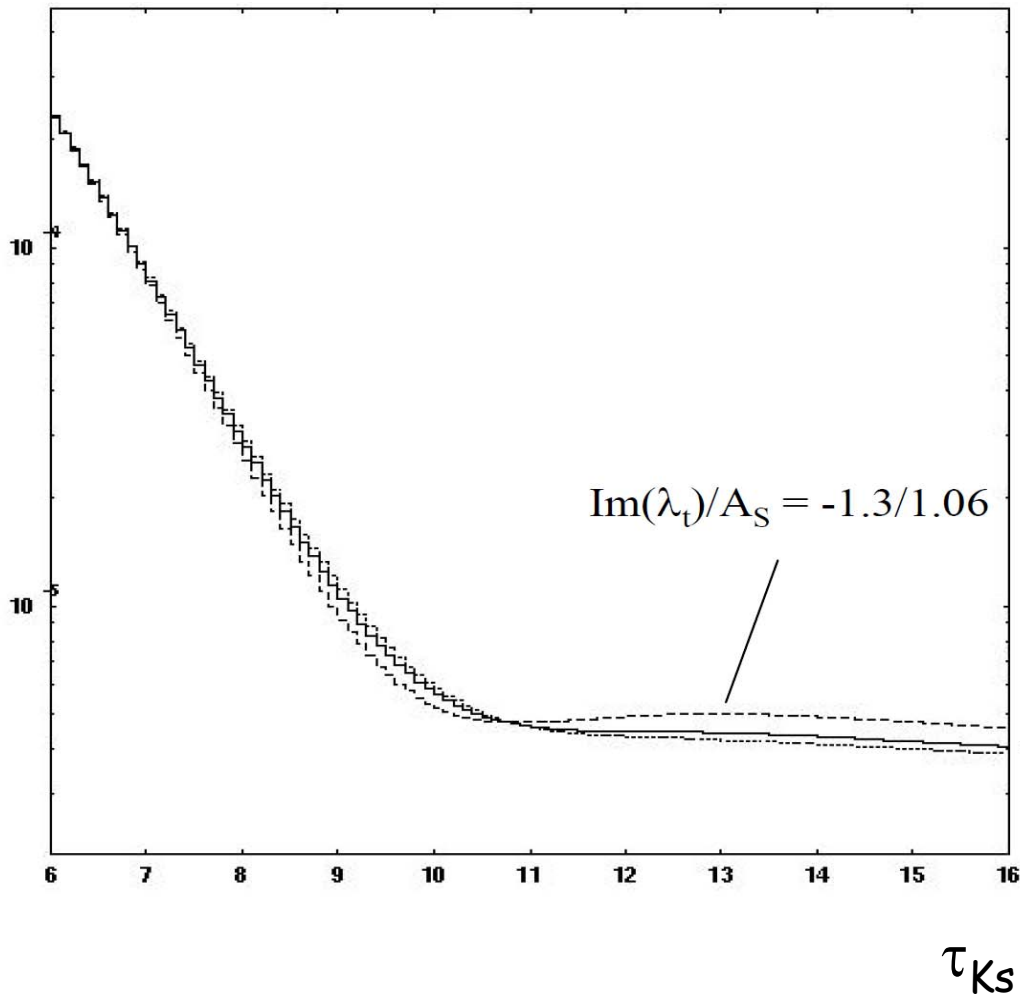


Number of  $\tau_S$  lifetimes from target

Hogan Nguyen, 4<sup>th</sup>  
Project-X workshop.



# The Sign of $A_S$ is very important



For  $\text{Im}(\lambda_t)/A_S = +1.3/1.06$   
 there is a great loss of resolution  
 extracting  $\text{Im}(\lambda_t)$

$\text{Im}(\lambda_t)/A_S = +1.3/1.06$

$\text{Im}(\lambda_t) = 0$

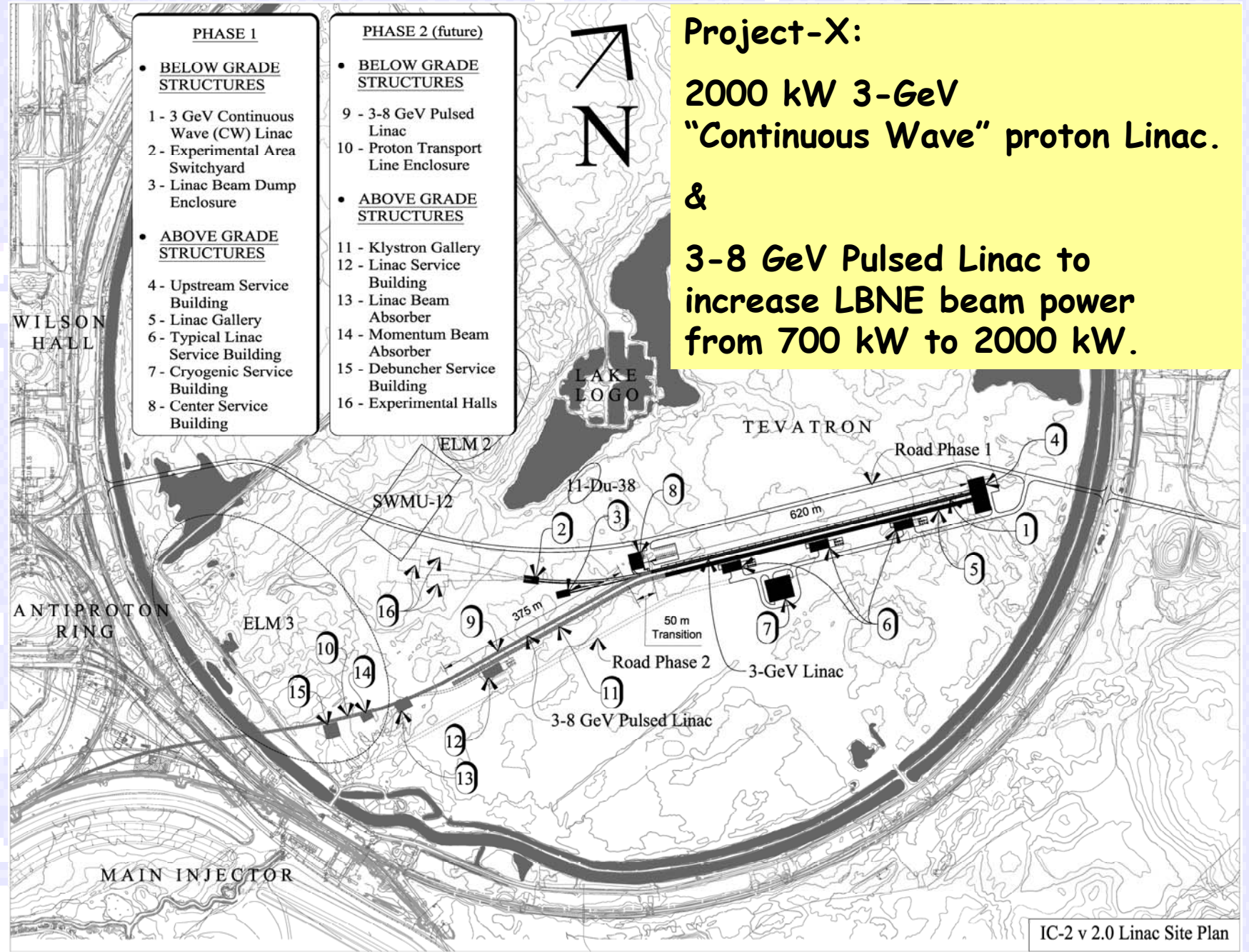
$\text{Im}(\lambda_t)$  in units of  $10^{-4}$

# Summary of LQCD Targets for Kaon Physics

- $\text{Re}(\varepsilon'_K/\varepsilon_K)$  !! New Physics could be hiding in plain sight.
- CKM parameters, most notably  $V_{cb}$  and  $V_{ub}$ . Important for establishing modest measured enhancements of  $K \rightarrow \pi VV$  as new physics. Alternatively a precision measurement of  $K \rightarrow \pi VV$  could ultimately be the best measure of  $V_{cb}$ .
- Continued progress on  $B_K$ ,  $f_K$ , and form factors.
- Initiate a campaign on radiative decays. The theoretical understanding of  $K_L \rightarrow \gamma^* \gamma^*$  is not robust, and must become solid to interpret  $K_L \rightarrow \mu\mu$ . Understanding the phase of  $K_L \rightarrow \pi^0 \gamma^*$  will be critical to developing a Project-X assault on  $K_L \rightarrow \pi^0 e^+ e^-$ .

**Project-X:**  
**2000 kW 3-GeV**  
**"Continuous Wave" proton Linac.**  
**&**  
**3-8 GeV Pulsed Linac to**  
**increase LBNE beam power**  
**from 700 kW to 2000 kW.**

- | PHASE 1  | PHASE 2 (future)   |
|--|--|
| <ul style="list-style-type: none"> <li><b>BELOW GRADE STRUCTURES</b></li> <li>1 - 3 GeV Continuous Wave (CW) Linac</li> <li>2 - Experimental Area Switchyard</li> <li>3 - Linac Beam Dump Enclosure</li> </ul>   | <ul style="list-style-type: none"> <li><b>BELOW GRADE STRUCTURES</b></li> <li>9 - 3-8 GeV Pulsed Linac</li> <li>10 - Proton Transport Line Enclosure</li> </ul>  |
| <ul style="list-style-type: none"> <li><b>ABOVE GRADE STRUCTURES</b></li> <li>4 - Upstream Service Building</li> <li>5 - Linac Gallery</li> <li>6 - Typical Linac Service Building</li> <li>7 - Cryogenic Service Building</li> <li>8 - Center Service Building</li> </ul> | <ul style="list-style-type: none"> <li><b>ABOVE GRADE STRUCTURES</b></li> <li>11 - Klystron Gallery</li> <li>12 - Linac Service Building</li> <li>13 - Linac Beam Absorber</li> <li>14 - Momentum Beam Absorber</li> <li>15 - Debuncher Service Building</li> <li>16 - Experimental Halls</li> </ul> |



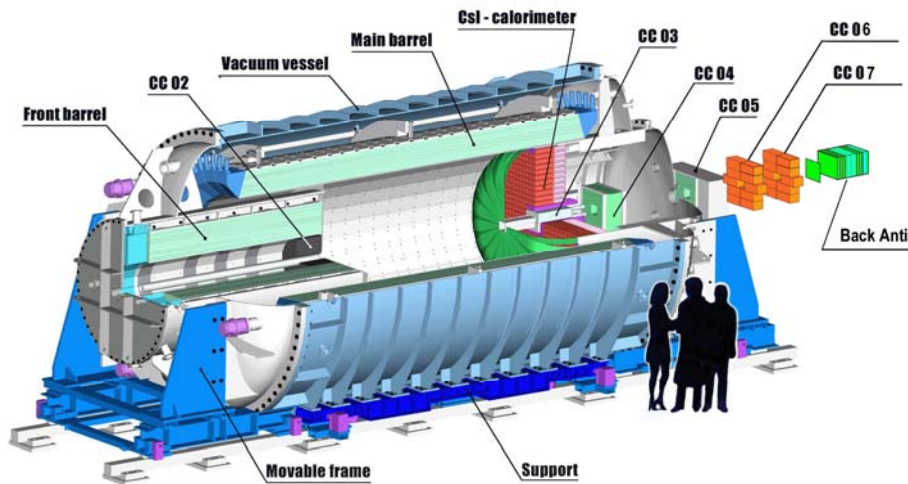
IC-2 v 2.0 Linac Site Plan

# $K_L \rightarrow \pi^0 \nu \bar{\nu}$ Experimental Challenge: "Nothing-in nothing out"

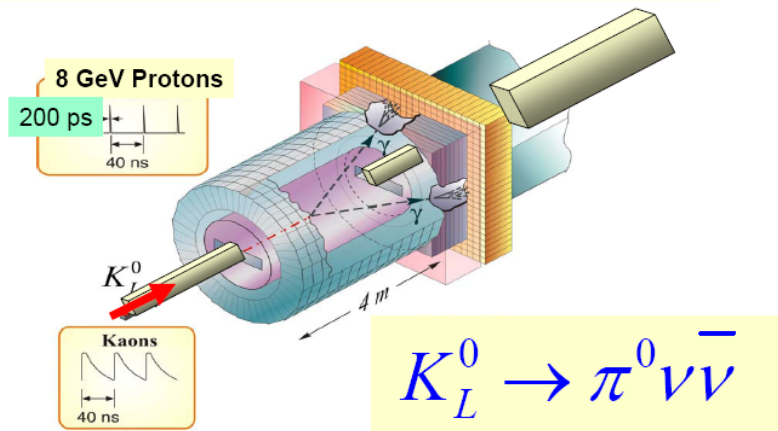
- KEK/JPARC approach emphasizes high acceptance for the two decay photons while vetoing everything else:

A hermetic "bottle" approach.

- The original KOPIO concept measures the kaon momentum and photon direction... Good! But costs detector acceptance and requires a large beam to compensate. Project-X Flux can get back to small kaon beam!



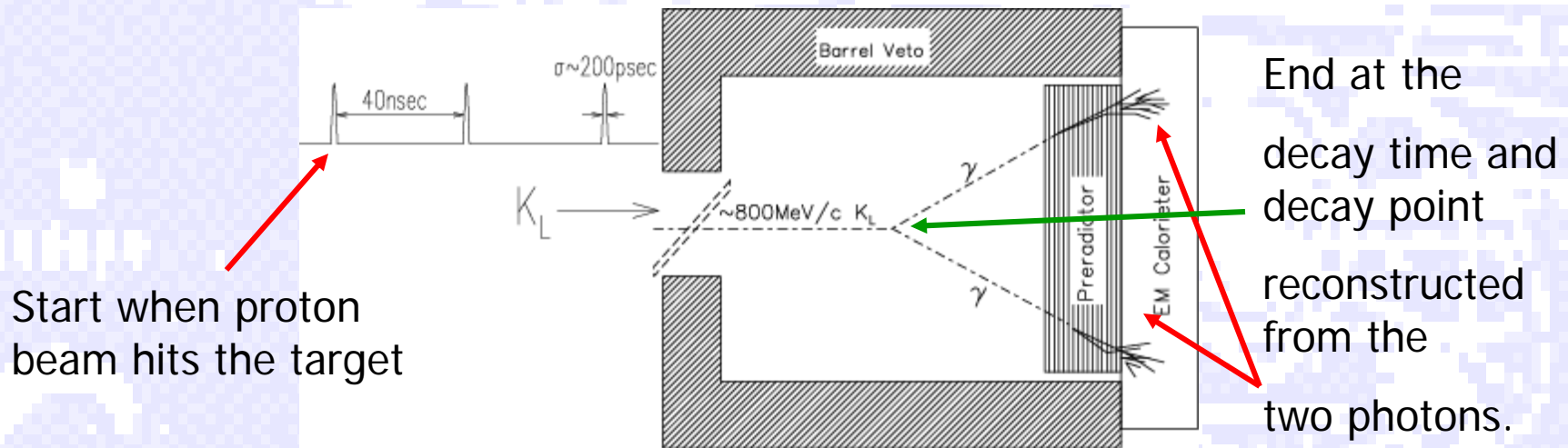
## Another $K_L^0 \rightarrow \pi^0 \nu \bar{\nu}$ Experiment Concept



- Use TOF to work in the  $K_L^0$  c.m. system
- Identify main 2-body background  $K_L^0 \rightarrow \pi^0 \pi^0$
- Reconstruct  $\pi^0 \rightarrow \gamma\gamma$  decays with pointing calorimeter
- $4\pi$  solid angle photon and charged particle vetos

# KOPIO inspired: Micro-bunch the beam, TOF determines $K_L$ momentum.

Fully reconstruct the neutral Kaon in  $K_L \rightarrow \pi^0 \rightarrow \gamma \gamma$  by measuring the Kaon momentum by time-of-flight.



Timing uncertainty due to microbunch width should not dominate the measurement of the kaon momentum; requires RMS width < 200ps. CW linac pulse timing of less than 50ps is intrinsic.

# An Incomplete Menu of World Class Research Targets Enabled by Project-X

## Neutrino Physics:

- Mass Hierarchy
- CP violation
- Precision measurement of the  $\theta_{23}$  (atmospheric mixing). Maximal??
- Anomalous interactions, e.g.  $\nu_{\mu} \rightarrow \nu_{\tau}$  probed with target emulsions ([Madrid Neutrino NSI Workshop](#), Dec 2009)
- Next generation precision cross section measurements

# An Incomplete Menu of World Class Research Targets Enabled by Project-X. continued...

## Muon Physics:

- Next generation muon-to-electron conversion experiment, new techniques for higher sensitivity and/or other nuclei.
- Next generation  $(g-2)_\mu$  if motivated by next round, theory, LHC. New techniques proposed to JPARC that are beam-power hungry...
- $\mu$  edm
- $\mu \rightarrow 3e$
- $\mu^+e^- \rightarrow \mu^-e^+$
- $\mu^-A \rightarrow \mu^+A'$  ;  $\mu^-A \rightarrow e^+A'$  ;  $\mu^-e^-(A) \rightarrow e^-e^-(A)$
- Systematic study of radiative muon capture on nuclei.

# An Incomplete Menu of World Class Research Targets Enabled by Project-X. continued...

## Baryons:

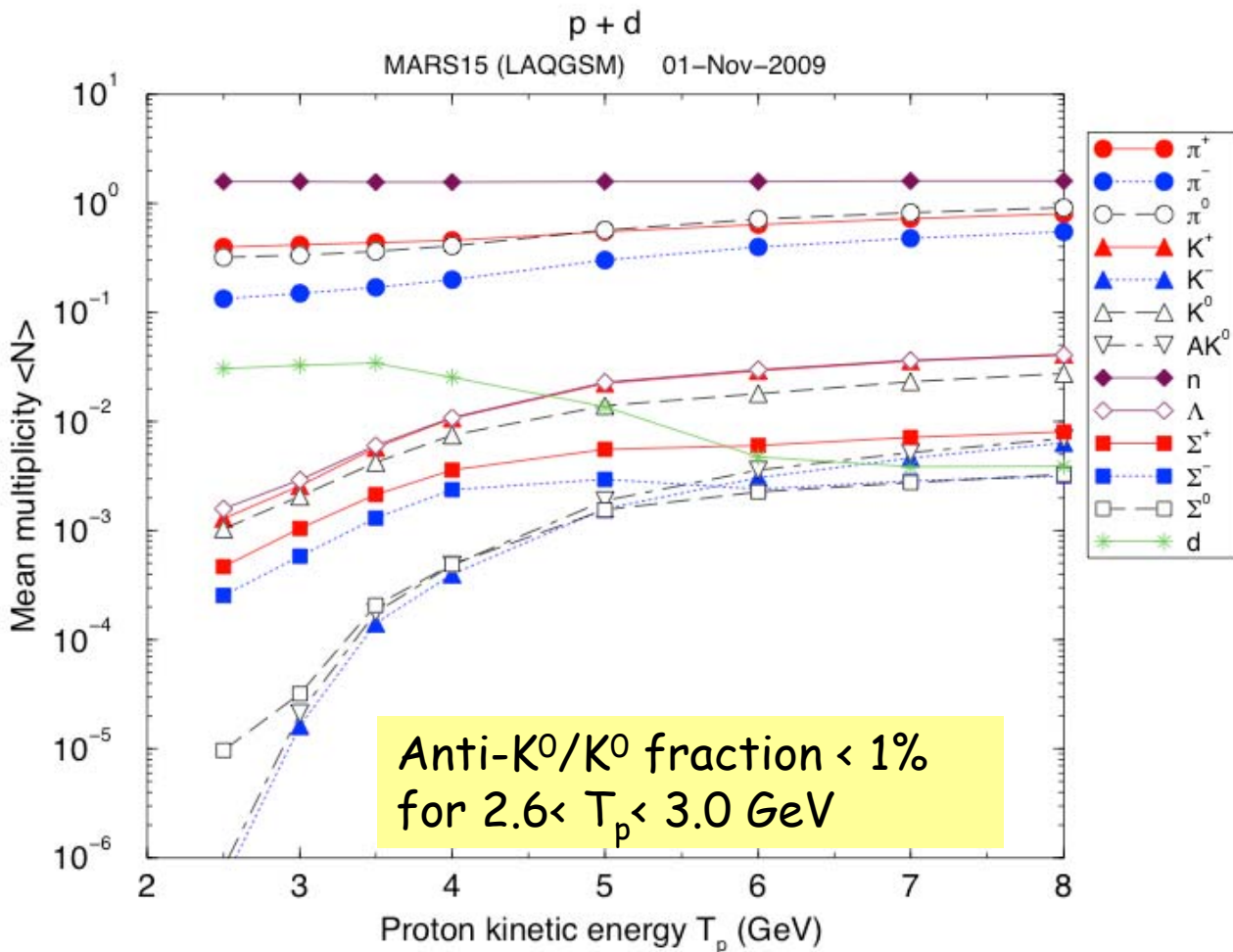
- $pp \rightarrow \Sigma^+ K^0 p^+$ ;  $\Sigma^+ \rightarrow p^+ \mu^+ \mu^-$  (HyperCP anomaly, and other rare  $\Sigma^+$  decays)
- $pp \rightarrow \overline{K^+} \Lambda^0 p^+$ ;  $\Lambda^0$  ultra rare decays
- $\Lambda^0 \leftrightarrow \overline{\Lambda^0}$  oscillations (Project-X operates below anti-baryon threshold)
- neutron EDM

## Nuclei:

- Production of Ra, Rn, Fr isotopes for nuclear edm experiments that are uniquely sensitive to Quark-Chromo and electron EDM's.

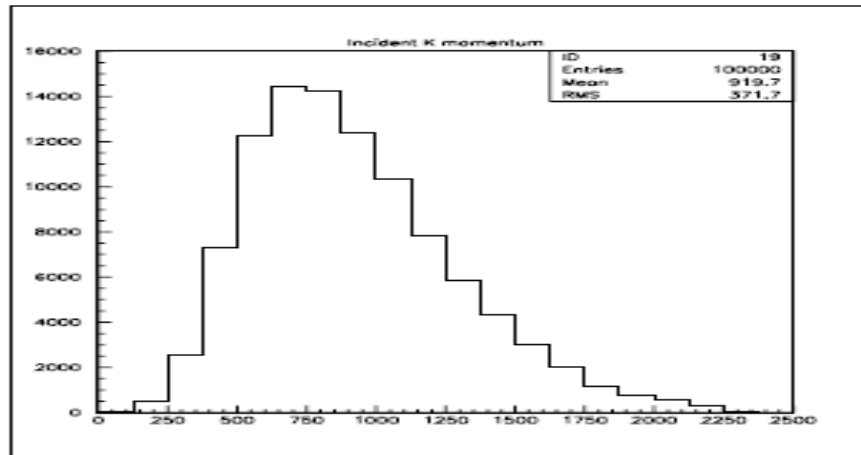
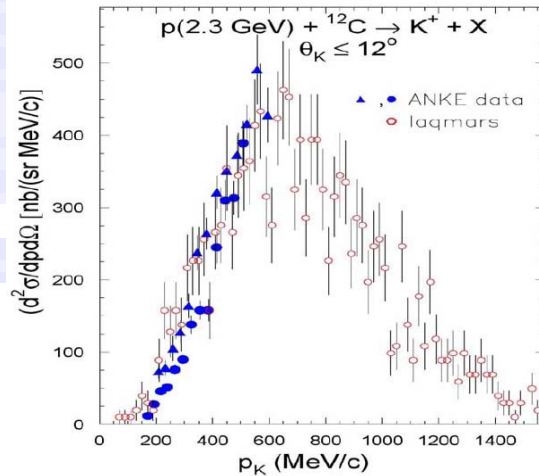


# IC2 is high power, but what about kaon yields??



LAQGSM/MARS-15

# KOPIO and ICD-2 kaon momentum spectra comparison



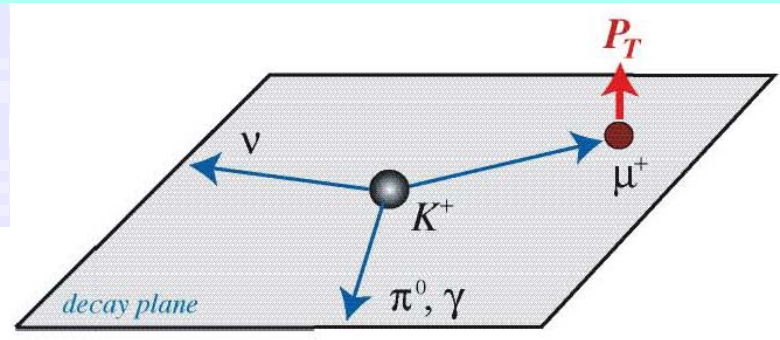
KOPIO  
Proposal

Figure 13:  $K_L^0$  spectrum incident on KOPIO decay volume.

# Transverse $\mu^+$ polarization in $K_{\mu 3}$

$K^+ \rightarrow \pi^0 \mu^+ \nu$  decay

$$P_T = \frac{\sigma_\mu \cdot (\mathbf{p}_{\pi^0, \gamma} \times \mathbf{p}_{\mu^+})}{|(\mathbf{p}_{\pi^0, \gamma} \times \mathbf{p}_{\mu^+})|}$$



- $P_T$  is T-odd, and spurious effects from final state interaction are small:  $P_T(\text{FSI}) < 10^{-5}$

Non-zero  $P_T$  is a signature of T violation.

- Standard Model (SM) contribution to  $P_T$ :  $P_T(\text{SM}) < 10^{-7}$

$P_T$  in the region  $10^{-3} \sim 10^{-4}$  is a sensitive probe of CP violation beyond the SM.

- There are theoretical models of **new physics** which allow a sizable  $P_T$  without conflicting with other experimental constraints.

**TREK experiment aims for a sensitivity of  $10^{-4}$**

# Direct CP violation

- Direct CP violation in  $K^0$  system :

$$\text{Re}(\varepsilon'/\varepsilon) = (1.66 \pm 0.26) \times 10^{-3} \quad \Rightarrow$$

$$\frac{\Gamma(K^0 \rightarrow \pi^+ \pi^-) - \Gamma(\bar{K}^0 \rightarrow \pi^+ \pi^-)}{\Gamma(K^0 \rightarrow \pi^+ \pi^-) + \Gamma(\bar{K}^0 \rightarrow \pi^+ \pi^-)} = (5.04 \pm 0.22) \times 10^{-6} \equiv R$$

- *If this effect is due to Higgs dynamics:*

Because there is no  $\Delta I=1/2$  suppression ( $\sim 20$ ) in the  $K^+$  system

$$P_T \sim R \times 20 = 5 \times 10^{-6} \times 20 \sim 10^{-4}$$

-- *unless enhanced couplings to leptons!*

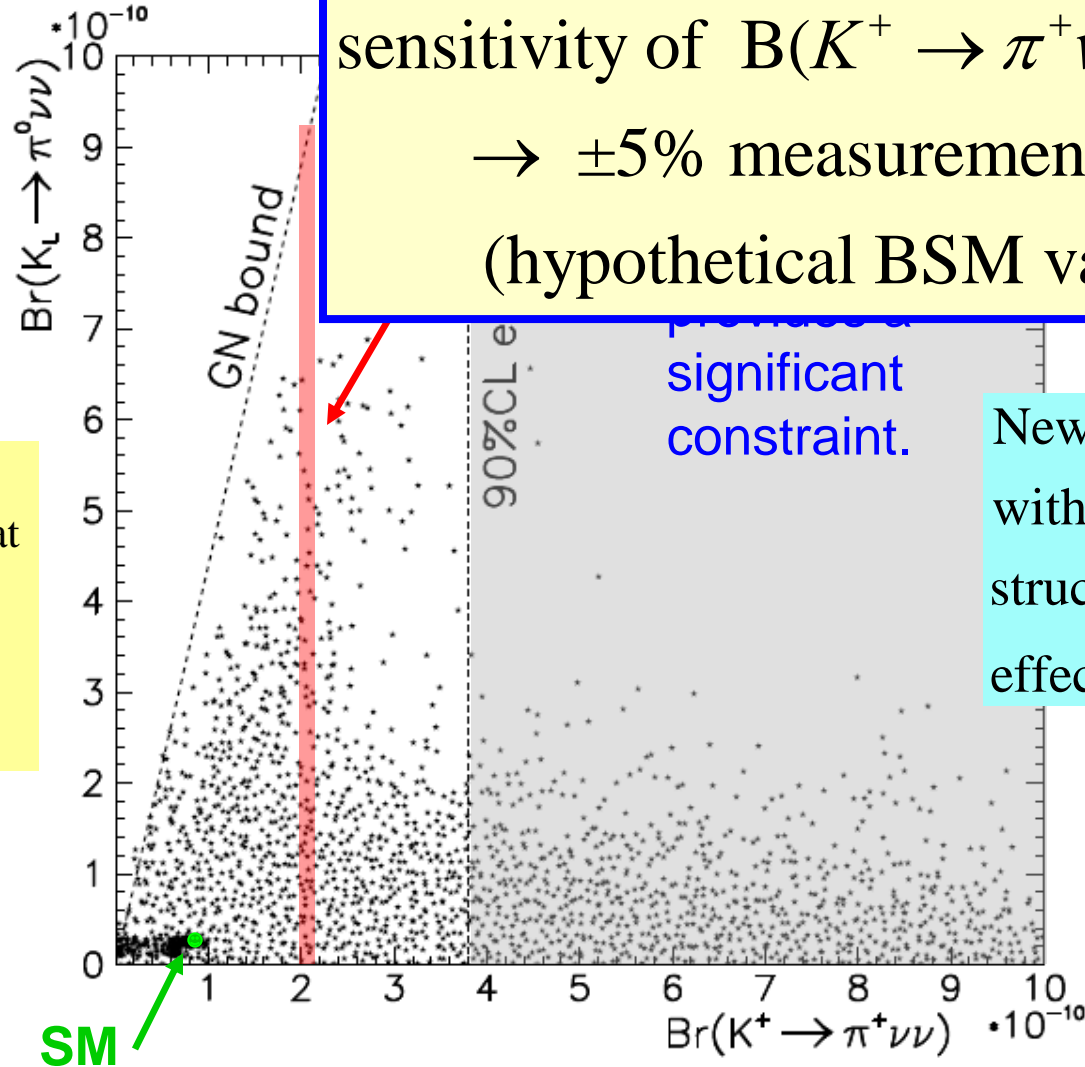
(I. Bigi, CERN Flavor WS, 2007 )

# General MSSM with R-parity

Fermilab P996 will improve the sensitivity of  $B(K^+ \rightarrow \pi^+ \nu \bar{\nu})$  by  $>100!$   
 $\rightarrow \pm 5\%$  measurement  
 (hypothetical BSM value)

Buras et al, NP B714,103(2005)

Points from a scan of MSSM parameters that satisfy experimental constraints except  $B(K^+ \rightarrow \pi^+ \nu \bar{\nu})$



New Physics models with generic flavor structure induce large effects in  $K^+ \rightarrow \pi^+ \nu \bar{\nu}$ .

$R$  Parity:  $R = (-1)^{2j+3B+L}$ .

# $K^+ \rightarrow \pi^+ \nu \bar{\nu}$ in the LHC Era

## New Physics found at LHC

➤ New particles with unknown flavor- and CP-violating couplings



Precision flavor-physics experiments needed to help sort out the flavor- and CP-violating couplings of the NP.



Quark Gen.	Processes to Study NP
1	$\mu$ -e Conversion, $\pi \rightarrow e\nu$
2	$K^+ \rightarrow \pi^+ \nu \bar{\nu}$ , $K_L^0 \rightarrow \pi^0 \nu \bar{\nu}$
3	$b \rightarrow s\gamma$ , other rare decays

## New Physics NOT found at LHC



Precision flavor-physics experiments needed -> sensitive to NP at mass scales beyond the reach of the LHC (through virtual effects).



$K^+ \rightarrow \pi^+ \nu \bar{\nu}$  and  $K_L^0 \rightarrow \pi^0 \nu \bar{\nu}$  have special status because of their small SM uncertainties and large NP reach.



Precision measurement of  $B(K^+ \rightarrow \pi^+ \nu \bar{\nu})$  is an immediate high priority.

\* It is experimentally more accessible than  $K_L^0 \rightarrow \pi^0 \nu \bar{\nu}$ .

\* The result can guide the Project-X Intensity Frontier program.

# STANDARD MODEL

$$B_{\text{SM}}(K^+ \rightarrow \pi^+ \nu \bar{\nu}) = \frac{\tau_{K^+} M_{K^+}^5}{32\pi^3} (1 + \Delta_{\text{EM}}) \left| f_+^{K^+ \pi^+}(0) \right|^2 I_{\nu^+} \left| \frac{G_F \alpha(M_Z)}{2\pi\sqrt{2} \sin^2 \theta_W} Y \right|^2$$

kinematics    EM    QCD    weak

$$B_{\text{SM}}(K_L \rightarrow \pi^0 \nu \bar{\nu}) = \frac{\tau_{K_L} M_{K_L}^5}{32\pi^3} \left| f_+^{K^0 \pi^0}(0) \right|^2 I_{\nu^0} \left| \frac{G_F \alpha(M_Z)}{2\pi\sqrt{2} \sin^2 \theta_W} \text{Im}Y \right|^2$$

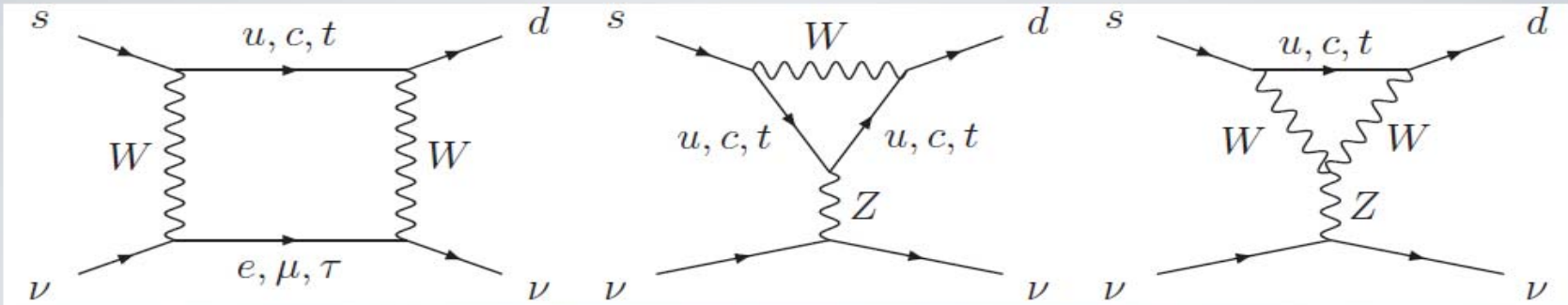
$$\frac{g^4}{16\pi^2 M_W^2}$$

$K_S$  has  $\text{Re}Y$

Andreas Kronfeld, 4<sup>th</sup> PX Workshop

April 27th 2010.

R. Tschirhart - Fermilab



- Induced in SM at one (and higher) loop(s):

$$\begin{aligned}
 Y &= V_{td}^* V_{ts} X(x_t) + V_{cd}^* V_{cs} X(x_c) + V_{ud}^* V_{us} X(x_u) \\
 &= V_{td}^* V_{ts} X(x_t) + V_{cd}^* V_{cs} [X(x_c) + |V_{us}|^4 \delta P_{c,u}]
 \end{aligned}$$

where  $X(x_q) = \frac{1}{3} \sum_l X(x_q, x_l)$ ,  $x_q = m_q^2 / M_W^2$ .

- GIM mechanism stems from CKM  $V_{ud}^* V_{us} = -V_{td}^* V_{ts} - V_{cd}^* V_{cs}$ .
- Last term is omnibus for higher dimension & long distance.



# $K^+ \rightarrow \pi^+ \nu \bar{\nu}$ History

