

# Lattice meets Experiment: BSM

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USQCD all hands meeting, Fermilab  
May 4<sup>th</sup>, 2012

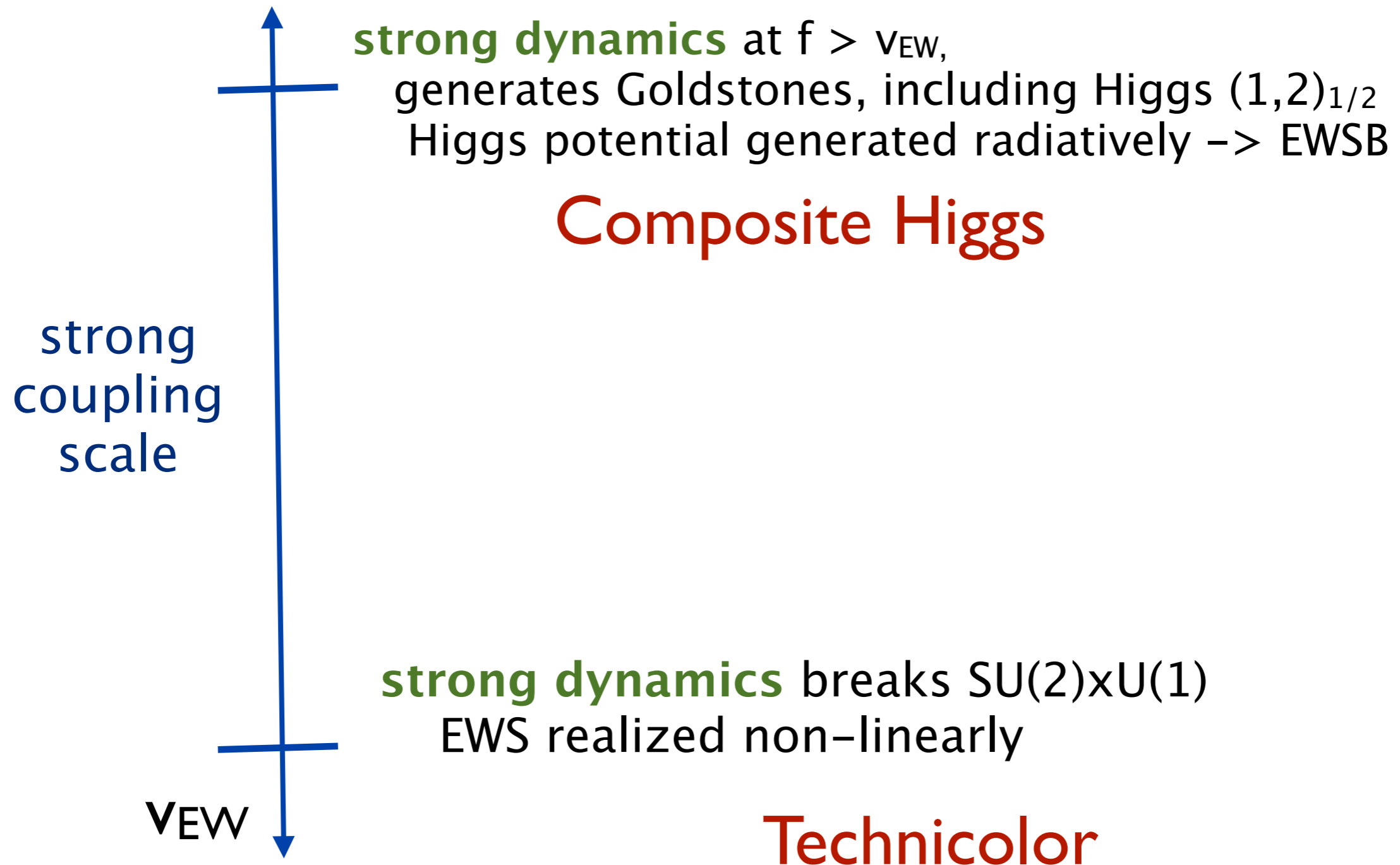
# synopsis of the interplay between lattice and BSM phenomenology/experiment

**Lattice Meets Experiment 2011: Beyond the Standard Model**



US Lattice Quantum Chromodynamics

the natural setting for lattice in BSM is  
new TeV-scale strong dynamics



wait... Technicolor?!?!

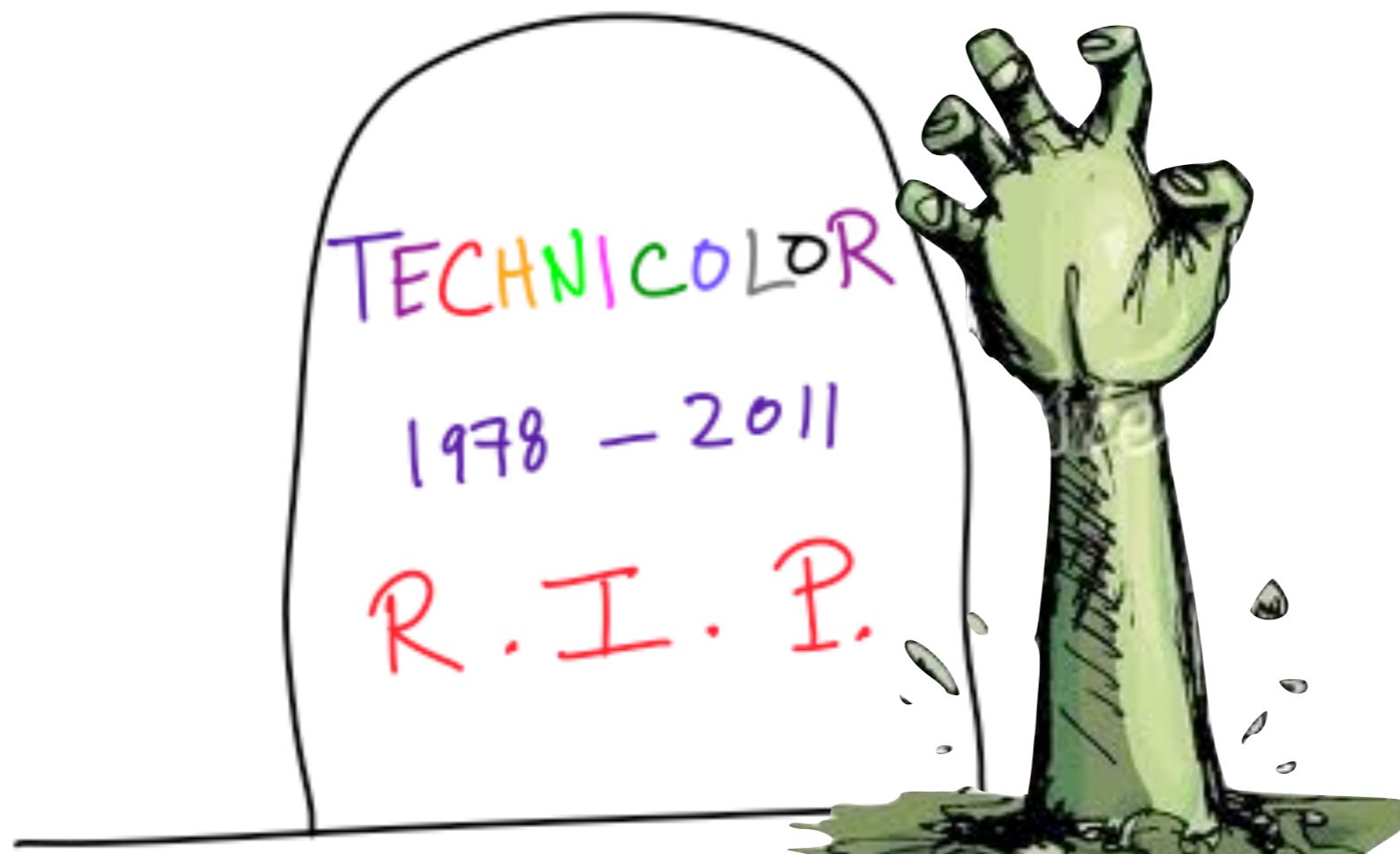
TRIUMPH OF WEAK COUPLING



Nima Arkani-Hamed, Madrid 12/16/11

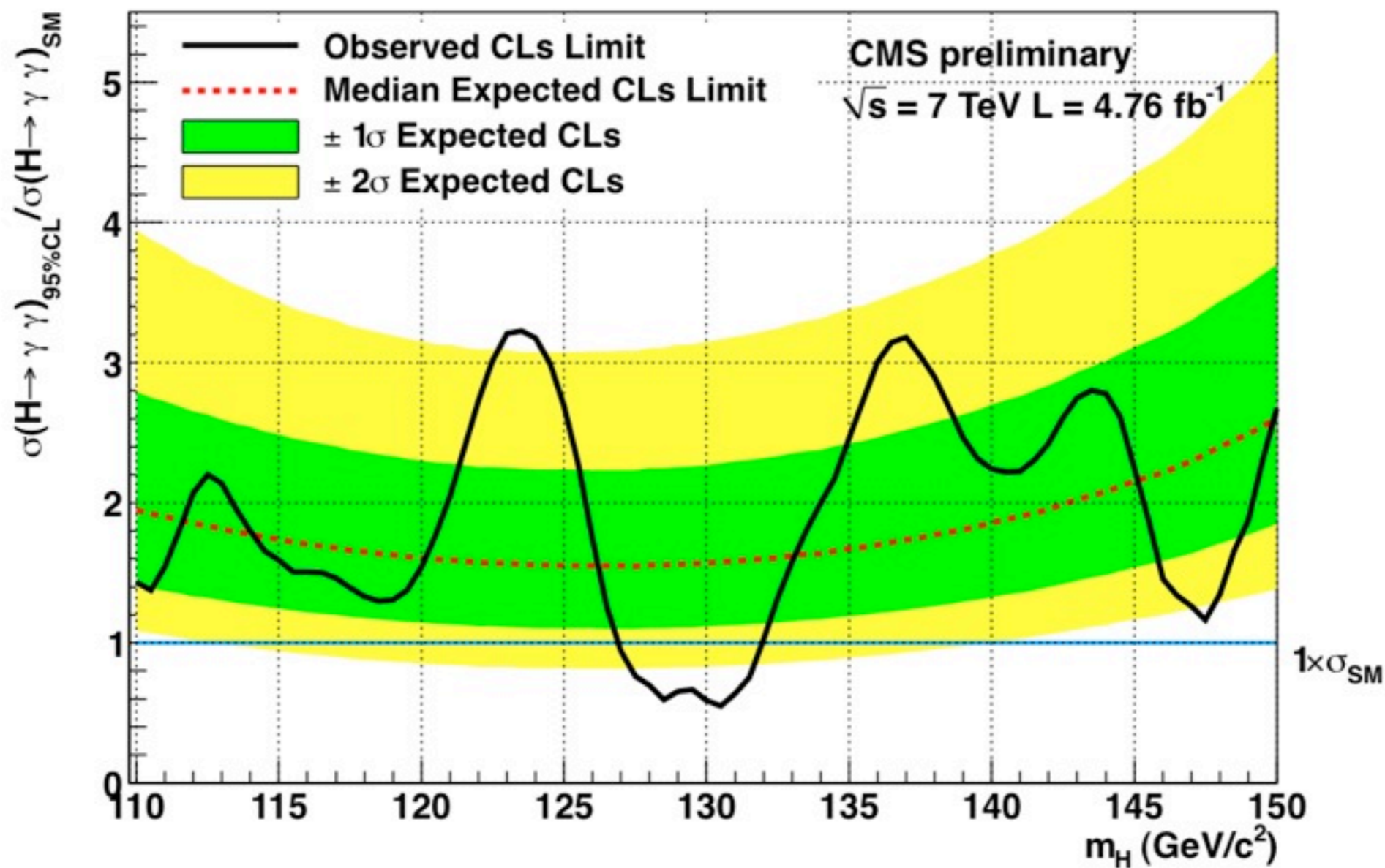
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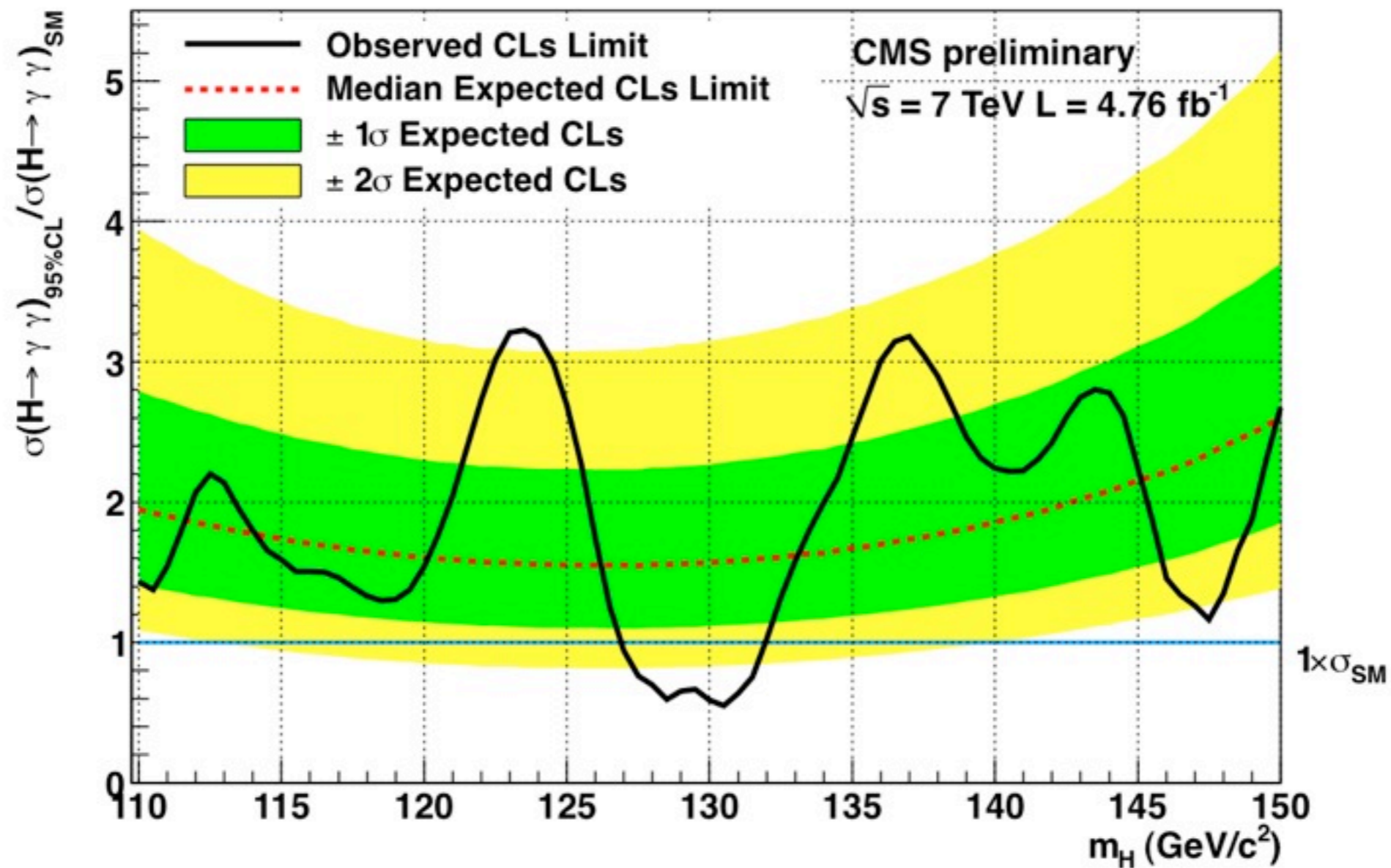
Nima Arkani-Hamed, Madrid 12/16/11

why so skeptical? as a wise experimentalist told me...



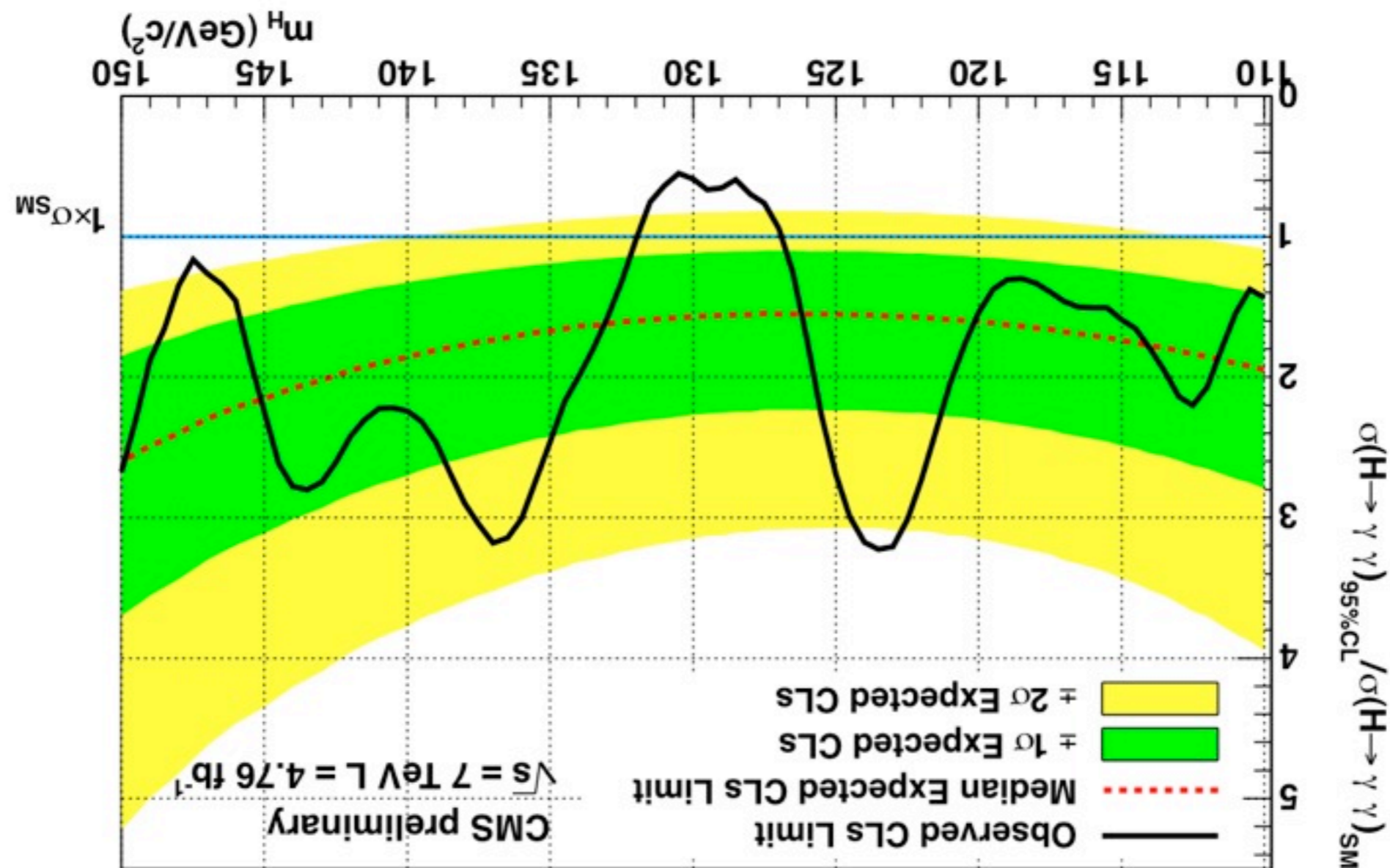
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be wary of peaks if you also see them with the graph upside-down



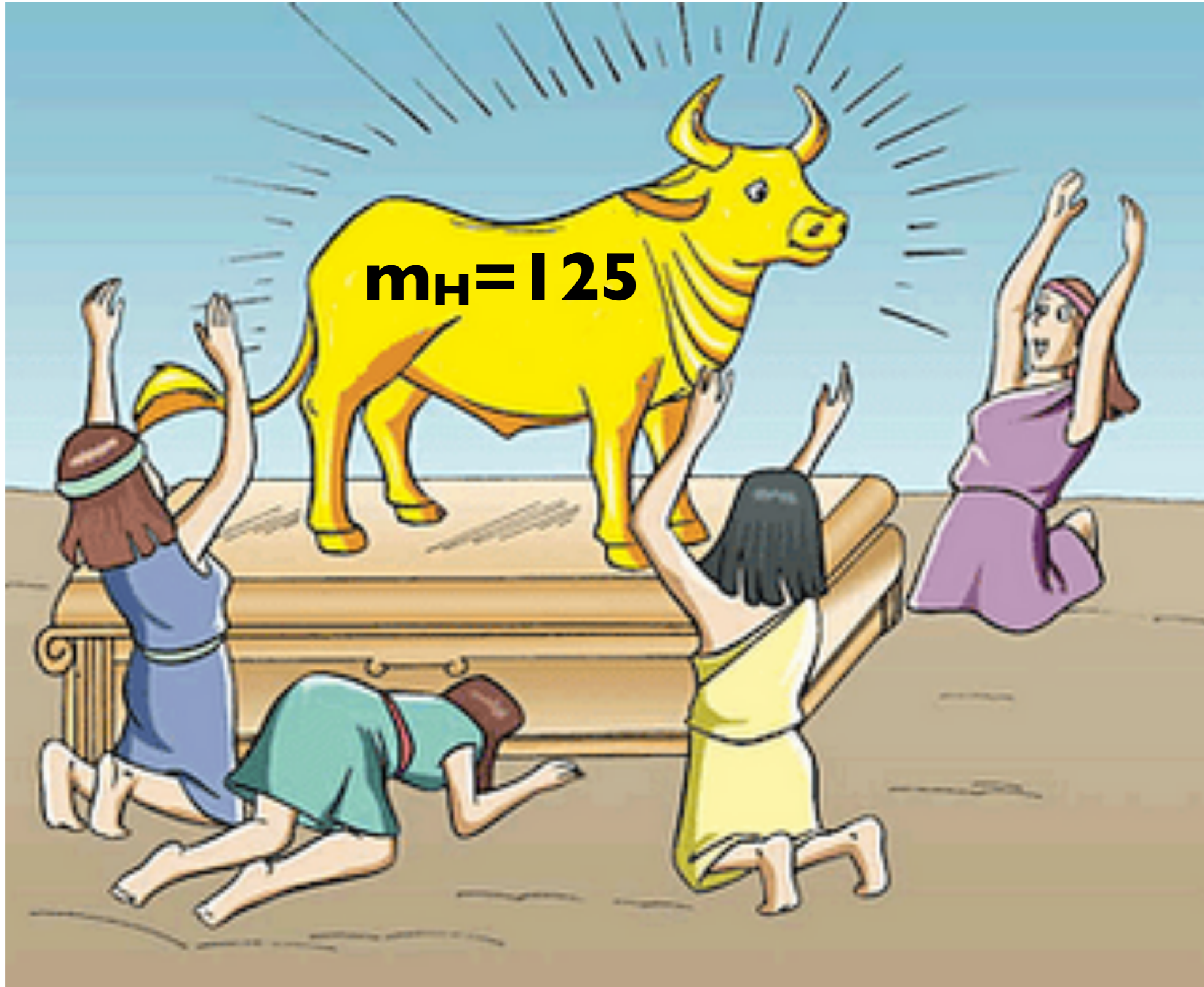
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... so lets not get carried away



on a more serious note

**Higgs boson is not discovered yet**

if it is:      **composite** or **fundamental?**

if it isn't:      **what is there?**

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lattice input  
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# on a more serious note

**Higgs boson is not discovered yet**

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**what is there?**

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umm.. where are all those superpartners?

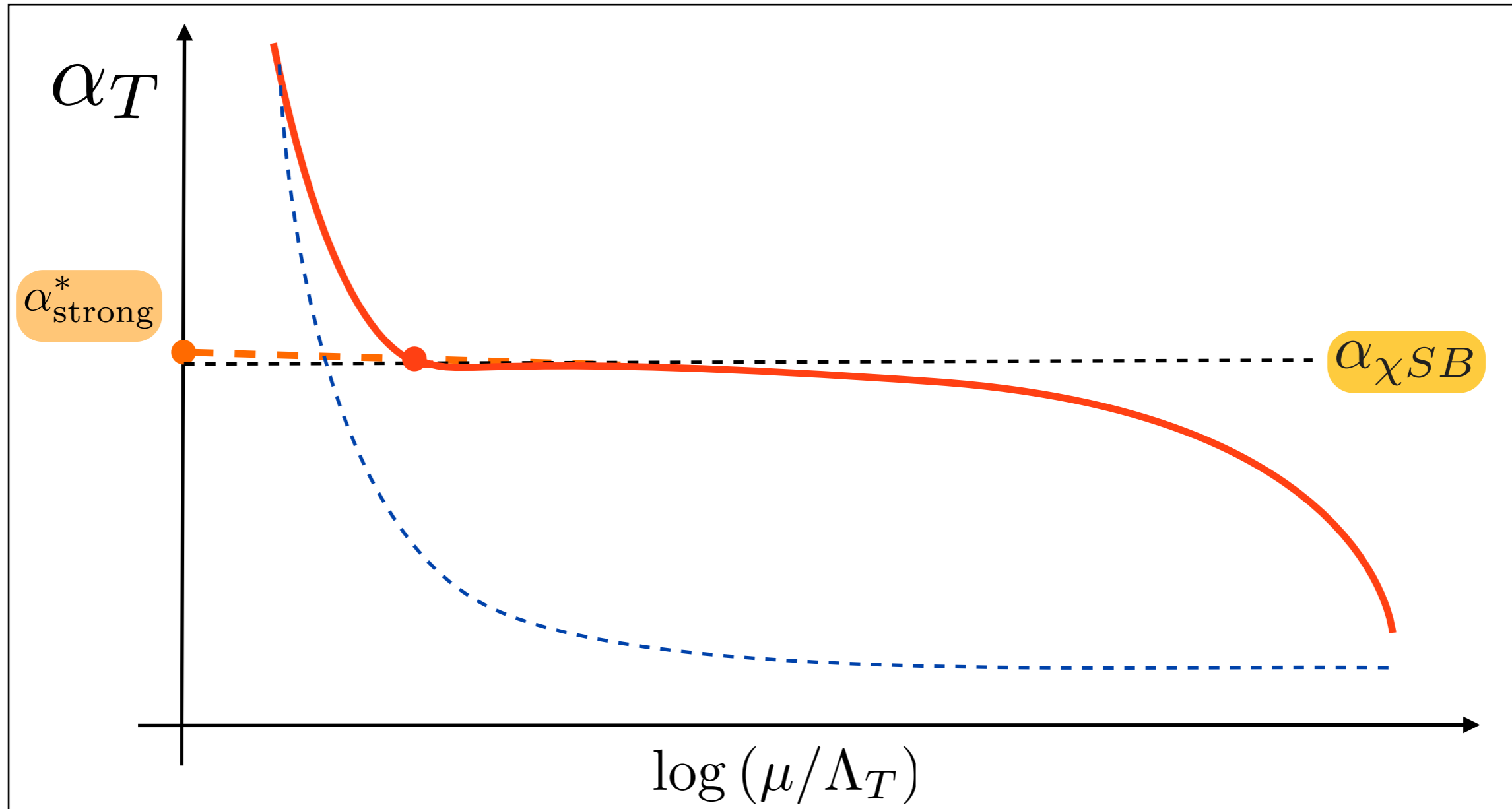
generic problem with new strong dynamics,

how do you get the physics you want from new dynamics without side effects?

want: W/Z masses, fermion masses, CKM

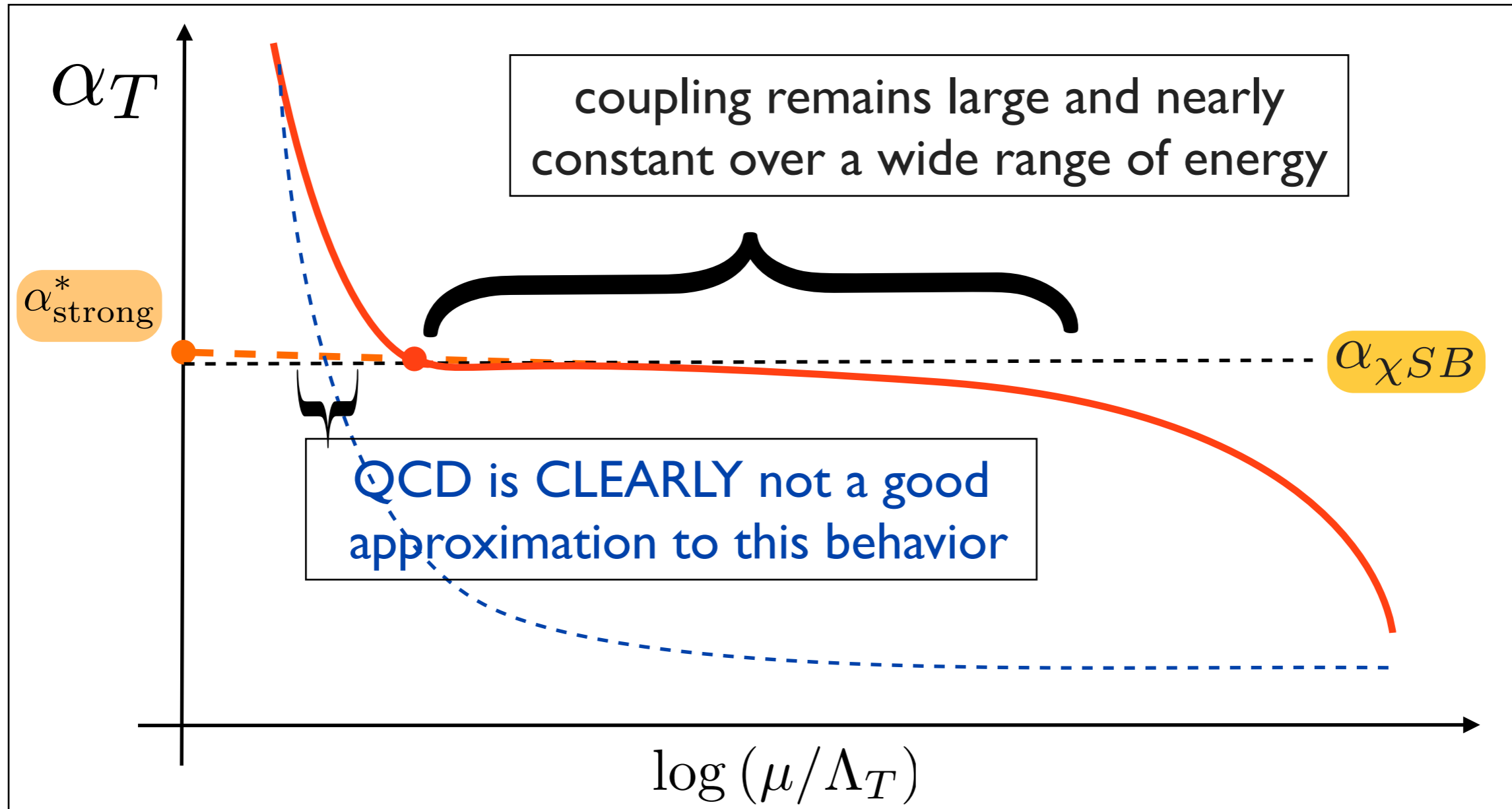
don't want: **flavor** precision electroweak  
EDMs proton decay  
$$\frac{(\bar{f}f)(\bar{f}f)}{\Lambda^2}$$

(near) conformal gauge theory  $\rightarrow$  separates scales



BSM lattice has focused on studying this scenario

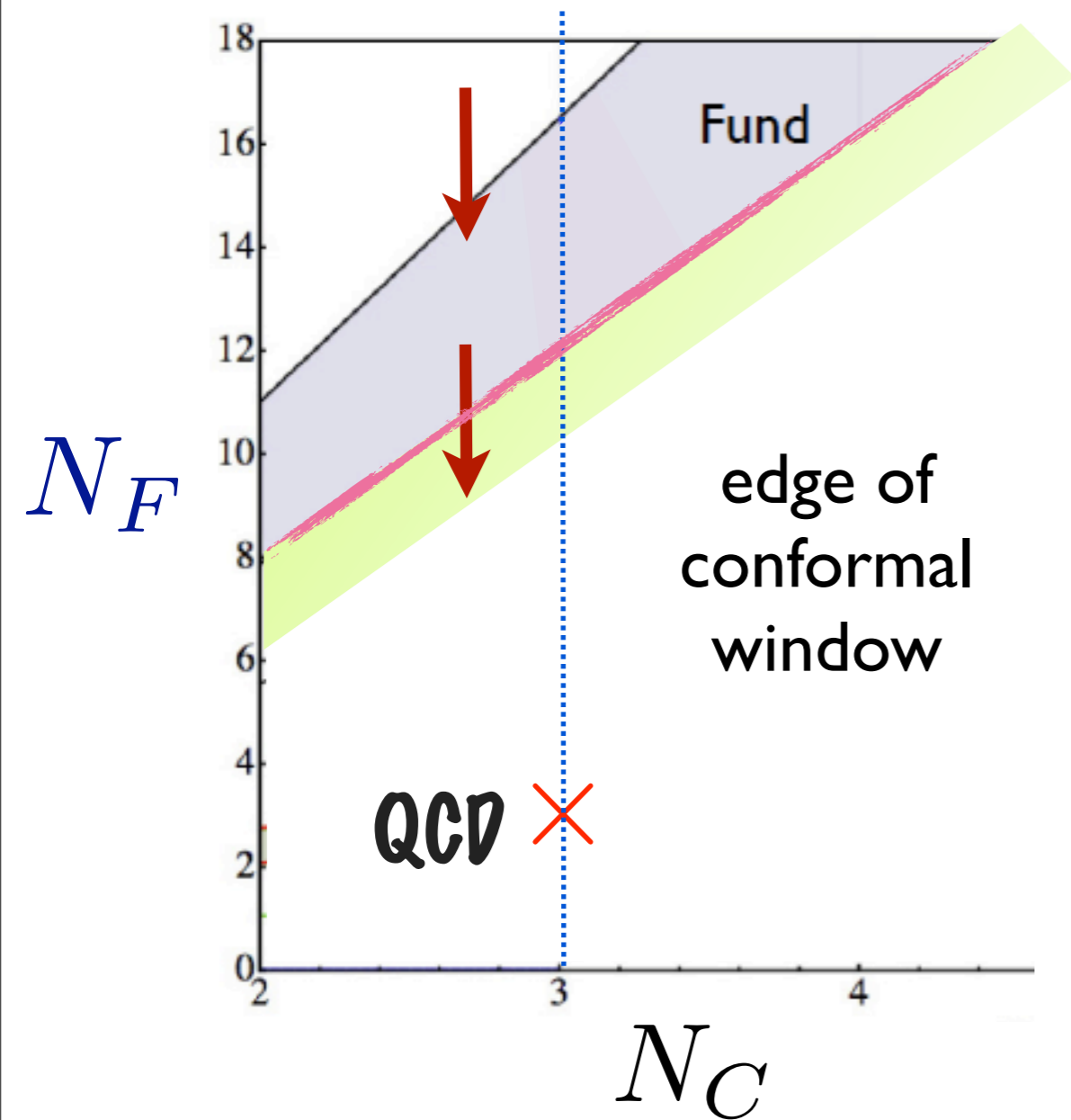
(near) conformal gauge theory  $\rightarrow$  separates scales



(Lane, Appelquist & Sannino)

BSM lattice has focused on studying this scenario

# conformal theory

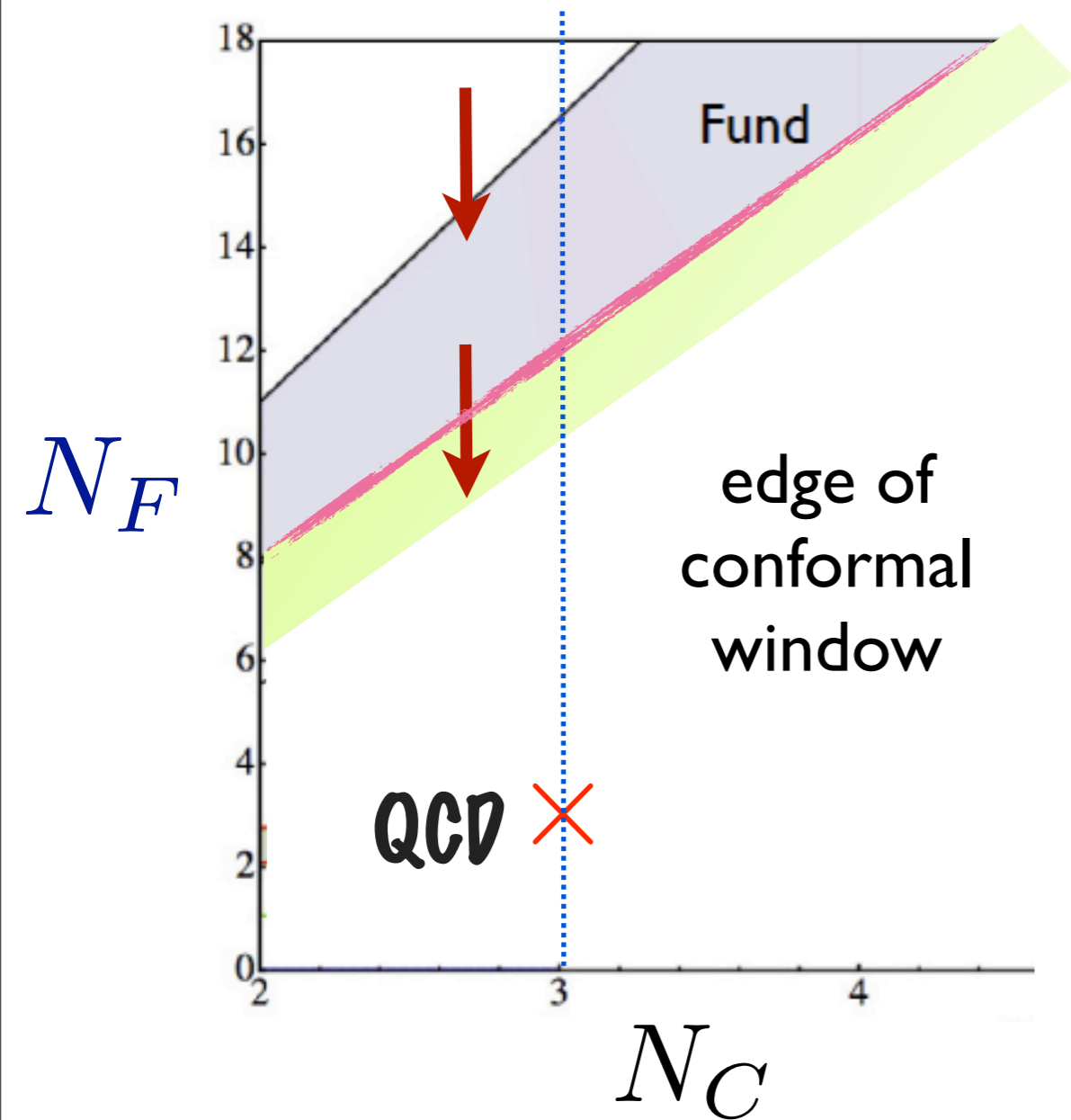


phase diagram has been the subject of numerous studies

figuring out which techniques work best



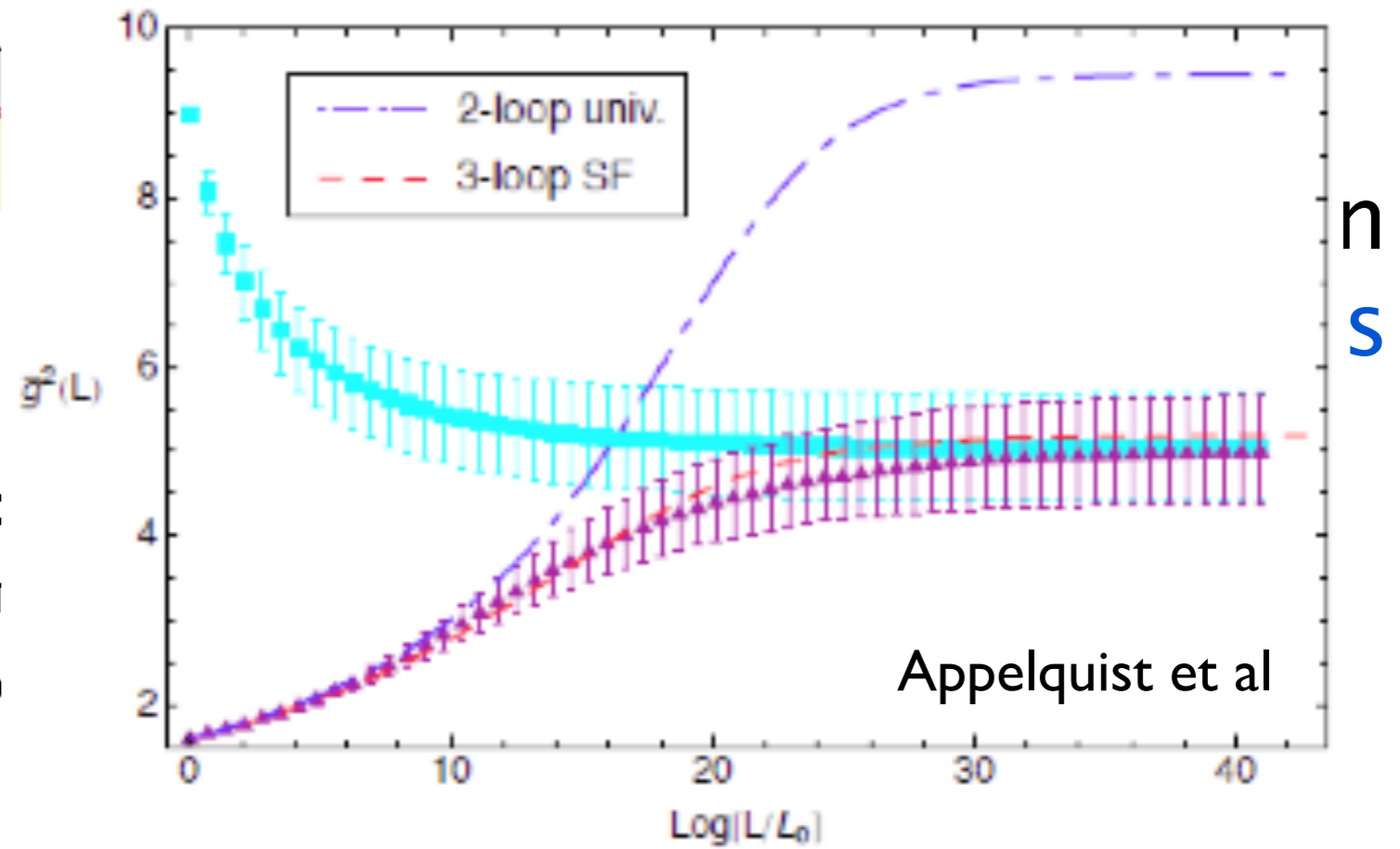
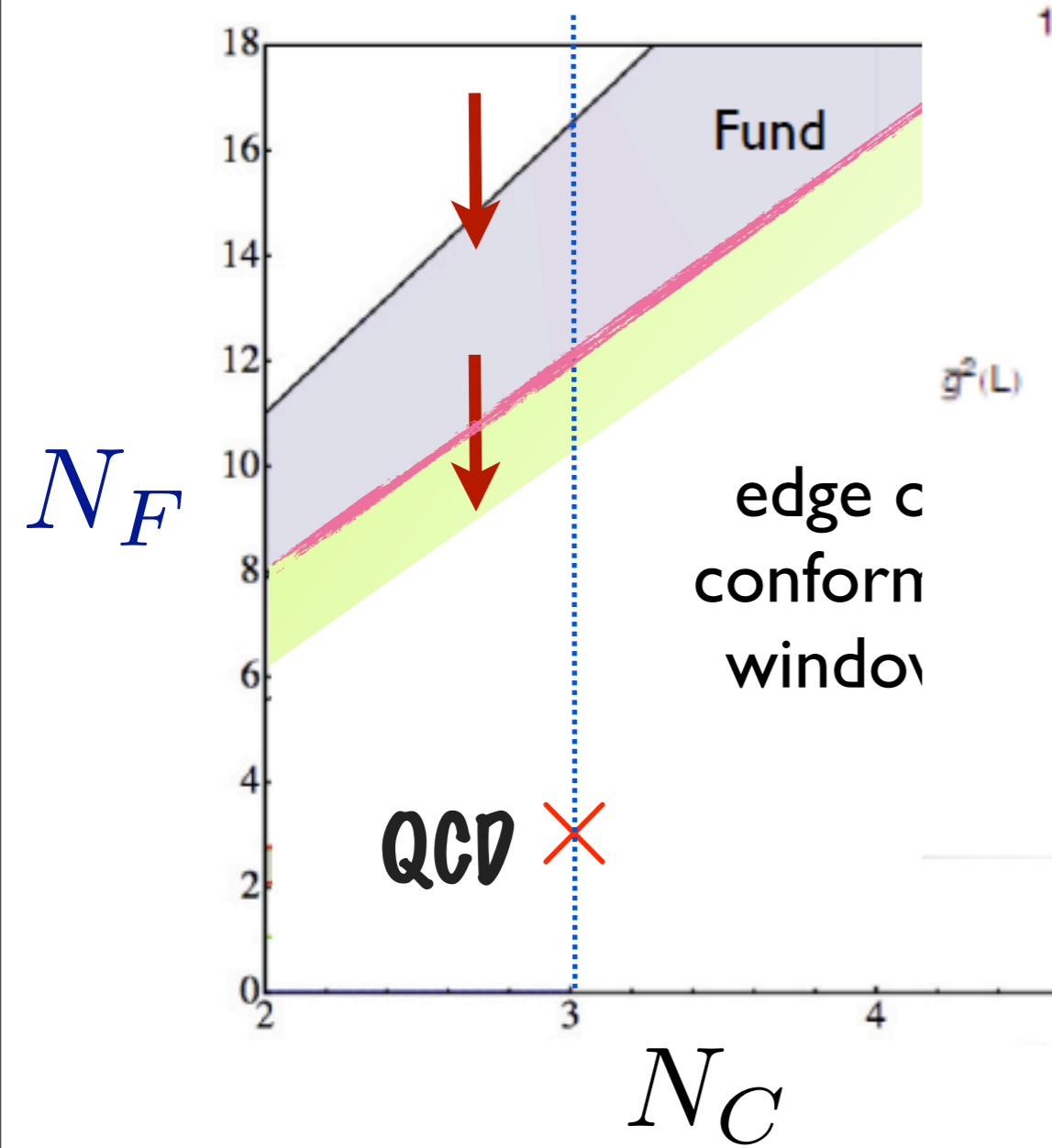
# conformal theory



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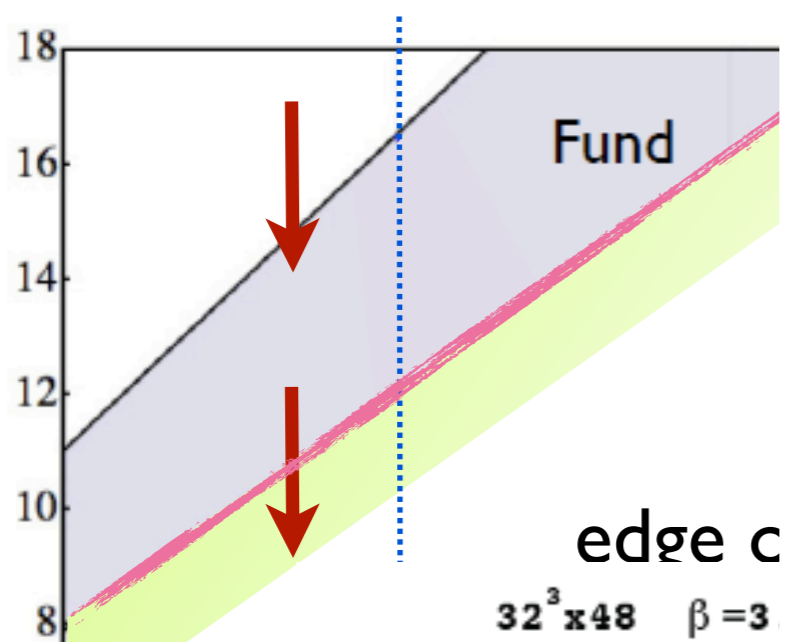
# conformal theory



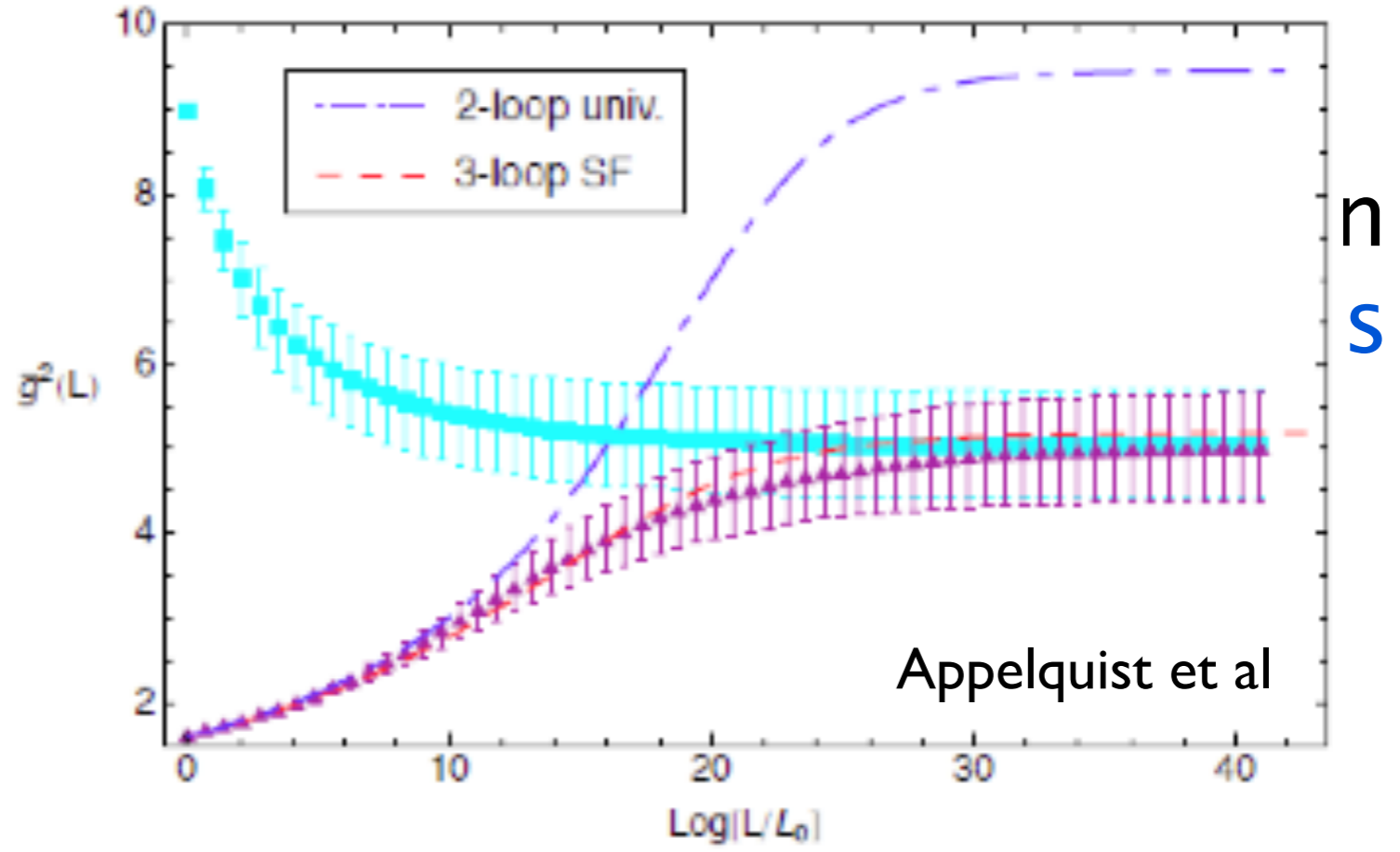
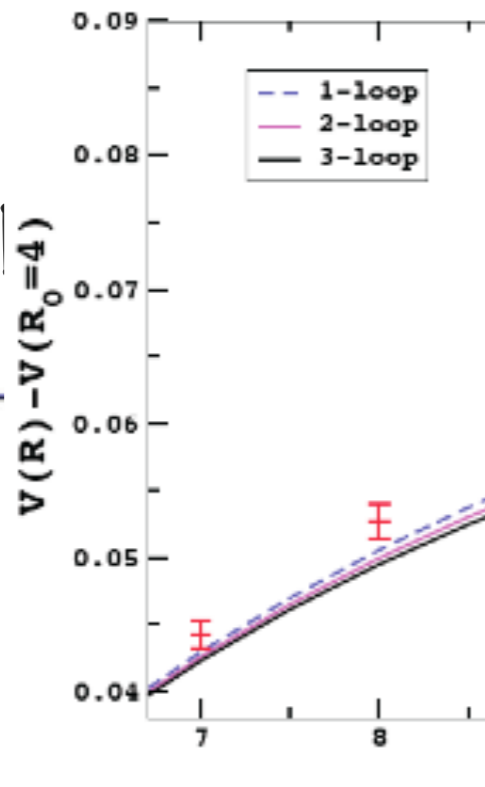
out which techniques work best

# conformal theory

$N_F$



QC

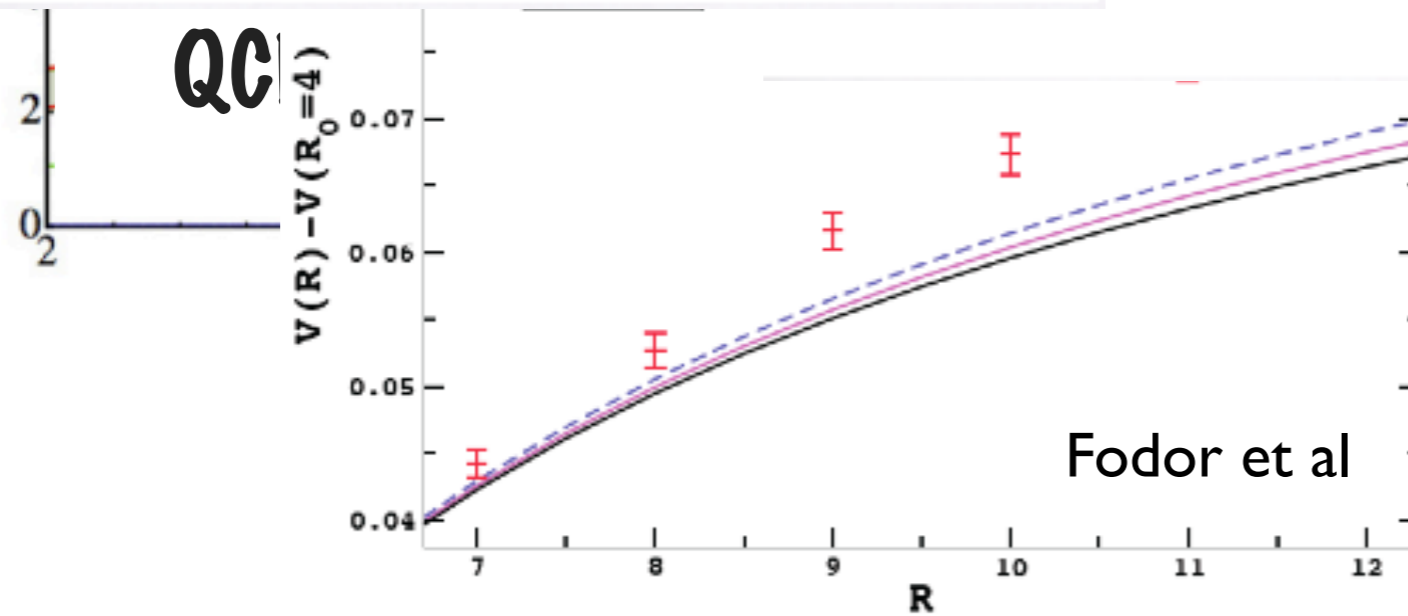
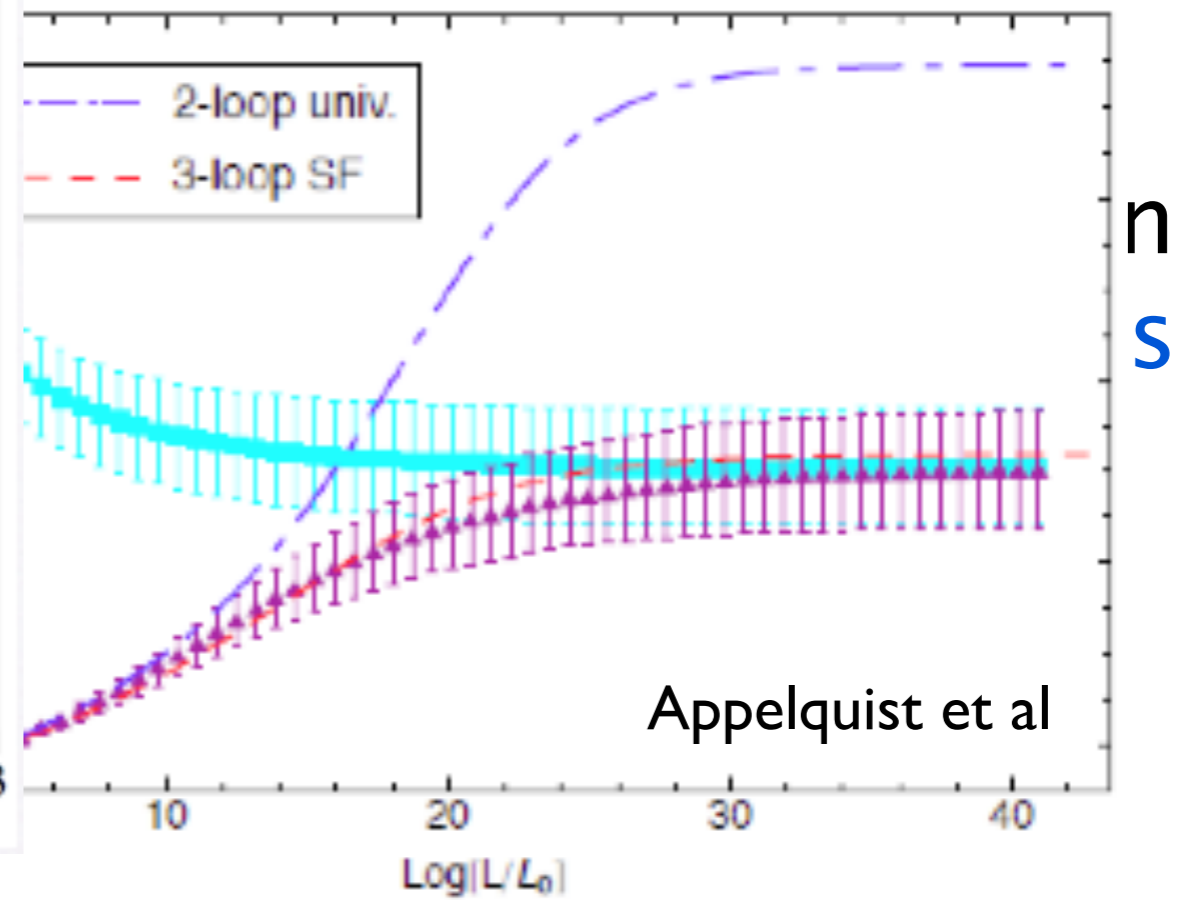
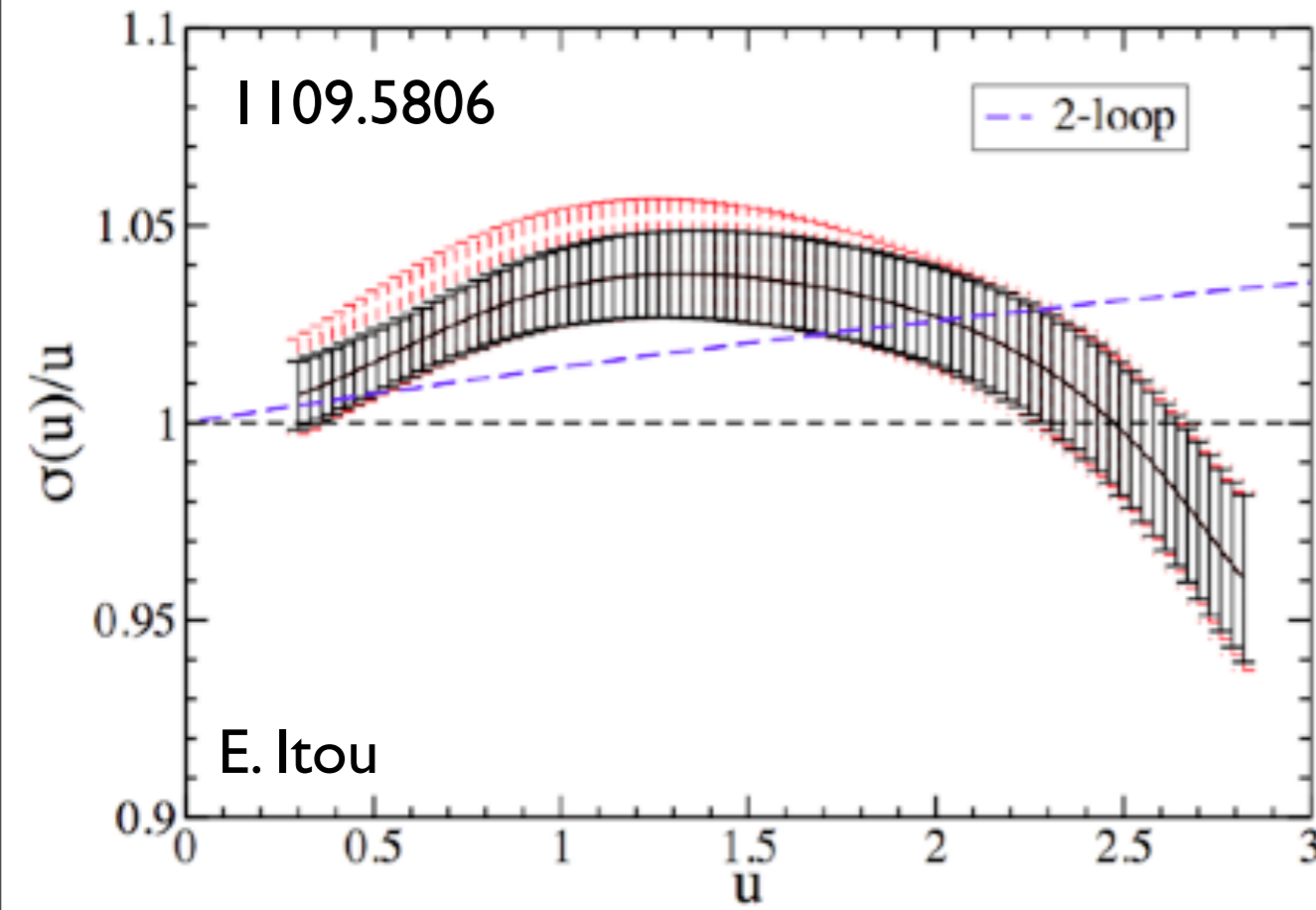


$n_s$

but which techniques work best

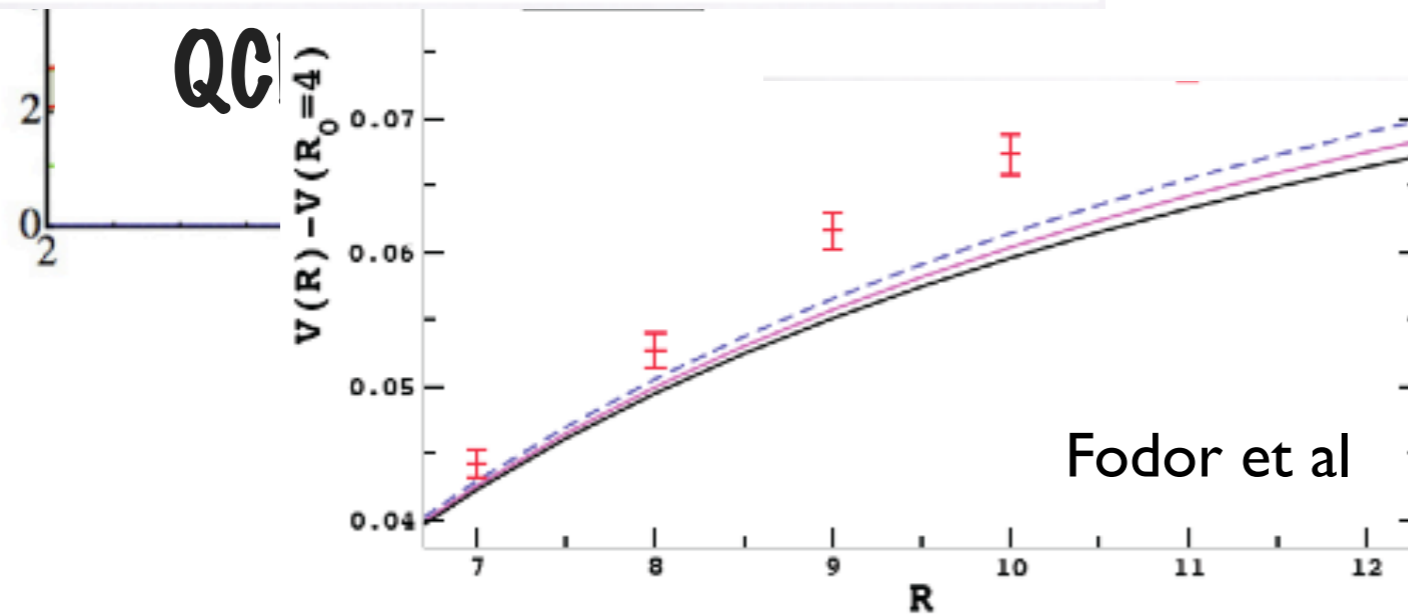
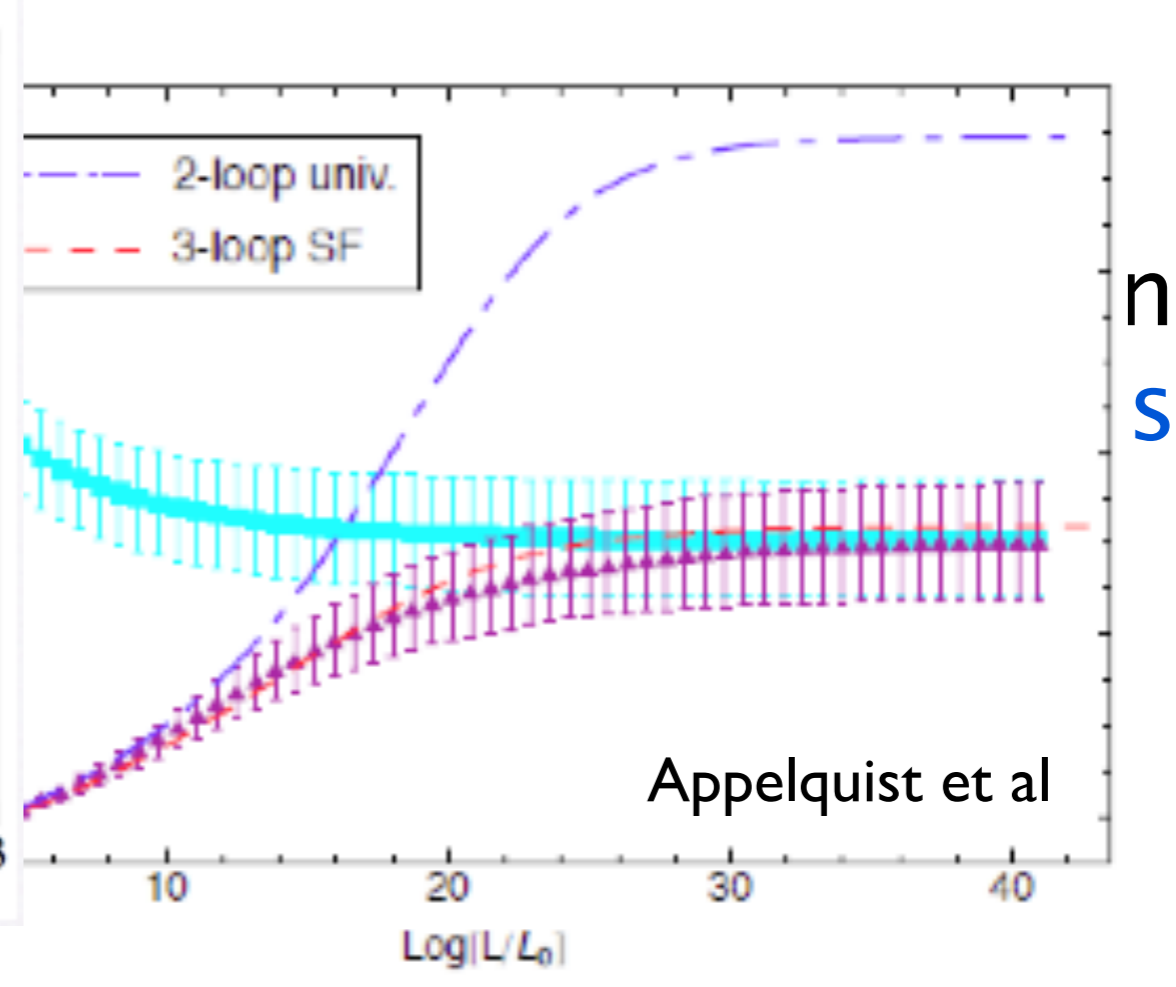
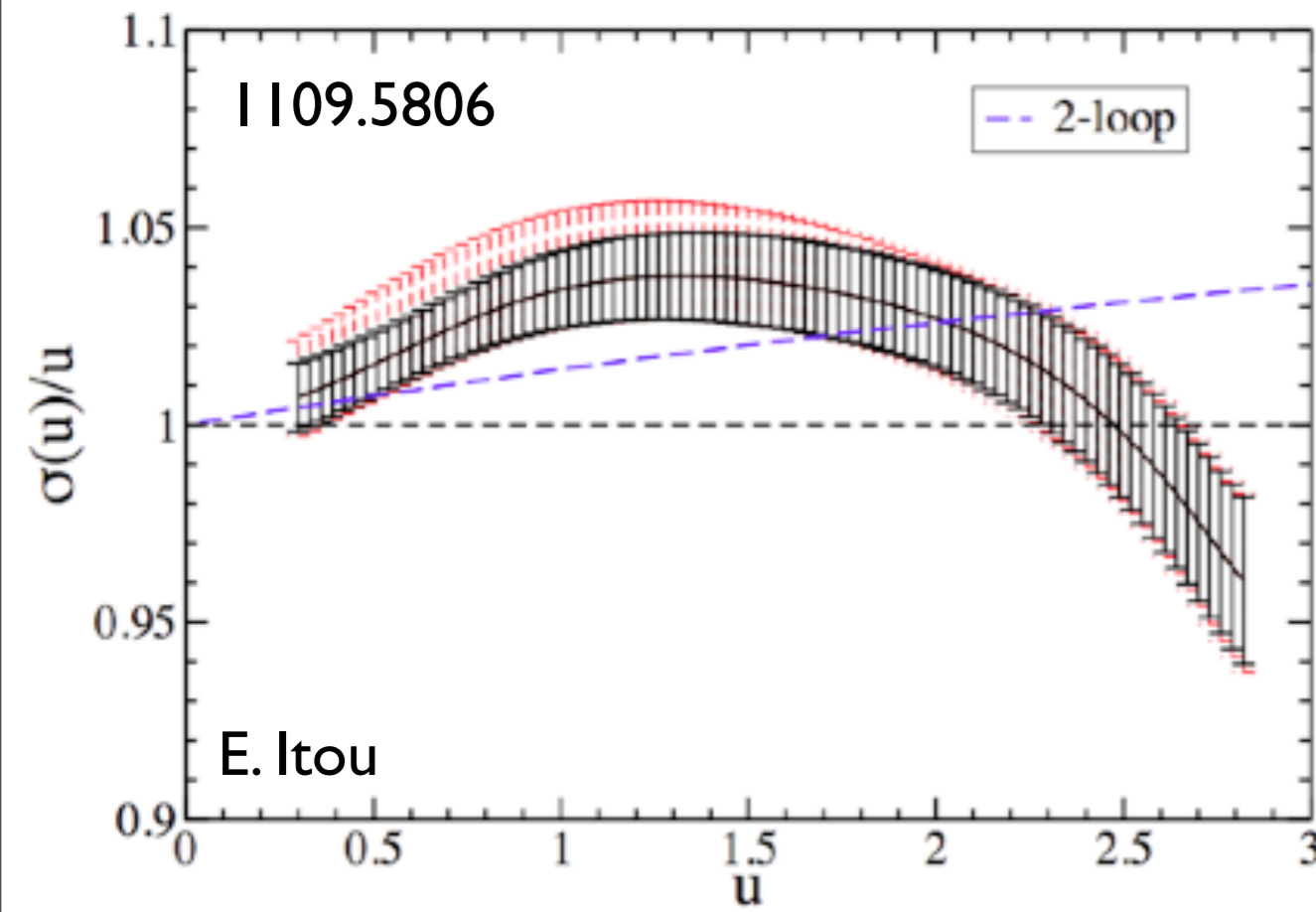
Fodor et al

# conformal theory



but which techniques work best

# conformal theory




but which techniques work best

once better understood, can study properties of near-conformal theories


# properties of $N_F \gg 3$ theories

ex.) anomalous dimension of  $\langle \bar{\psi} \psi \rangle$

generates  
fermion mass,  
want low  $\Lambda$

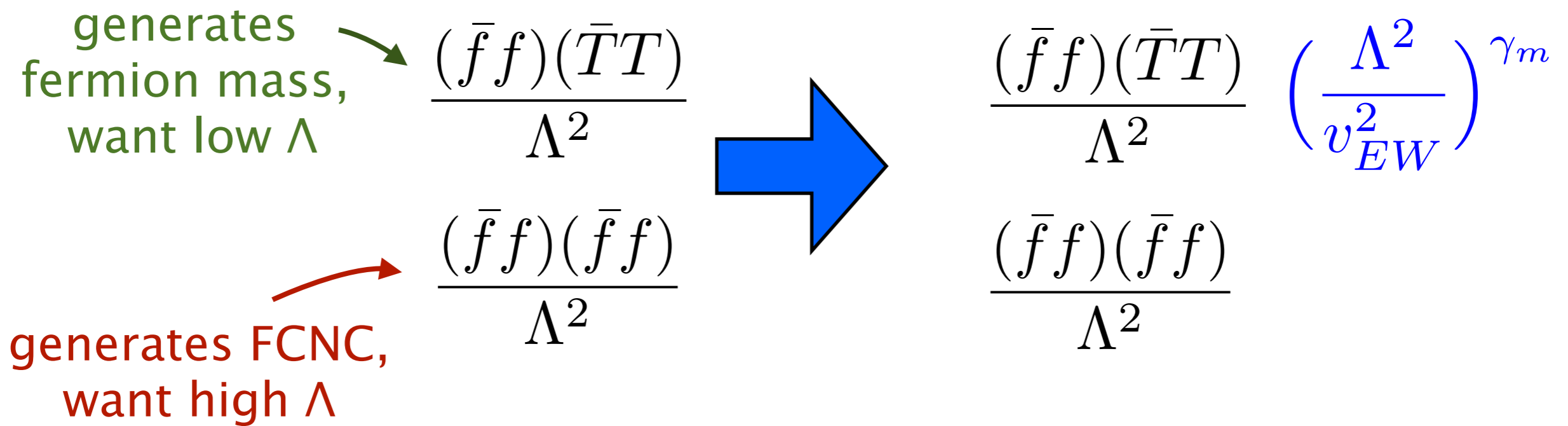

$$\frac{(\bar{f}f)(\bar{T}T)}{\Lambda^2}$$

generates FCNC,  
want high  $\Lambda$


$$\frac{(\bar{f}f)(\bar{f}f)}{\Lambda^2}$$

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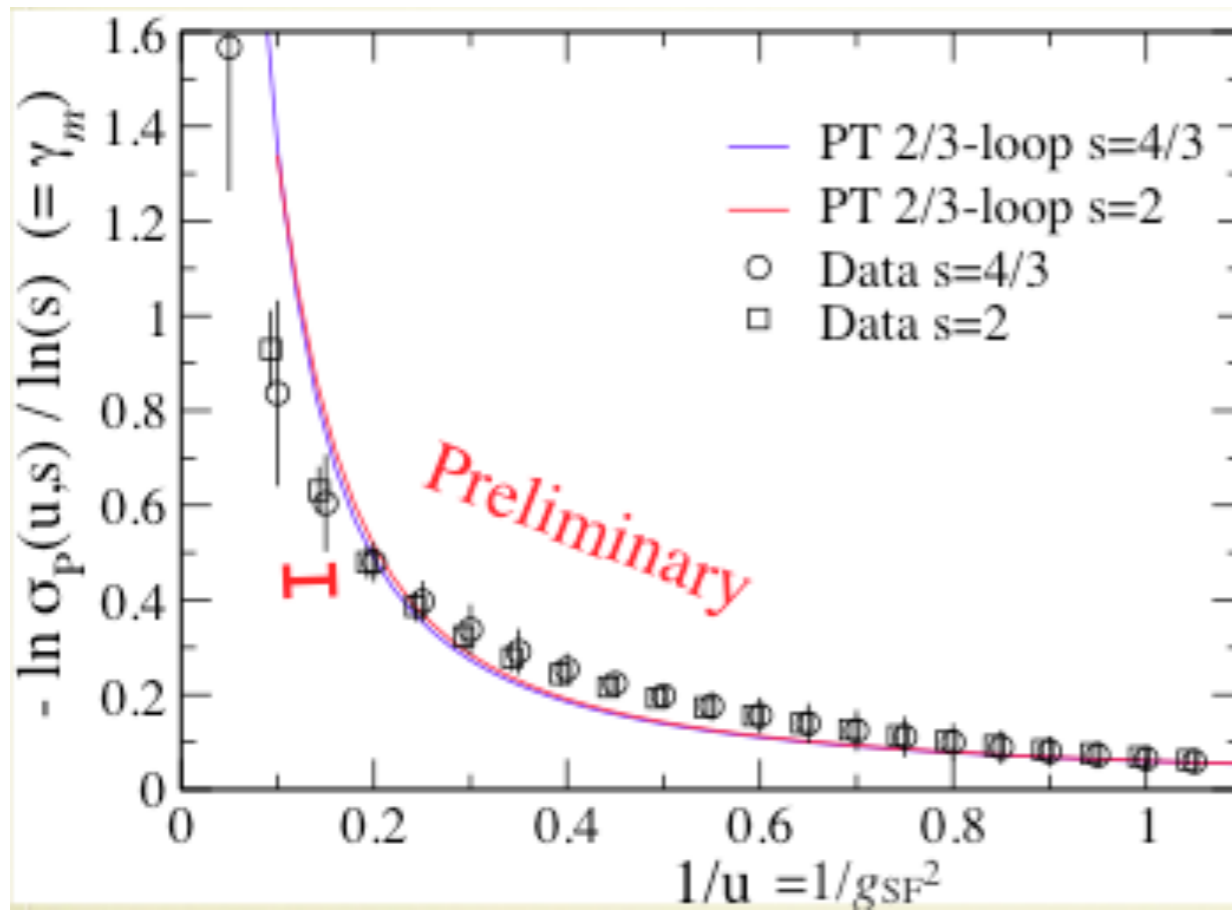
$$\frac{(\bar{f}f)(\bar{T}T)}{\Lambda^2} \quad \rightarrow \quad \frac{(\bar{f}f)(\bar{T}T)}{\Lambda^2} \left( \frac{\Lambda^2}{v_{EW}^2} \right)^{\gamma_m}$$
$$\frac{(\bar{f}f)(\bar{f}f)}{\Lambda^2}$$

what is  $\gamma_m$  in near conformal theories?



# properties of $N_F \gg 3$ theories

ex.) anomalous dimension of  $\langle \bar{\psi} \psi \rangle$



$N_F = 10$ , indications  
of  $\gamma_m \sim O(1)$

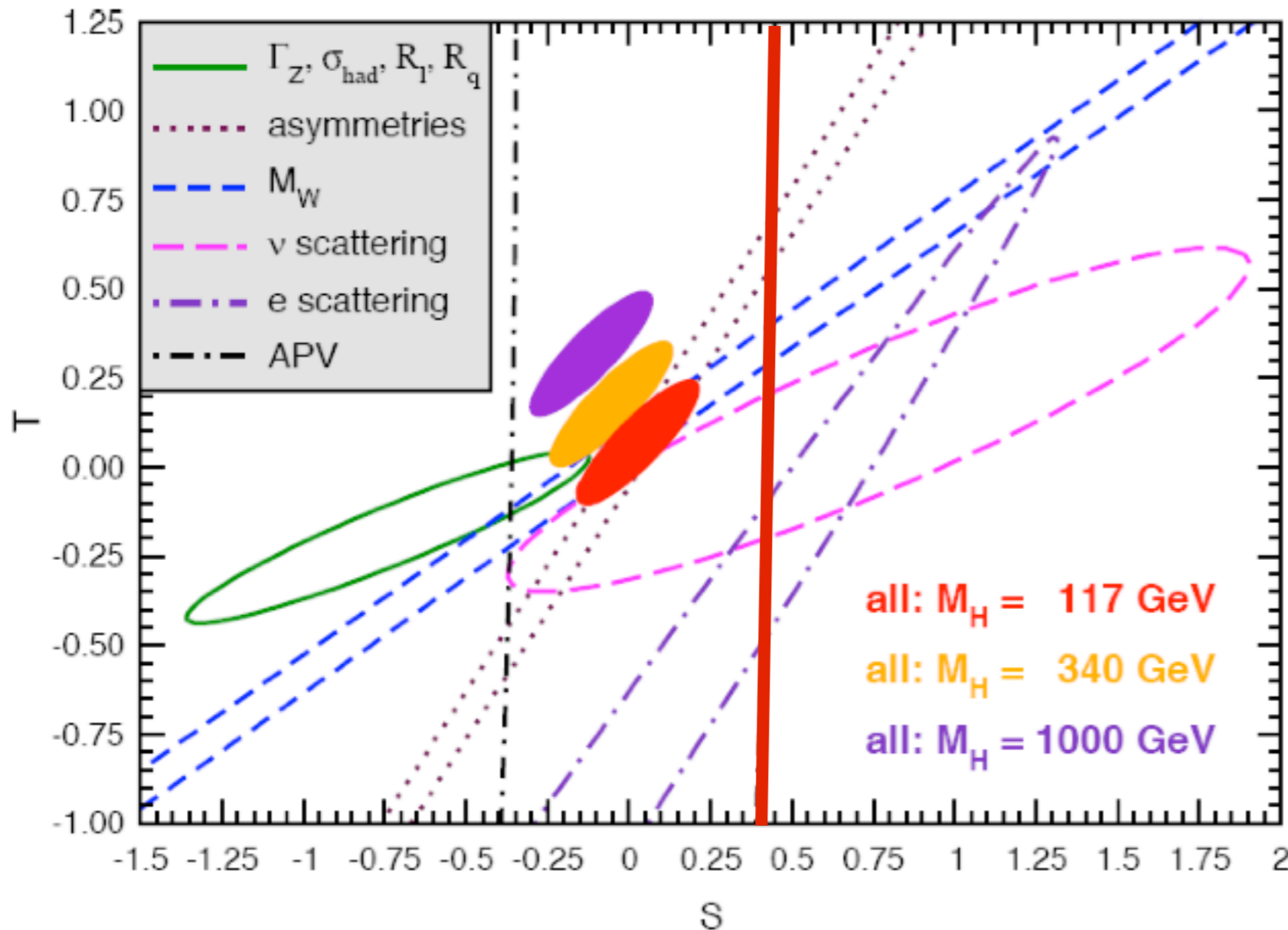
(N. Yamada)

can have  $\Lambda$  that satisfy flavor  
constraints, while generating  
realistic fermion masses

# properties of $N_F \gg 3$ theories

precision electroweak parameters:

if TeV-scale dynamics is QCD-like, expect  $S \sim 0.3$

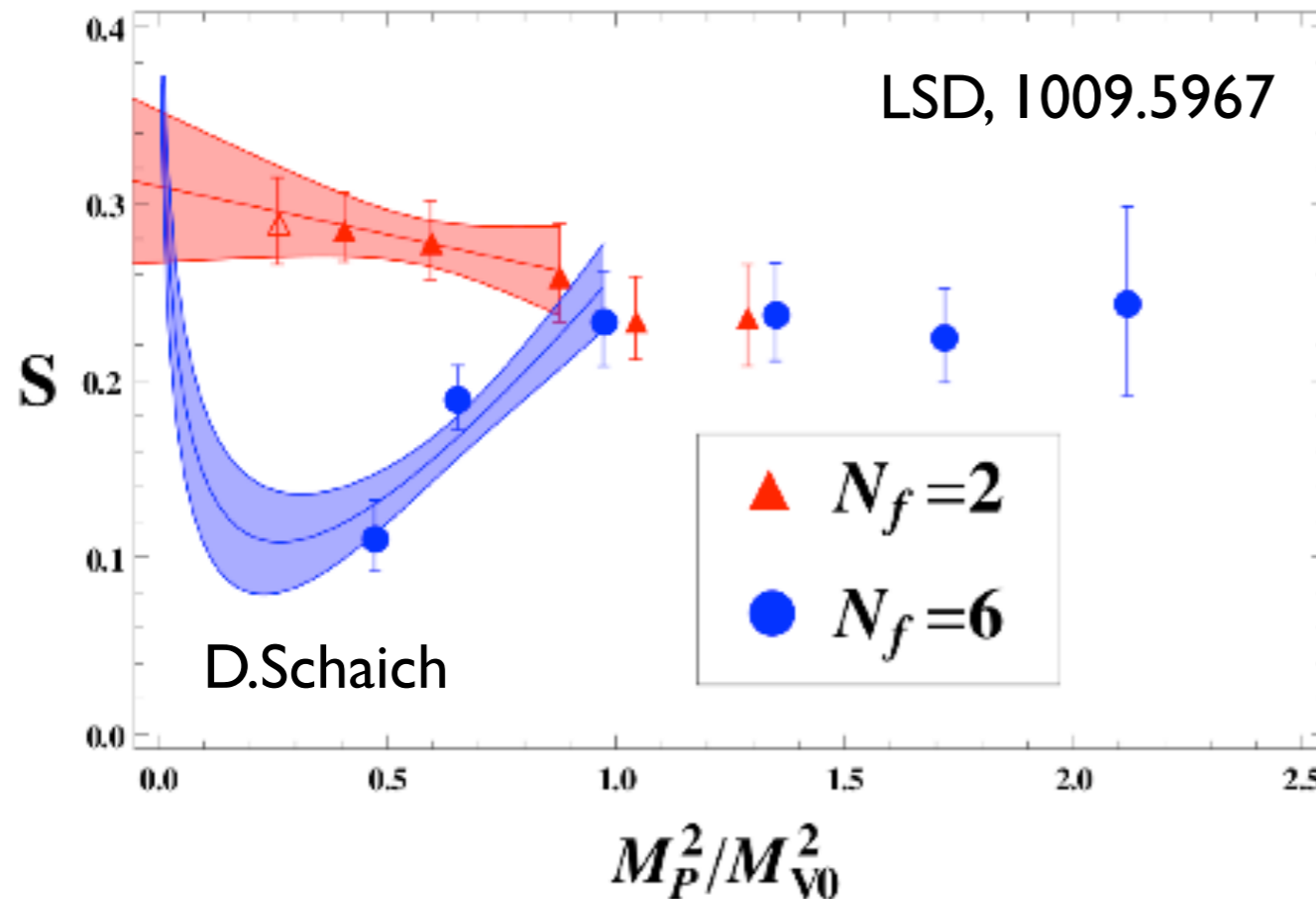


what about in a  
near-conformal  
theory?

$$S = 4\pi N_D \lim_{Q^2 \rightarrow 0} \frac{d}{dQ^2} \Pi_{V-A}(Q^2) - \Delta S_{SM}$$

# properties of $N_F \gg 3$ theories

indications that  $S$  (per EW doublet) can be small



points the way for model-building:

- 1 chiral EW doublet (all you need)
- $N_F-1$  vector-like doublets or singlets

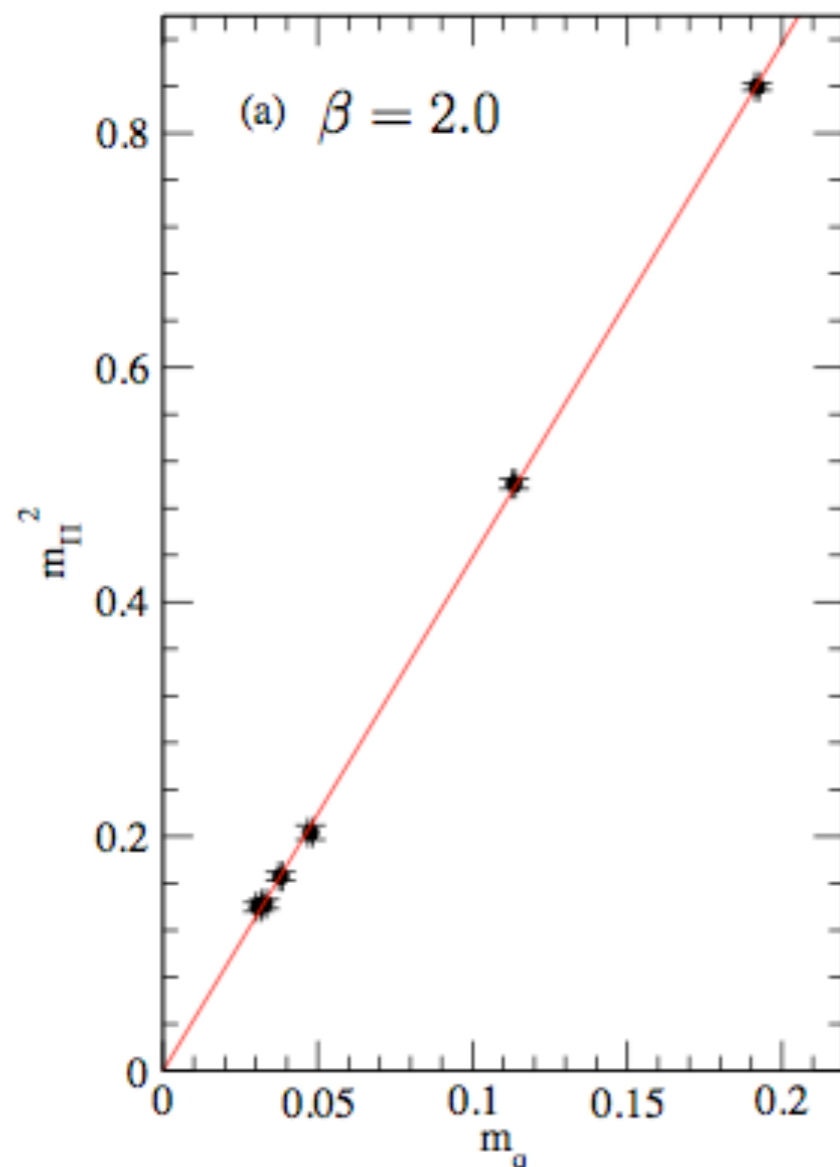
and phenomenology:

small  $S$  tied to  $\sim$ restoration of parity doubling in spectra

# Other directions

other patterns of chiral symmetry breakdown

we're most familiar with  $SU(N) \times SU(N) \rightarrow SU(N)$ ,  
but what about  $SU(N) \rightarrow SO(N)$  or  $Sp(N)$



commonly used in  
**composite Higgs**  
models

study of  
 $SU(4)/Sp(4)$   
breaking  
(R. Lewis 1109.3513)

# Other directions

role of four-fermion operators

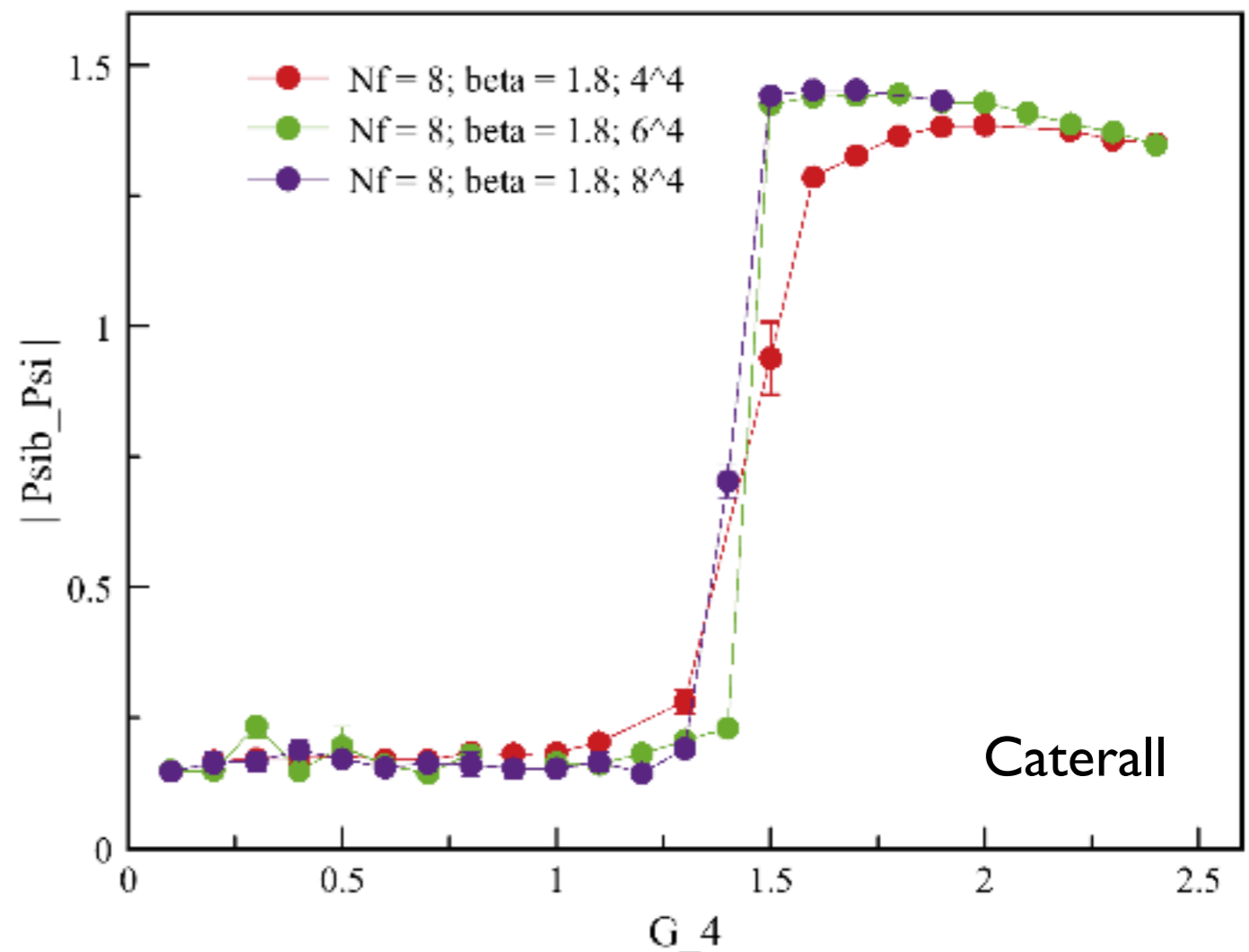
$$S = \int d^4x \bar{\psi}(i\partial - A)\psi + \underbrace{\frac{G^2}{2} [(\bar{\psi}\psi)^2 + (\bar{\psi}i\gamma_5\tau^a\psi)^2]} - \frac{1}{2g^2} \text{Tr}[F_{\mu\nu}F^{\mu\nu}]$$

expected/necessary in all models of BSM strong dynamics

‘gauged NJL’ model

chiral symmetry  
breaking at large  $G$

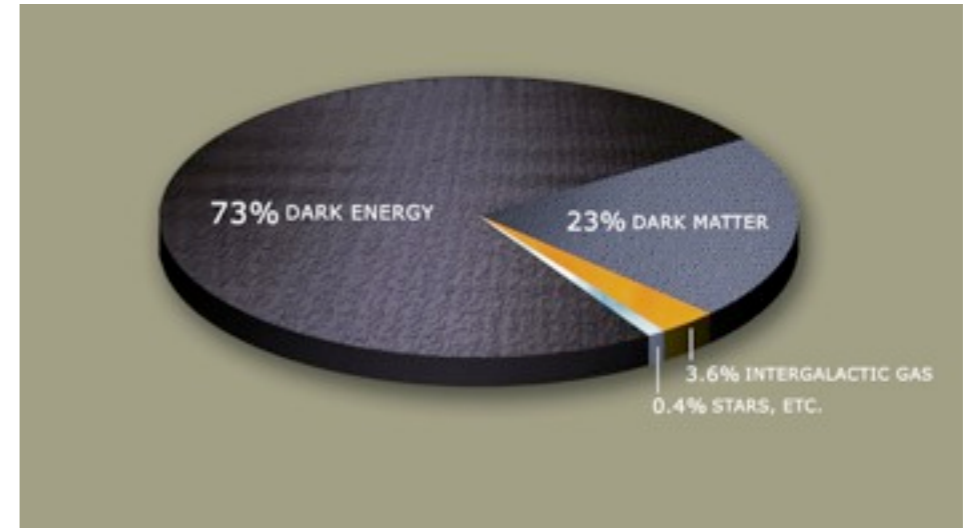
interesting to extend  
to more flavors,  
complexity



# Other directions

## technicolor & Dark Matter:

- lightest technibaryon can be stable by analog of  $U(1)_B$
- an initial matter/anti-matter asymmetry gets shared among baryons, leptons, technibaryons via sphalerons
- can get observed  $\Omega_{DM}/\Omega_B$  easily for  $\sim$  TeV scale DM  
must be electrically neutral, EW singlets to avoid direct detection  
Then leading operators are **charge radius** and **polarizability**:



(Chivukula, Barr, Fahri, Nussinov)

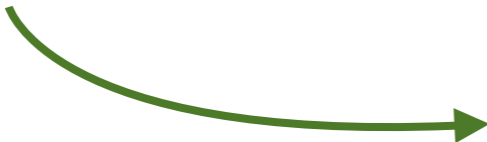
$$\text{ex.) } \frac{B^* B v_\mu \partial_\nu F^{\mu\nu}}{\Lambda_{TC}^2}, \frac{B^* B F_{\mu\nu} F^{\mu\nu}}{\Lambda_{TC}^3}$$

**lattice input?**

# BSM $\leftrightarrow$ lattice wish list (~few years)

- continue search for best techniques for study of near-CFT ( ex.)  $N_F, N_C$  phase diagram )
- $0^{++}$  state? a dilaton associated with approximate scale invariance?
- baryon spectroscopy in non-QCD scenarios
- more complex gauged NJL scenarios
  
- S-parameter
- WW-scattering, additional coefficients in EW-chiral Lagrangian

# Conclusions

- lattice is an invaluable tool to studying viable models of TeV-scale strong dynamics
- focus so far on conformal/near conformal theories  
difficult problem, still learning which techniques/tools work best
- insight into properties/spectra in these theories  
 input to model building and collider physics

**LOTS TO DO!**